

Nuclear Parton Densities

status & future avenues

Marco Stratmann

BROOKHAVEN
NATIONAL LABORATORY

marco@bnl.gov

work done in collaboration with D. de Florian, R. Sassot, and P. Zurita: **PRD85 (2012) 074028**
(arXiv:1112.6324)

Outline

- ❑ **Nuclear PDFs 101**
framework, experimental input, main features of nPDFs
- ❑ **strategies to parametrize nPDFs**
overview of existing analyses, issues
- ❑ **results of our new global QCD analysis**
what is new, some technical aspects, comparison to data & other fits
- ❑ **future avenues in dA (pA) collisions at RHIC (LHC)**
prompt photons, Drell Yan

foundation: pQCD & factorization

QCD improved parton model – a success story ever since

- describes quantitatively a large variety of hard processes in e^+e^- , ep, pp, ...

- key assumption:** factorization of long- and short-distance physics
corrections: inverse powers of large scale

$$\frac{d\sigma}{dp_T} = \sum_{ab} \underbrace{f_a(x_a, \mu) \otimes f_b(x_b, \mu)}_{\text{from experiment}} \otimes \underbrace{d\hat{\sigma}_{ab}(\mu)}_{\text{calculable}} + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$

- predictive power
- systematic framework** to compute higher order corrections
NLO standard; NNLO known or on the horizon

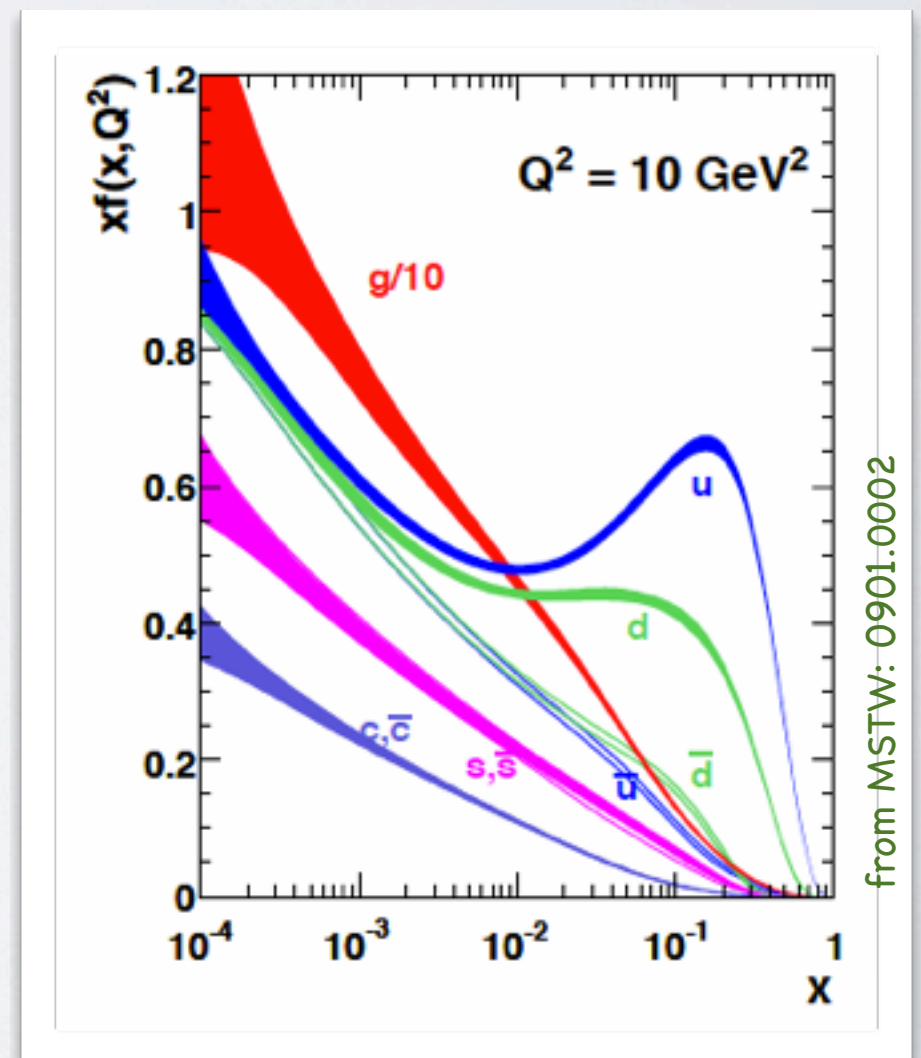
foundation: pQCD & factorization

QCD improved parton model – a success story ever since

- describes quantitatively a large variety of hard processes in e^+e^- , ep, pp, ...
- key assumption:** **factorization** of long- and short-distance physics
 corrections: inverse powers of large scale
- predictive power
- systematic framework** to compute higher order corrections
 NLO standard; NNLO known or on the horizon
- small amount of phenomenological parameters to be determined from data
parton densities, masses, α_s , fragmentation fcts.

parton content of **free** protons
 rather well known by now in broad x, Q^2 range
 some fine details are missing though

$$\frac{d\sigma}{dp_T} = \sum_{ab} \underbrace{f_a(x_a, \mu)}_{\text{from experiment}} \otimes \underbrace{f_b(x_b, \mu)}_{\text{from experiment}} \otimes \underbrace{d\hat{\sigma}_{ab}(\mu)}_{\text{calculable}} + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$



PDFs for bound nucleons

main idea:

- keep standard pQCD framework and **assume factorization** also for nuclei $\frac{d\sigma}{dp_T} = \sum_{ab} f_a(\mathbf{x}_a, \mu) \otimes f_b(\mathbf{x}_b, \mu) \otimes d\hat{\sigma}_{ab}(\mu) + \mathcal{O}\left(\frac{1}{p_T^n}\right)$

PDFs for bound nucleons

main idea:

- keep standard pQCD framework and **assume factorization** also for nuclei

$$\frac{d\sigma}{dp_T} = \sum_{ab} f_a(x_a, \mu) \otimes f_b^A(x_b, \mu) \otimes d\hat{\sigma}_{ab}(\mu) + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$

pp → pA collisions

introduce **universal nuclear PDF**

PDFs for bound nucleons

main idea:

- keep standard pQCD framework and **assume factorization** also for nuclei

$$\frac{d\sigma}{dp_T} = \sum_{ab} f_a(x_a, \mu) \otimes f_b^A(x_b, \mu) \otimes d\hat{\sigma}_{ab}(\mu) + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$

pp → pA collisions

introduce **universal nuclear PDF**

dictates use of same

- DGLAP scale evolution
- hard scattering cross sections as for free proton PDFs

PDFs for bound nucleons

main idea:

- keep standard pQCD framework and **assume factorization** also for nuclei

$$\frac{d\sigma}{dp_T} = \sum_{ab} f_a(x_a, \mu) \otimes \underbrace{f_b^A(x_b, \mu)}_{\text{introduce universal nuclear PDF}} \otimes d\hat{\sigma}_{ab}(\mu) + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$

pp → pA collisions

dictates use of same

- DGLAP scale evolution
- hard scattering cross sections as for free proton PDFs



all nuclear effects are universally absorbed into a set of non-perturbative nPDFs independent of the hard probe

PDFs for bound nucleons

main idea:

- keep standard pQCD framework and **assume factorization** also for nuclei

$$\frac{d\sigma}{dp_T} = \sum_{ab} f_a(x_a, \mu) \otimes \underbrace{f_b^A(x_b, \mu)}_{\text{introduce universal nuclear PDF}} \otimes d\hat{\sigma}_{ab}(\mu) + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$

pp → pA collisions

dictates use of same

- DGLAP scale evolution
- hard scattering cross sections as for free proton PDFs



all nuclear effects are universally absorbed into a set of non-perturbative nPDFs independent of the hard probe

- very restrictive framework which makes testable predictions for a slew of hard probes

PDFs for bound nucleons

main idea:

- keep standard pQCD framework and **assume factorization** also for nuclei

$$\frac{d\sigma}{dp_T} = \sum_{ab} f_a(x_a, \mu) \otimes \underbrace{f_b^A(x_b, \mu)}_{\text{introduce universal nuclear PDF}} \otimes d\hat{\sigma}_{ab}(\mu) + \mathcal{O}\left(\frac{1}{p_T^n}\right)$$

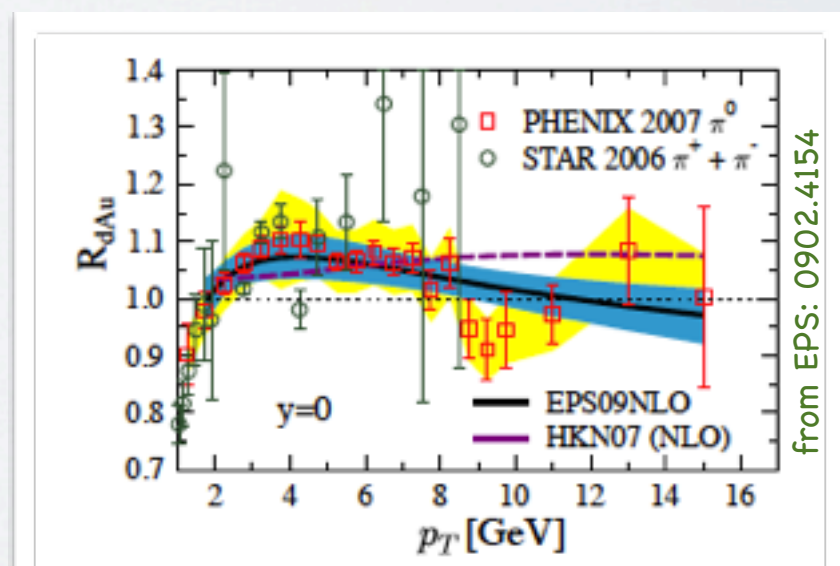
pp → pA collisions

dictates use of same

- DGLAP scale evolution
- hard scattering cross sections as for free proton PDFs

all nuclear effects are universally absorbed into a set of non-perturbative nPDFs independent of the hard probe

- very restrictive framework which makes testable predictions for a slew of hard probes
- **complication** (often happily ignored): nuclear modifications of final-state hadrons hard to accommodate (modified fragmentation?)



nuclear PDFs: what do we expect to learn ?

factorization and/or DGLAP evolution will eventually break down – so what?

nuclear PDFs: what do we expect to learn ?

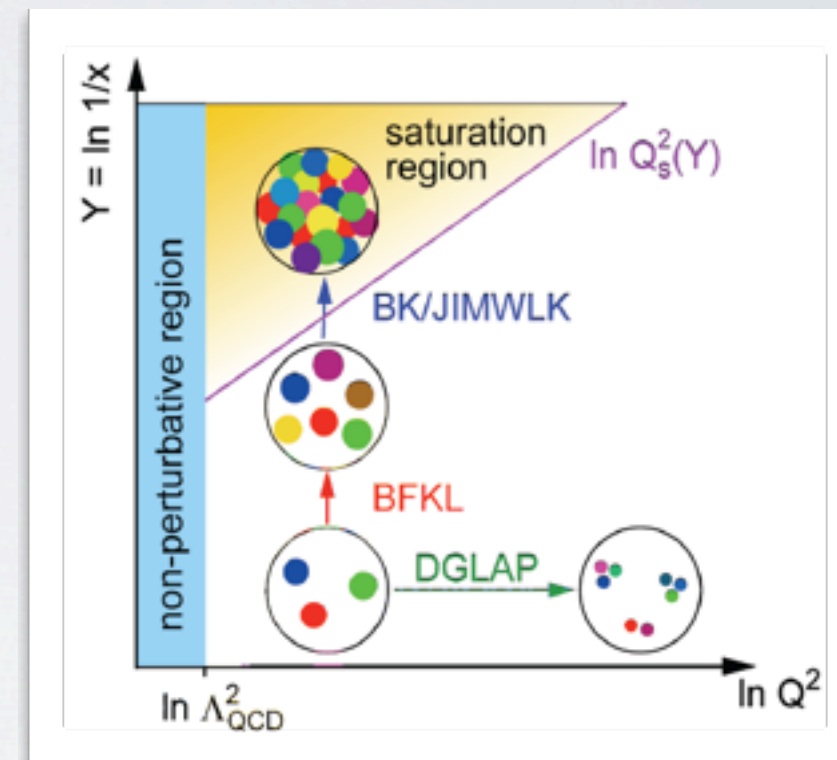
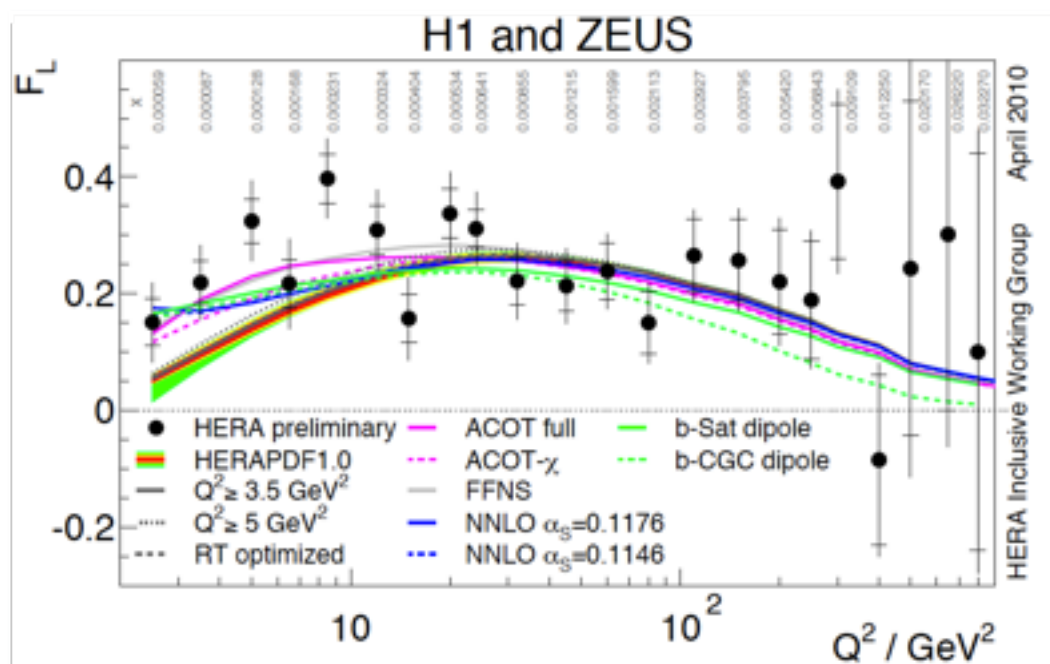
factorization and/or DGLAP evolution will eventually break down – so what?

- nPDFs can parametrize nuclear effects with little bias and without assuming certain “mechanisms” to model the observed modifications/effects
link to models of nucleon structure at low scales and proposed nuclear modifications
- a global QCD analysis of many hard probes will reveal tensions due to the assumed framework (linear DGLAP / factorization)

nuclear PDFs: what do we expect to learn ?

factorization and/or DGLAP evolution will eventually break down - so what?

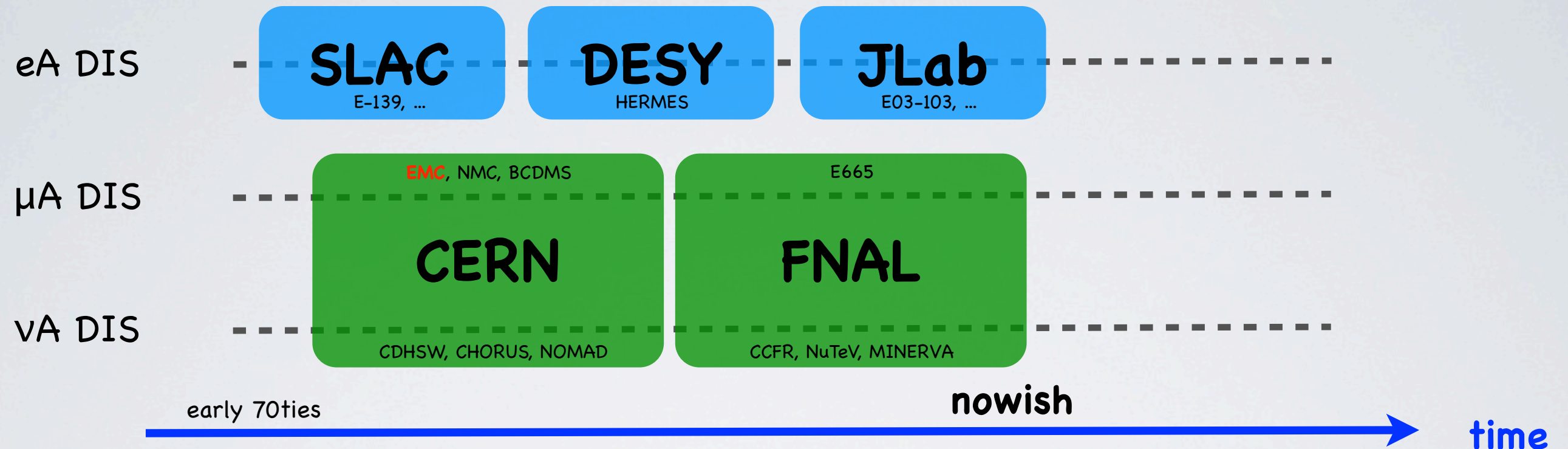
- nPDFs can parametrize nuclear effects with little bias and without assuming certain “mechanisms” to model the observed modifications/effects
link to models of nucleon structure at low scales and proposed nuclear modifications
- a global QCD analysis of many hard probes will reveal tensions due to the assumed framework (linear DGLAP / factorization)
- map out kinematic regime where nPDF framework applies and study transition to saturation region
 - ▶ transition often characterized by “saturation scale” $Q_s(x,A)$
 - ▶ non-linear effects (recombination) demanded by unitarity



- ▶ no unambiguous hints for saturation in ep down to $x = 10^{-5}$
- ▶ most promising so far: RHIC hadron yields in dAu collisions
- ▶ effects amplified in eA/pA collisions; “nuclear oompf” $\propto A^{1/3}$

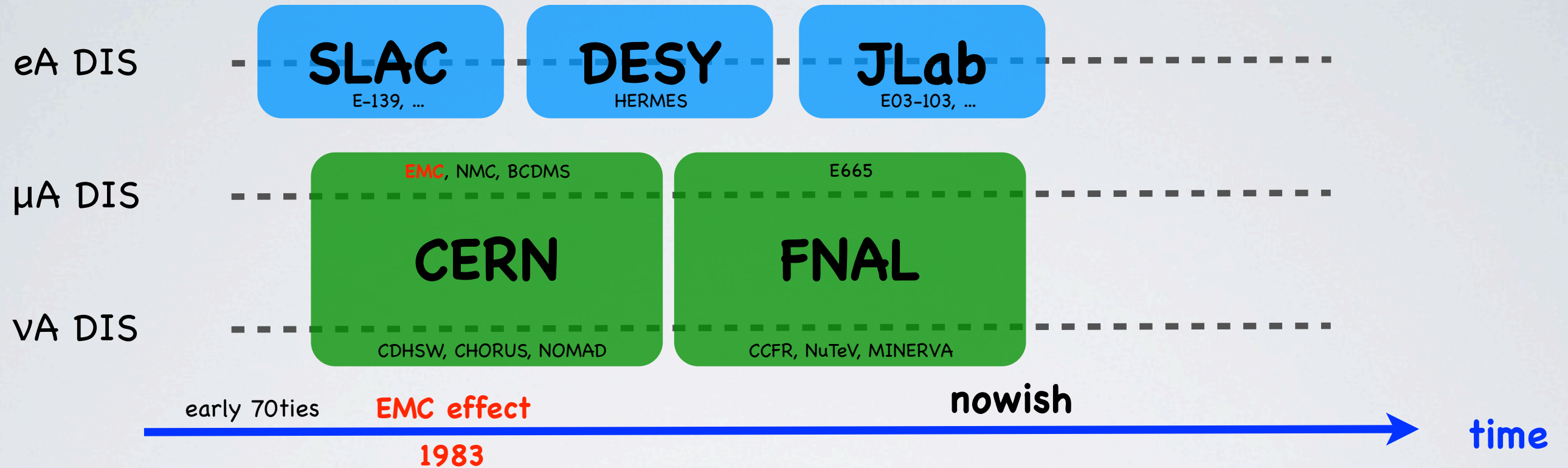
experimental input

thriving experimental programs since the early seventies



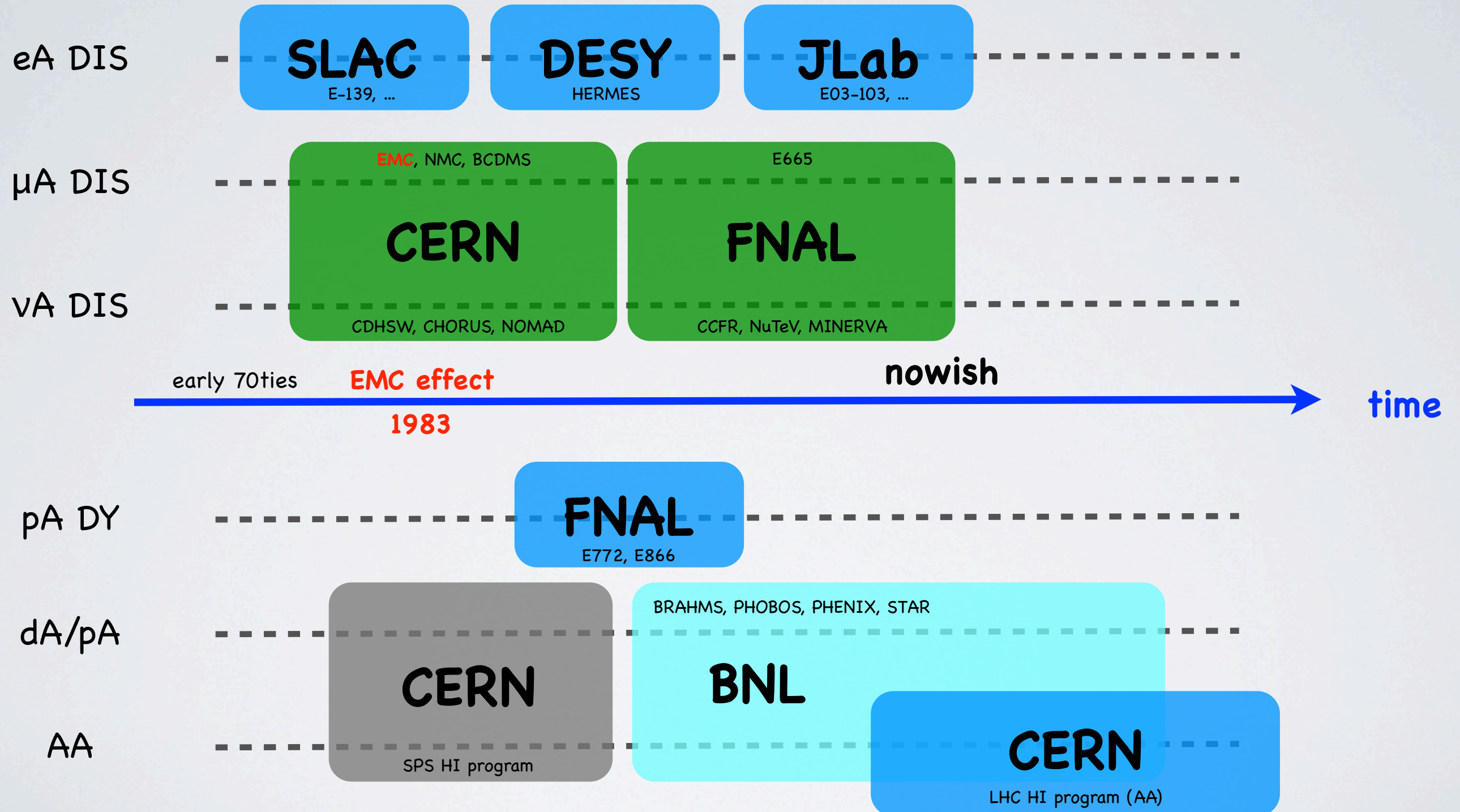
experimental input

thriving experimental programs since the early seventies



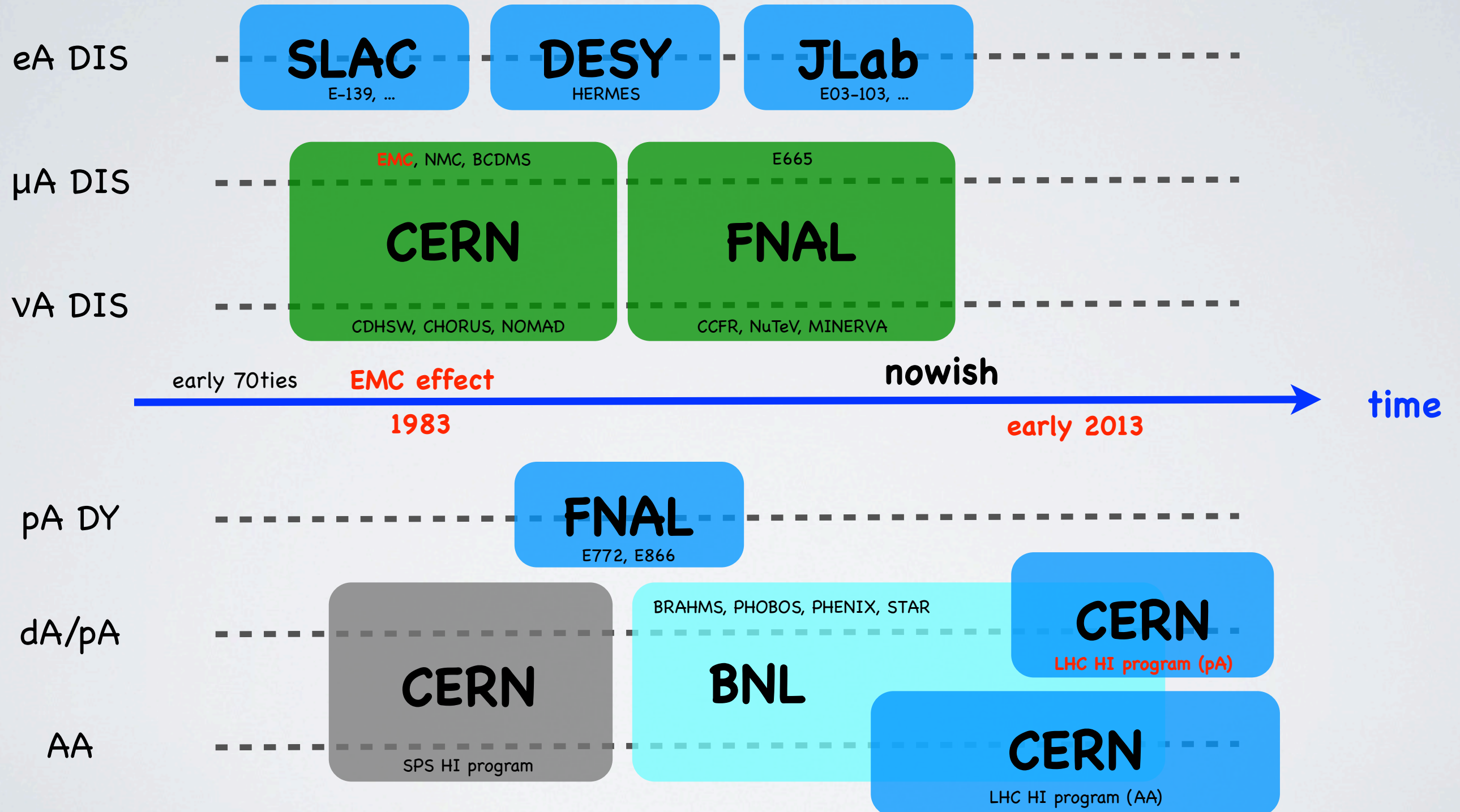
experimental input

thriving experimental programs since the early seventies



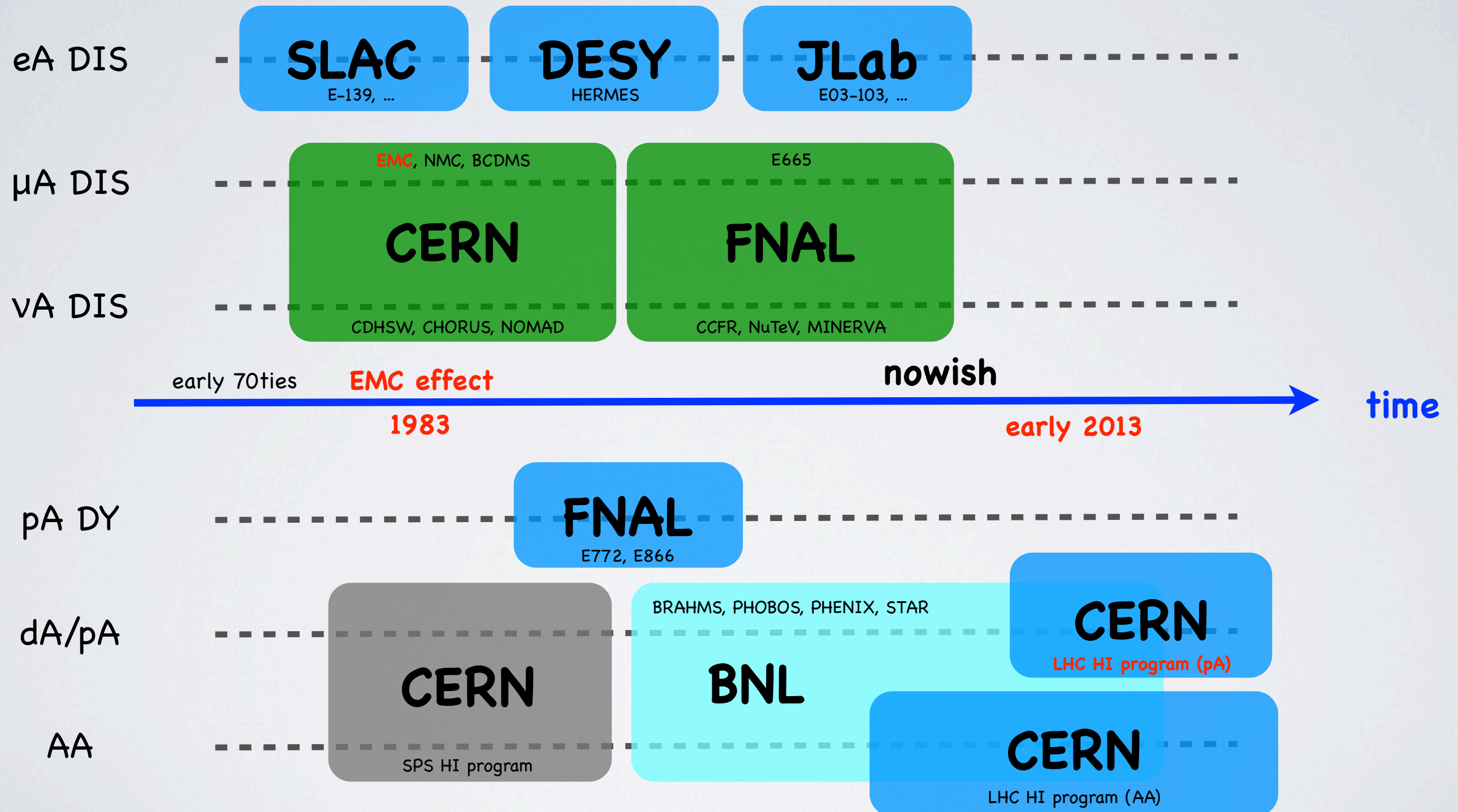
experimental input

thriving experimental programs since the early seventies



experimental input

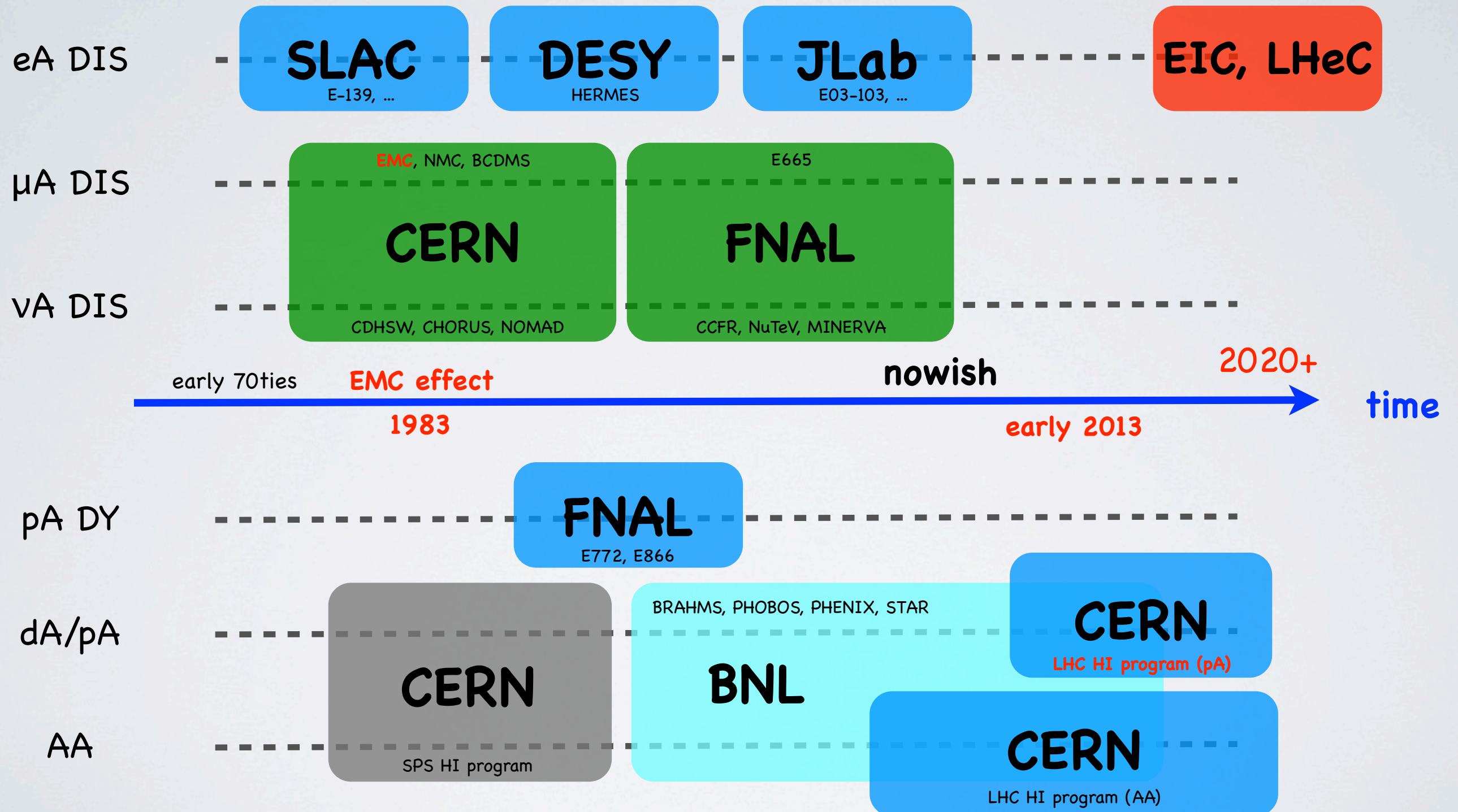
thriving experimental programs since the early seventies



biggest obstacle for nPDF analysis: no eA collider yet

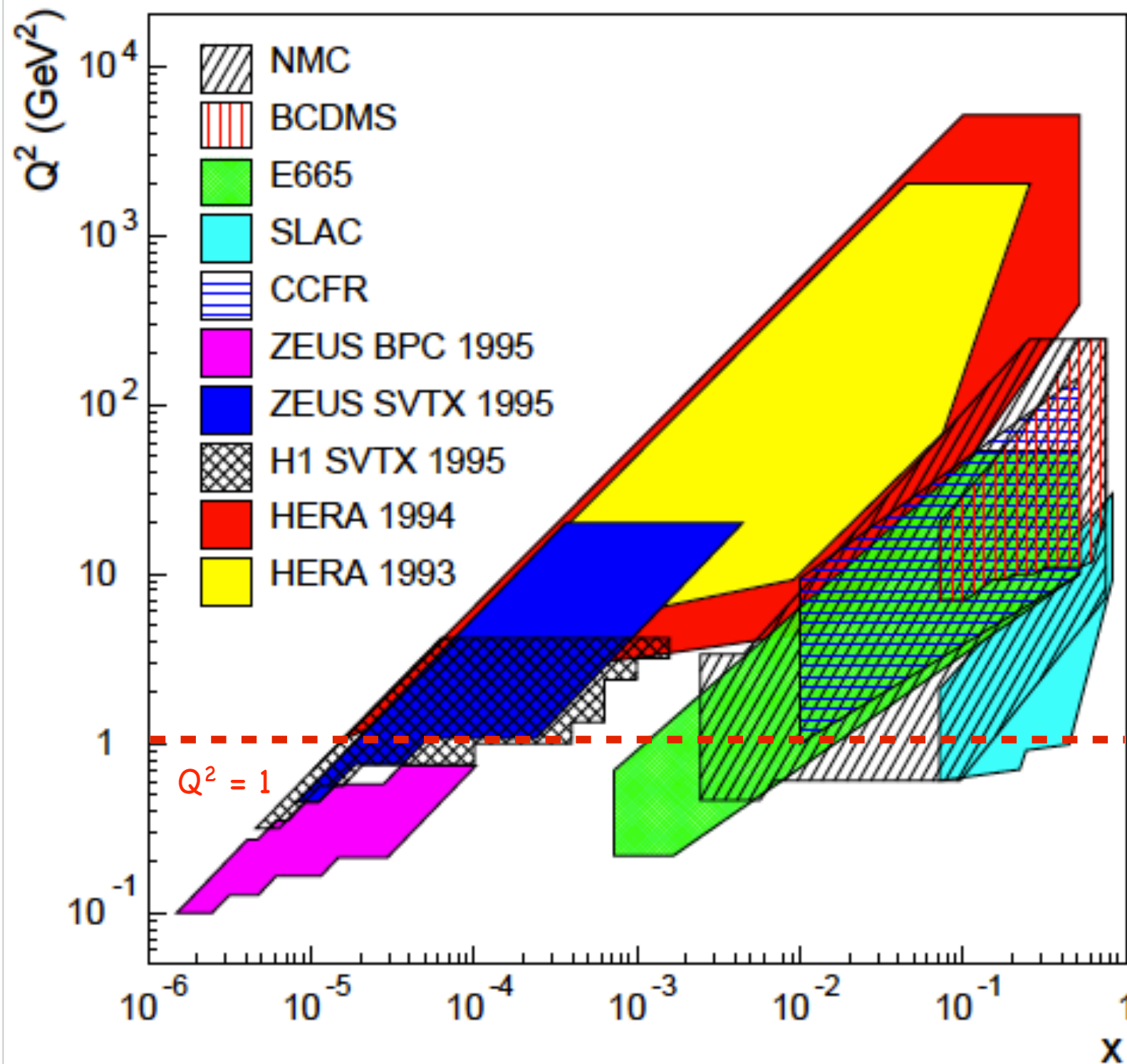
experimental input

thriving experimental programs since the early seventies

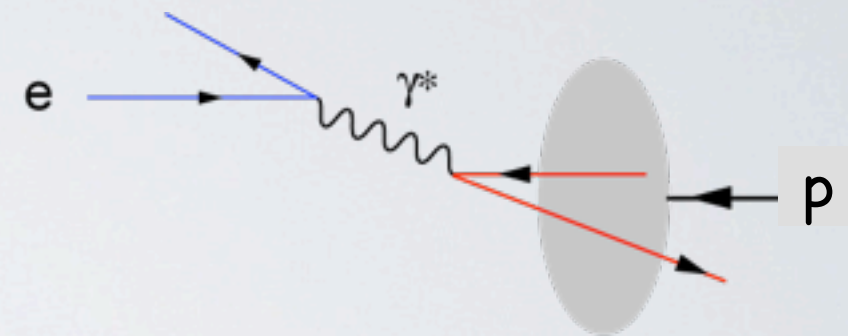


biggest obstacle for nPDF analysis: no eA collider yet

experimental input: x, Q^2 plane

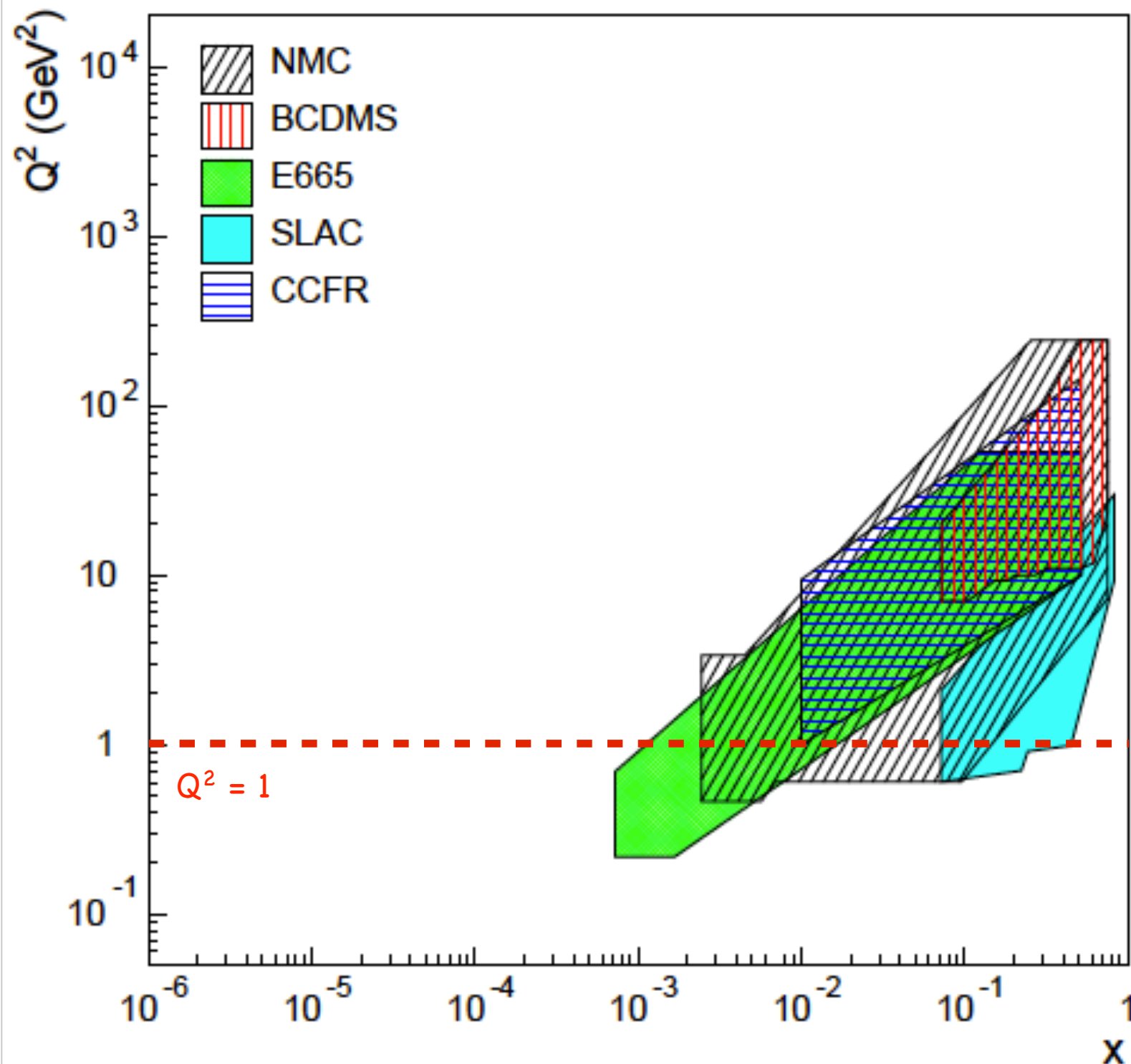


current kinematic coverage
for electron-proton DIS

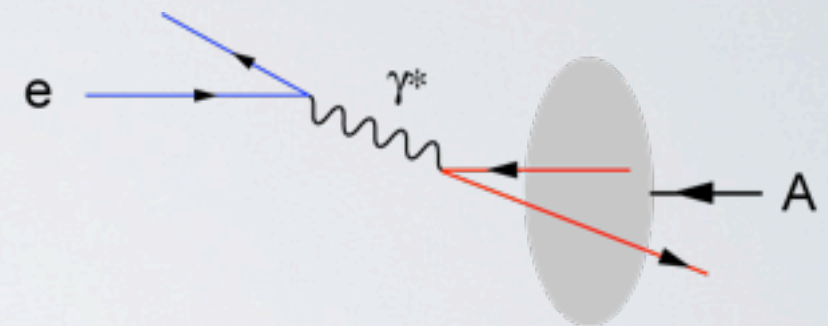


determines small- x behaviour
of quarks and gluons in
all analyses of proton PDFs

experimental input: x, Q^2 plane

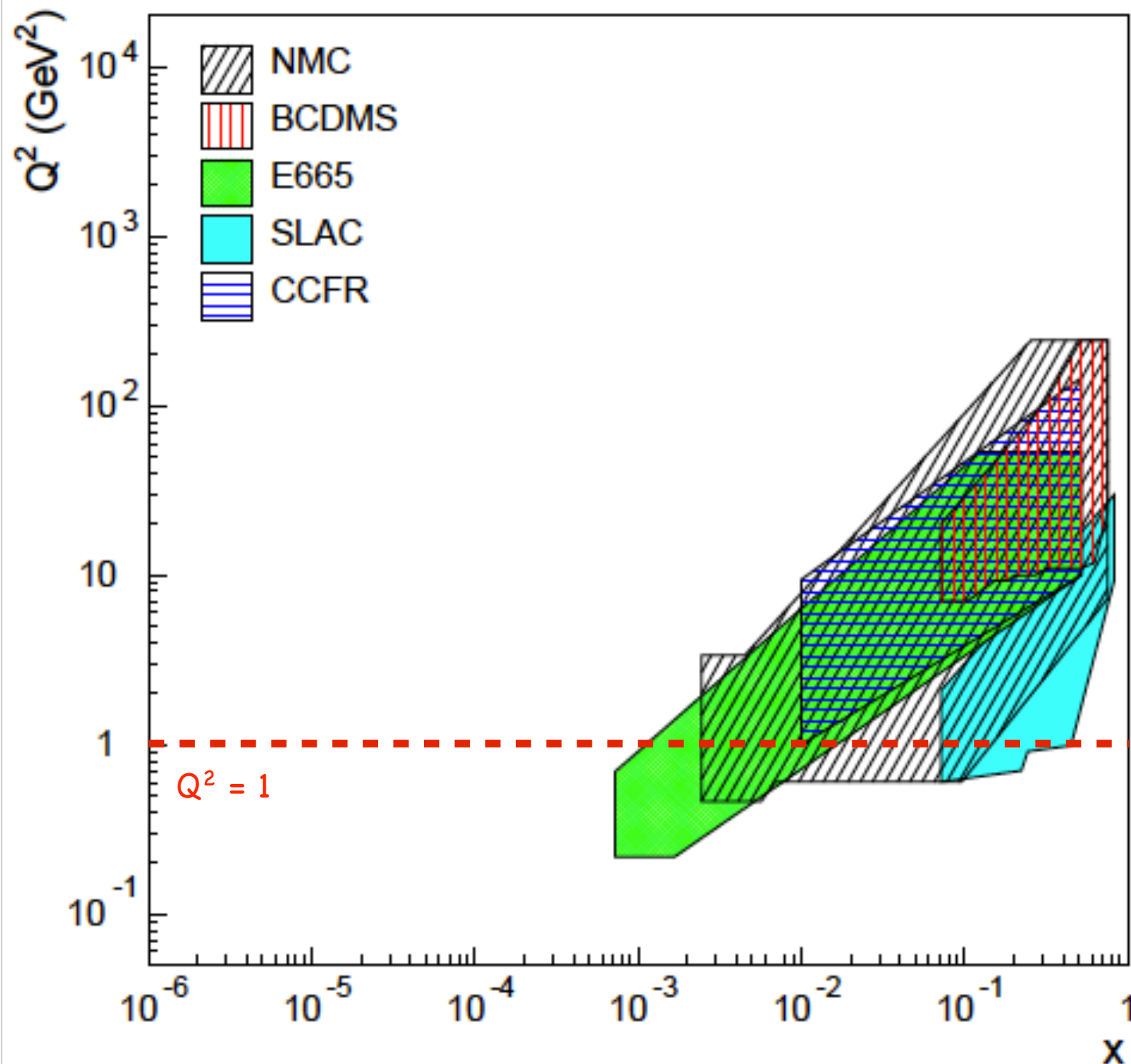


much more limited coverage
in eA DIS

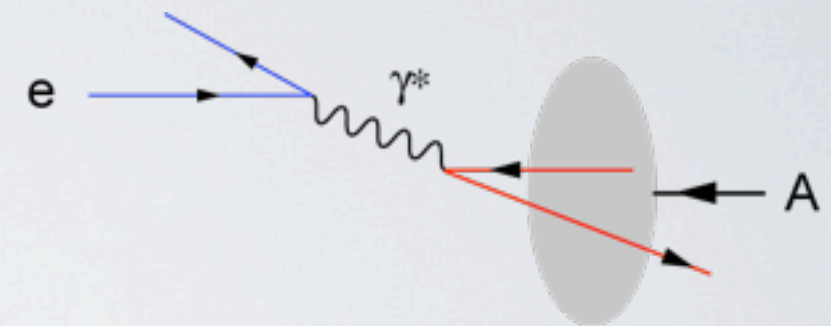


yet, the best constraint for nPDFs

experimental input: x, Q^2 plane



much more limited coverage
in eA DIS



yet, the best constraint for nPDFs

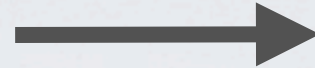
- low x , low Q^2
where saturation is relevant
- high Q^2
to test scale evolution



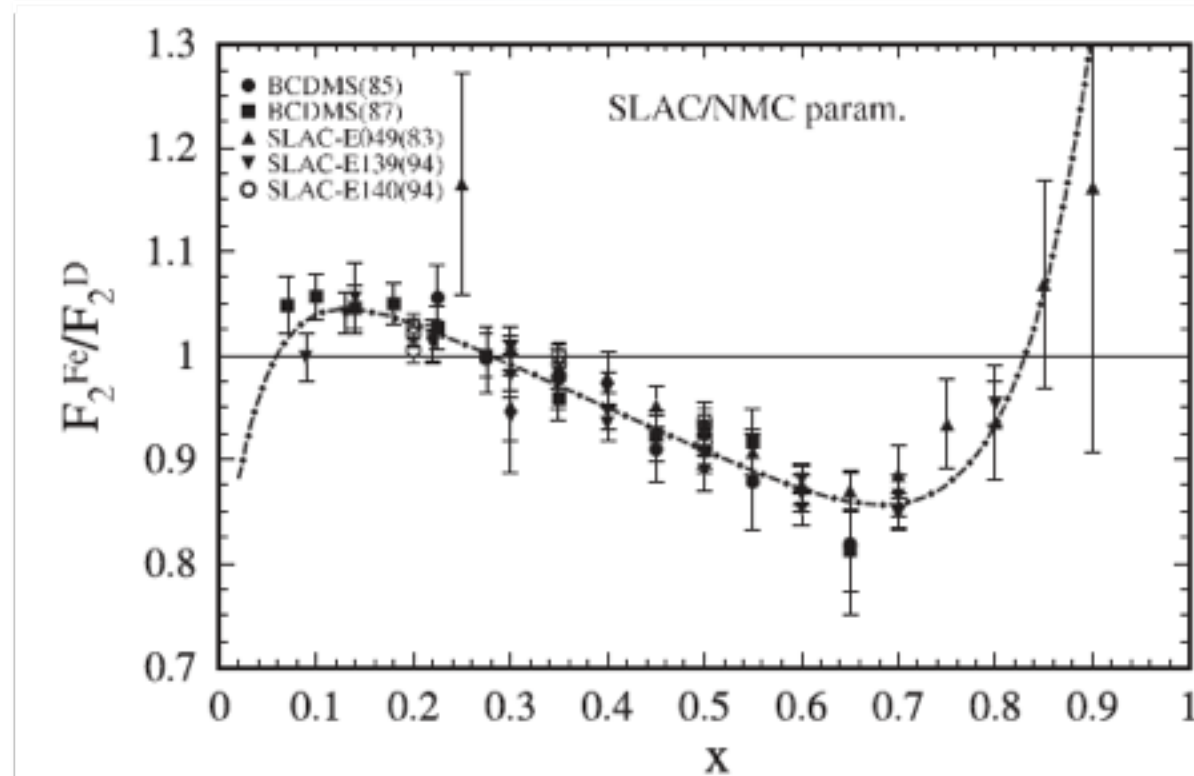
an electron-ion collider
(EIC, LHeC projects)
is in high demand

the many facets of nPDFs

nuclei behave rather differently
than a simple incoherent
superposition of protons and neutrons

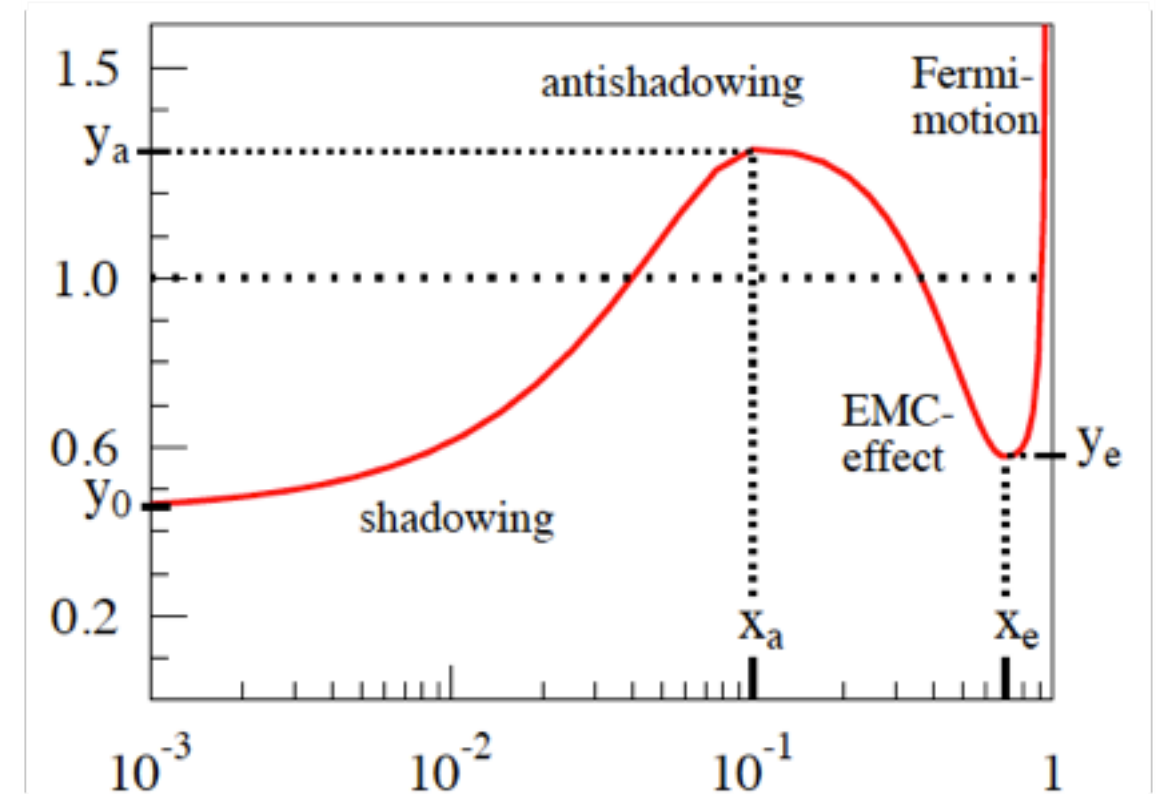


quarks and gluons in bound nucleons
exhibit highly non-trivial
momentum distributions



nuclear modifications
traditionally parametrized as ratios

scaling variable (per nucleon)
 $p_N = p_A/A$



$$f_i^A(x_N, Q_0) = R_i^A(x_N, Q_0) \times f_i^P(x_N, Q_0)$$

$$x_N = \frac{Q^2}{2p_N \cdot q} \quad 0 < x_N < A$$

strategies to parametrize nPDFs

all **measurements** usually given in terms of ratios w.r.t. some light nucleus

e.g. $R_A(x_N, Q^2) = \frac{F_2^A(x_N, Q^2)}{F_2^D(x_N, Q^2)}$

where $F_2^A = \frac{1}{A} \left[Z F_2^{p/A} + (A - Z) F_2^{n/A} \right]$

■ nPDFs give distributions in bound proton $f_i^{p/A}(x_N, Q^2)$

■ ... assume isospin invariance for

$$f_i^{n/A}(x_N, Q^2)$$

strategies to parametrize nPDFs

all **measurements** usually given in terms of ratios w.r.t. some light nucleus

e.g. $R_A(x_N, Q^2) = \frac{F_2^A(x_N, Q^2)}{F_2^D(x_N, Q^2)}$

where $F_2^A = \frac{1}{A} \left[Z F_2^{p/A} + (A - Z) F_2^{n/A} \right]$

■ nPDFs give distributions in bound proton $f_i^{p/A}(x_N, Q^2)$

■ ... assume isospin invariance for

$f_i^{n/A}(x_N, Q^2)$

conventional ansatz

multiplicative nuclear correction factor $f_i^{p/A}(x_N, Q_0) = R_i^A(x_N, Q_0) \times f_i^p(x_N, Q_0)$

used in
 Hirai, Kumano, Nagai (HKN) arXiv:0709.3038
 Eskola, Paukkunen, Salgado (EPS) arXiv:0902.4154
 de Florian, Sassot, MS, Zurita (DSSZ) arXiv:1112.6324

input scale of $O(1 \text{ GeV})$

free proton densities

choose ansatz and determine from data

- ▶ works well with small amount of parameters
- ▶ cannot account for $x_N > 1$ region [as free proton PDFs limited to $0 < x_N < 1$]

strategies to parametrize nPDFs

all **measurements** usually given in terms of ratios w.r.t. some light nucleus

e.g. $R_A(x_N, Q^2) = \frac{F_2^A(x_N, Q^2)}{F_2^D(x_N, Q^2)}$

where $F_2^A = \frac{1}{A} \left[Z F_2^{p/A} + (A - Z) F_2^{n/A} \right]$

■ nPDFs give distributions in bound proton $f_i^{p/A}(x_N, Q^2)$

■ ... assume isospin invariance for

$$f_i^{n/A}(x_N, Q^2)$$

conventional ansatz

multiplicative nuclear correction factor $f_i^{p/A}(x_N, Q_0) = R_i^A(x_N, Q_0) \times f_i^p(x_N, Q_0)$

used in
 Hirai, Kumano, Nagai (HKN) arXiv:0709.3038
 Eskola, Paukkunen, Salgado (EPS) arXiv:0902.4154
 de Florian, Sassot, MS, Zurita (DSSZ) arXiv:1112.6324

input scale of $O(1 \text{ GeV})$

free proton densities

choose ansatz and determine from data

- ▶ works well with small amount of parameters
- ▶ cannot account for $x_N > 1$ region [as free proton PDFs limited to $0 < x_N < 1$]

direct ansatz

parametrize nPDFs directly $f_i^{p/A}(x_N, Q_0)$

used in Keppel, Kovarik, Olness, ... (nCTEQ) arXiv:0907.2357

- ▶ still dependent on some free proton PDF to compute ratios
- ▶ natural to choose same functional form as for proton PDF

convolutional approach

define nPDF through a weight function

used in de Florian, Sassot (nDS) hep-ph/0311227

$$f_i^{p/A}(x_N, Q_0) = \int_{x_N}^A \frac{dy}{y} W_i^A(y, Q_0) f_i^p\left(\frac{x_N}{y}, Q_0\right)$$

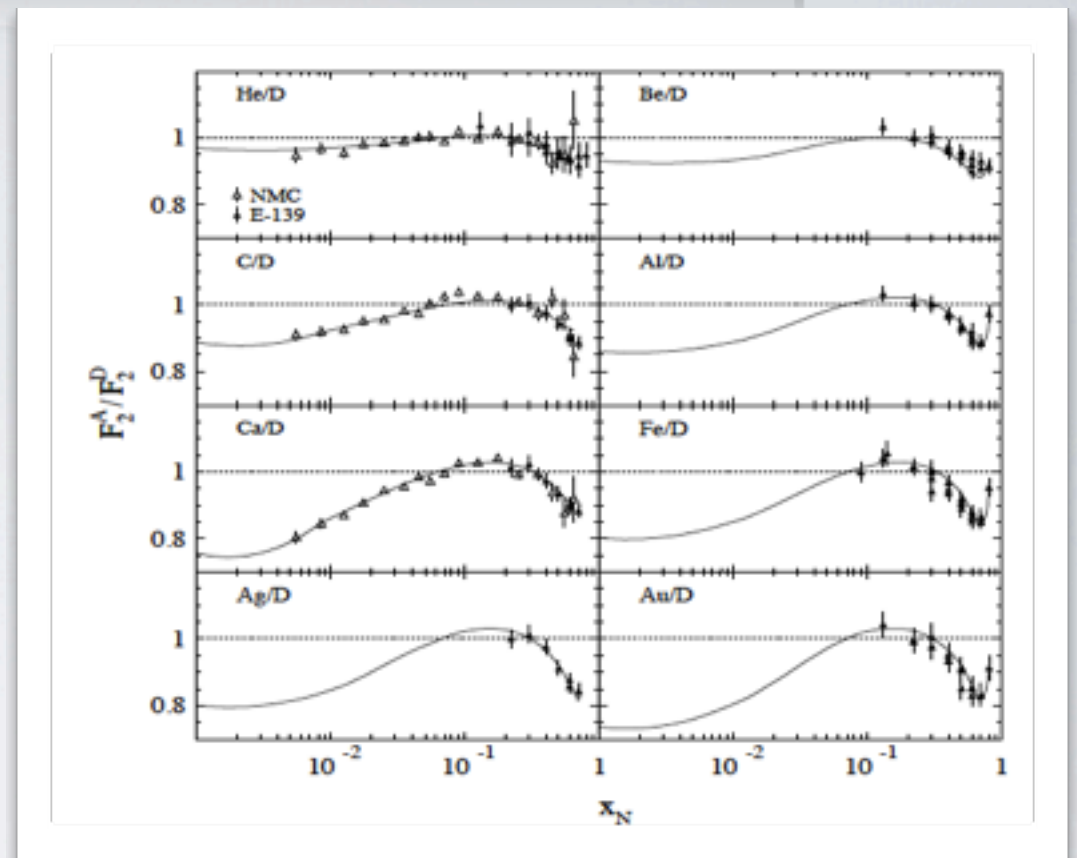
choose ansatz and determine from data

- ▶ W can be viewed as an effective nucleon momentum density in a nucleus

a brief history of selected nPDF fits

nDS de Florian, Sassot - hep-ph/0311227

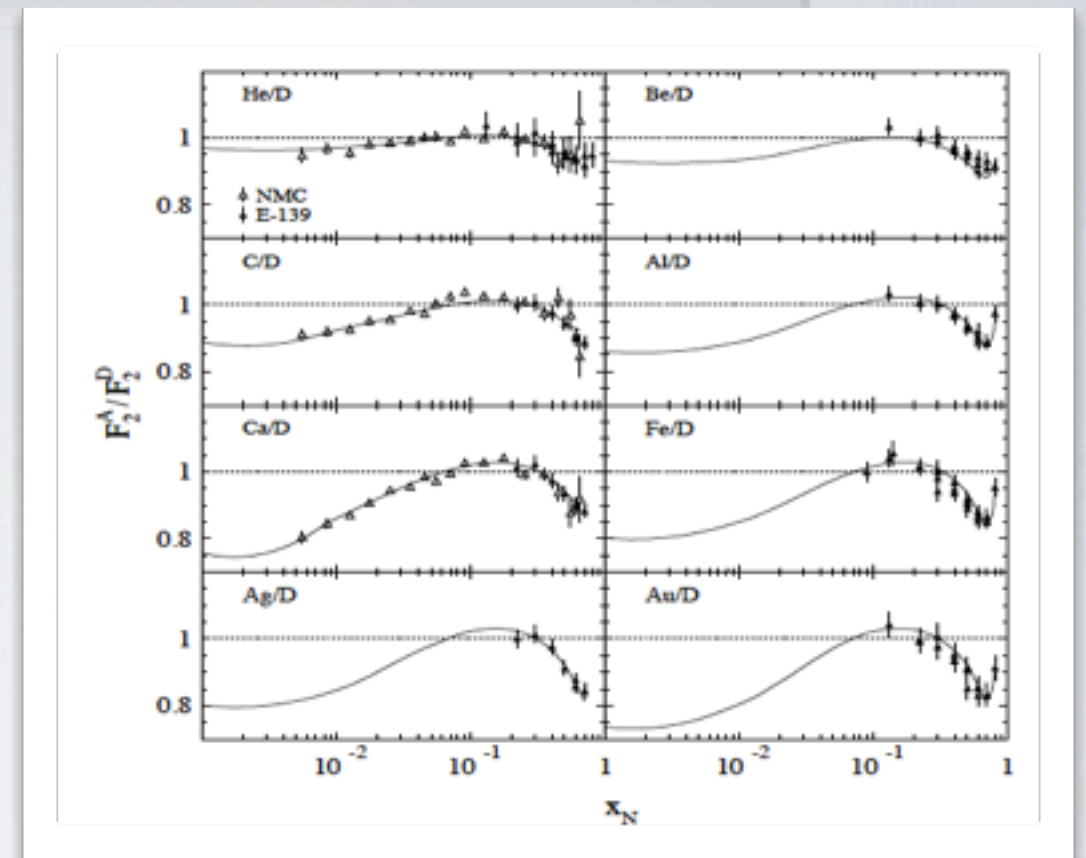
- ▶ **first NLO analysis** $\chi^2/\text{d.o.f.} = 0.74$
- ▶ only SLAC & NMC DIS sets and some DY data
- ▶ convolutional approach in Mellin N-space
- ▶ no error analysis



a brief history of selected nPDF fits

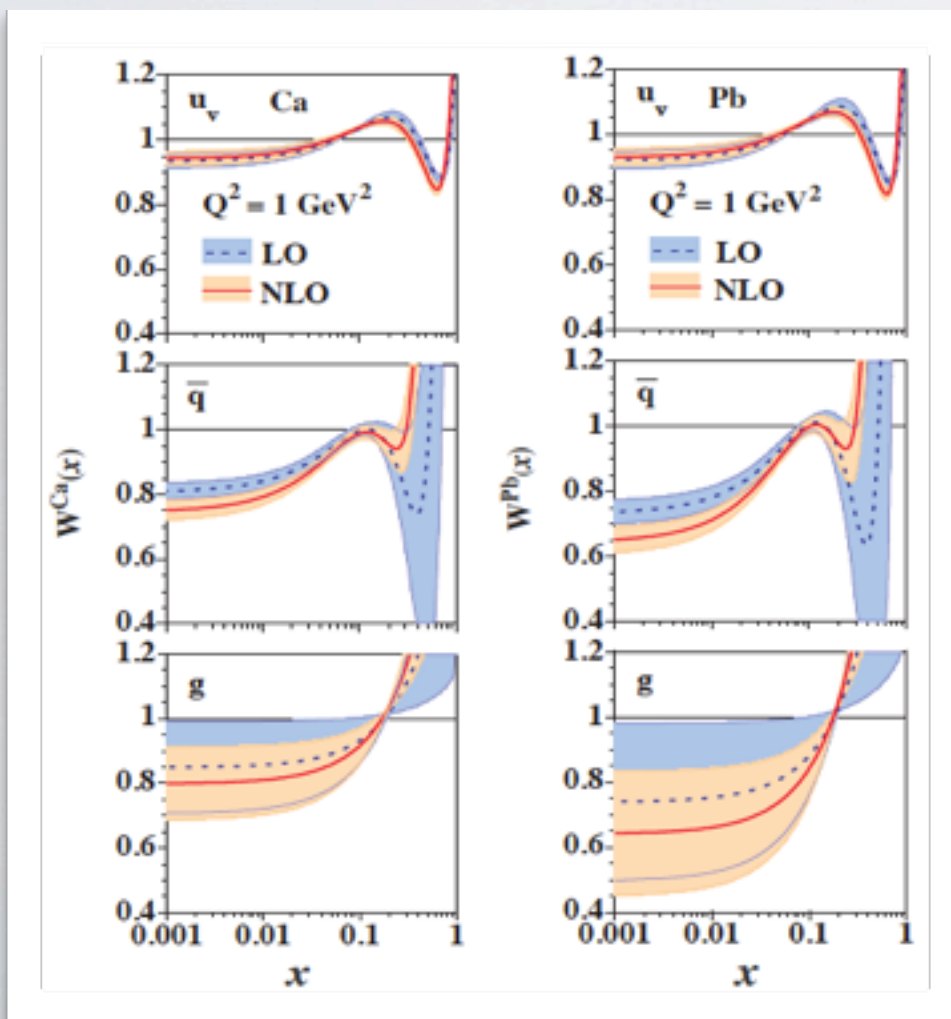
nDS de Florian, Sassot - hep-ph/0311227

- ▶ **first NLO analysis** $\chi^2/\text{d.o.f.} = 0.74$
- ▶ only SLAC & NMC DIS sets and some DY data
- ▶ convolutional approach in Mellin N-space
- ▶ no error analysis



HKN Hirai, Kumano, Nagai - arXiv:0709.3038

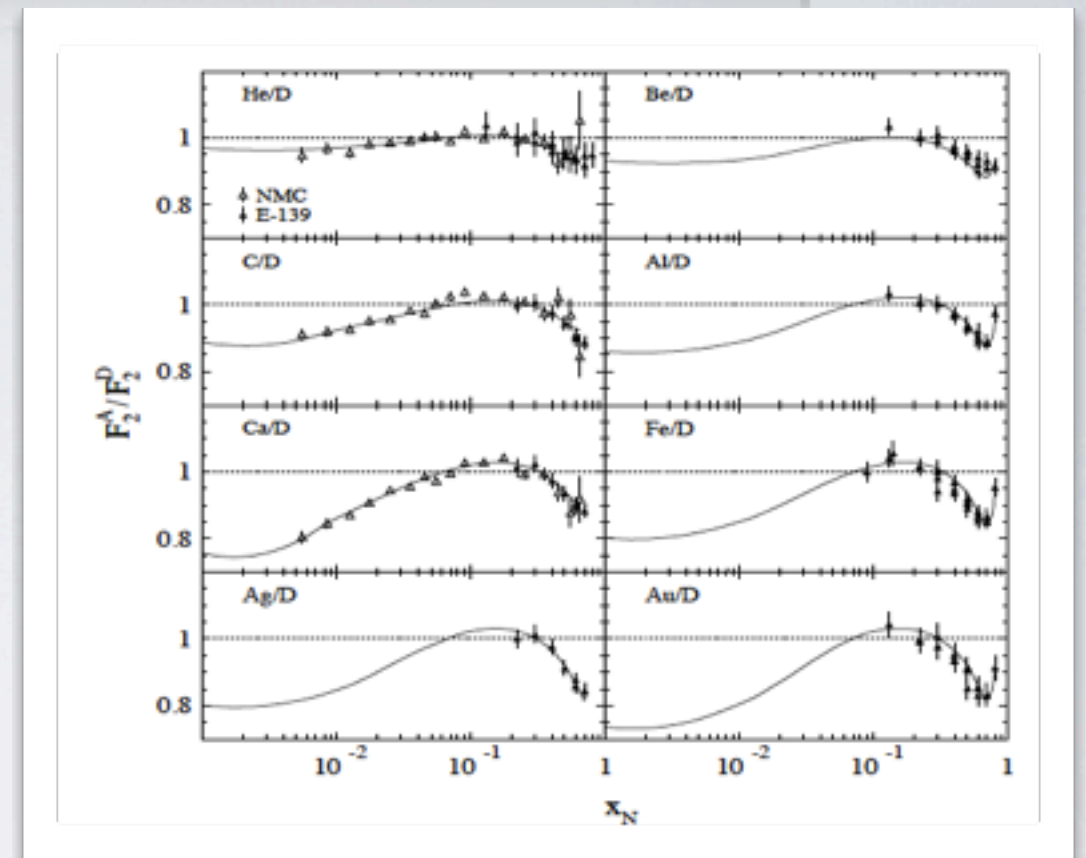
- ▶ LO and NLO analyses $\chi^2/\text{d.o.f.} = 1.2$
- ▶ standard DIS and DY data sets
- ▶ standard multiplicative ansatz
- ▶ **first error analysis** (Hessian method)



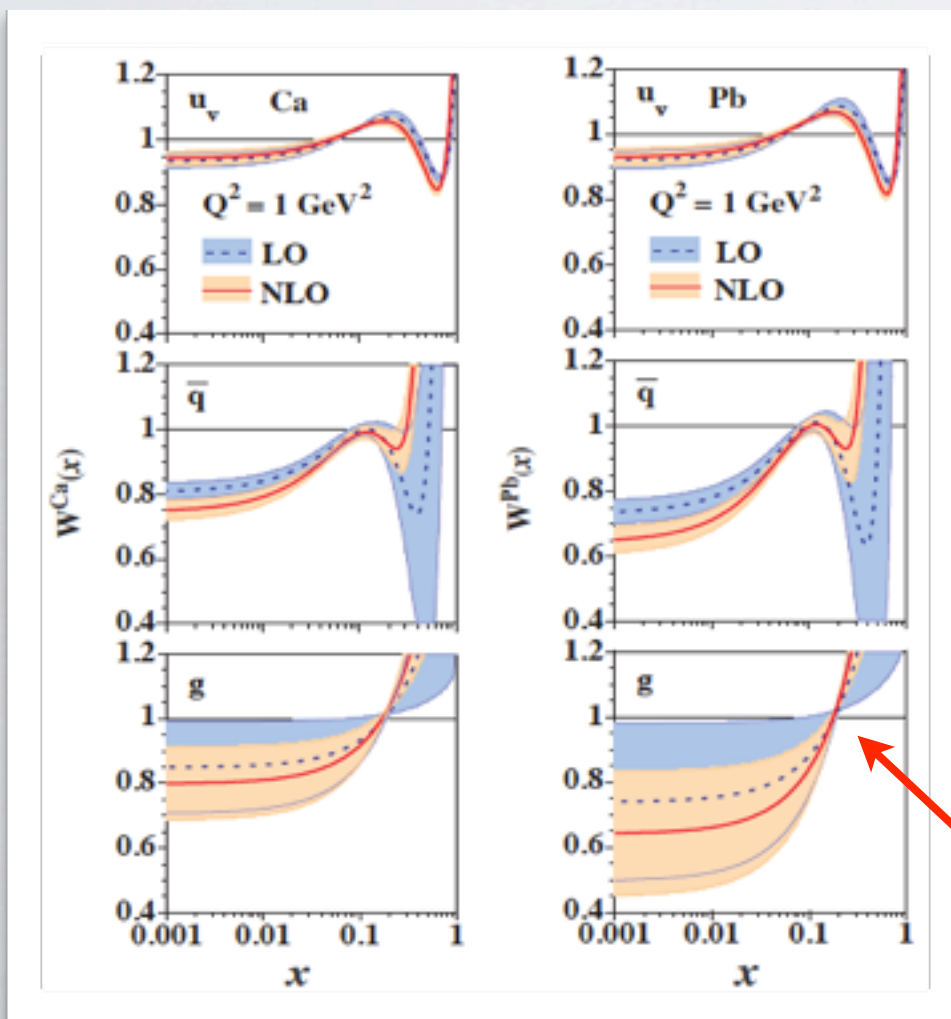
a brief history of selected nPDF fits

nDS de Florian, Sassot - hep-ph/0311227

- ▶ **first NLO analysis** $\chi^2/\text{d.o.f.} = 0.74$
- ▶ only SLAC & NMC DIS sets and some DY data
- ▶ convolutional approach in Mellin N-space
- ▶ no error analysis



HKN Hirai, Kumano, Nagai - arXiv:0709.3038

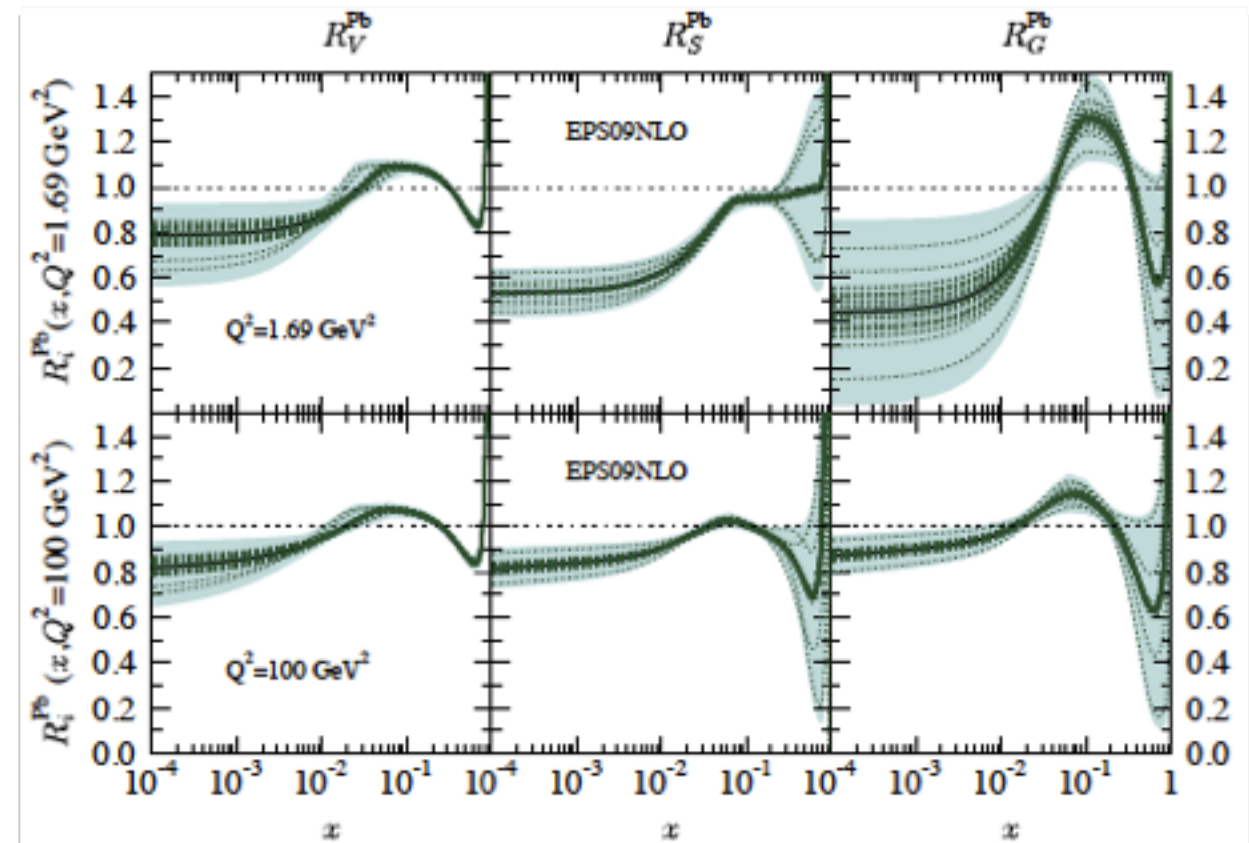


- ▶ LO and NLO analyses $\chi^2/\text{d.o.f.} = 1.2$
- ▶ standard DIS and DY data sets
- ▶ standard multiplicative ansatz
- ▶ **first error analysis** (Hessian method)
- ▶ rather "unusual" gluon distribution at large x

selected nPDF fits (cont'd)

EPS Eskola, Paukkunen, Salgado - arXiv:0902.4154

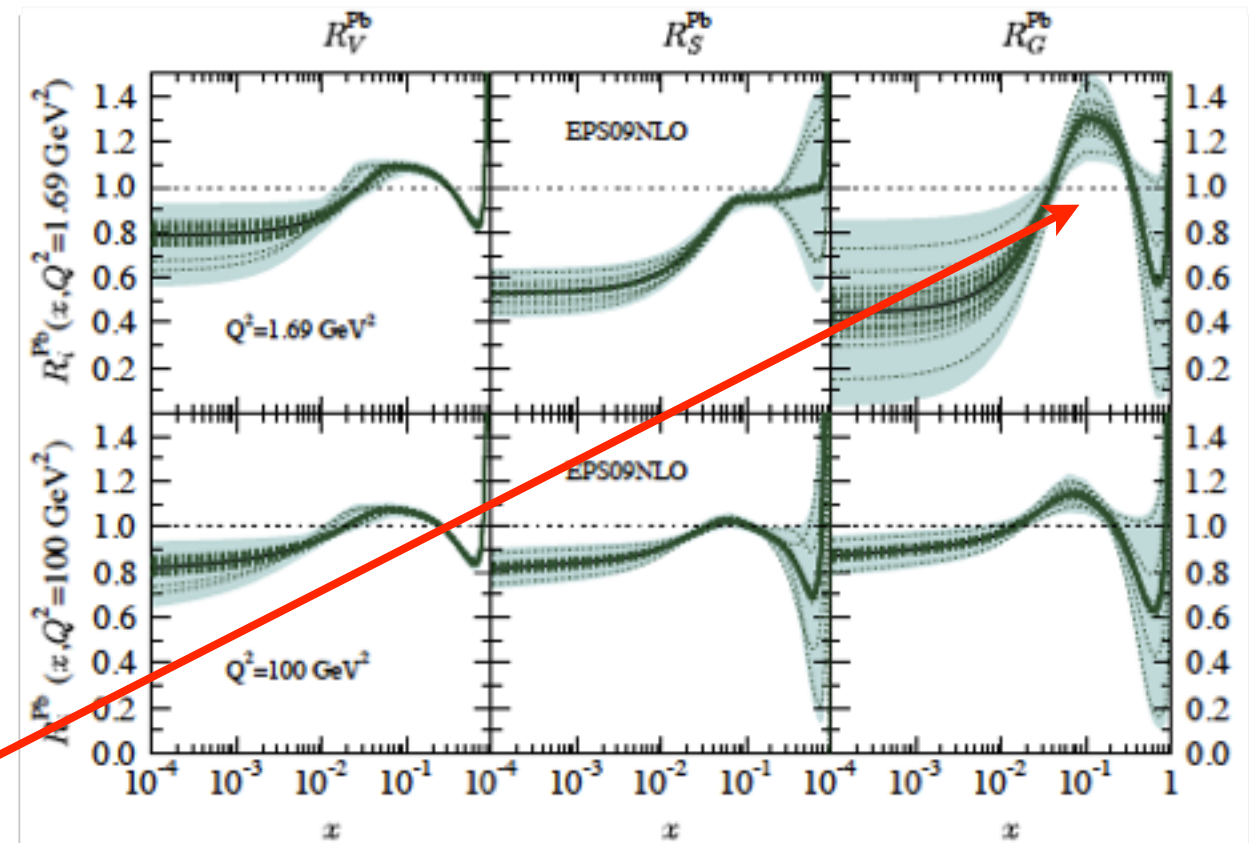
- ▶ NLO analysis $\chi^2/\text{d.o.f.} = 0.8$
- ▶ usual DIS & DY data
- ▶ **RHIC dAu data to constrain gluon better**
- ▶ complicated piecewise multipl. ansatz
- ▶ Hessian error analysis



selected nPDF fits (cont'd)

EPS Eskola, Paukkunen, Salgado - arXiv:0902.4154

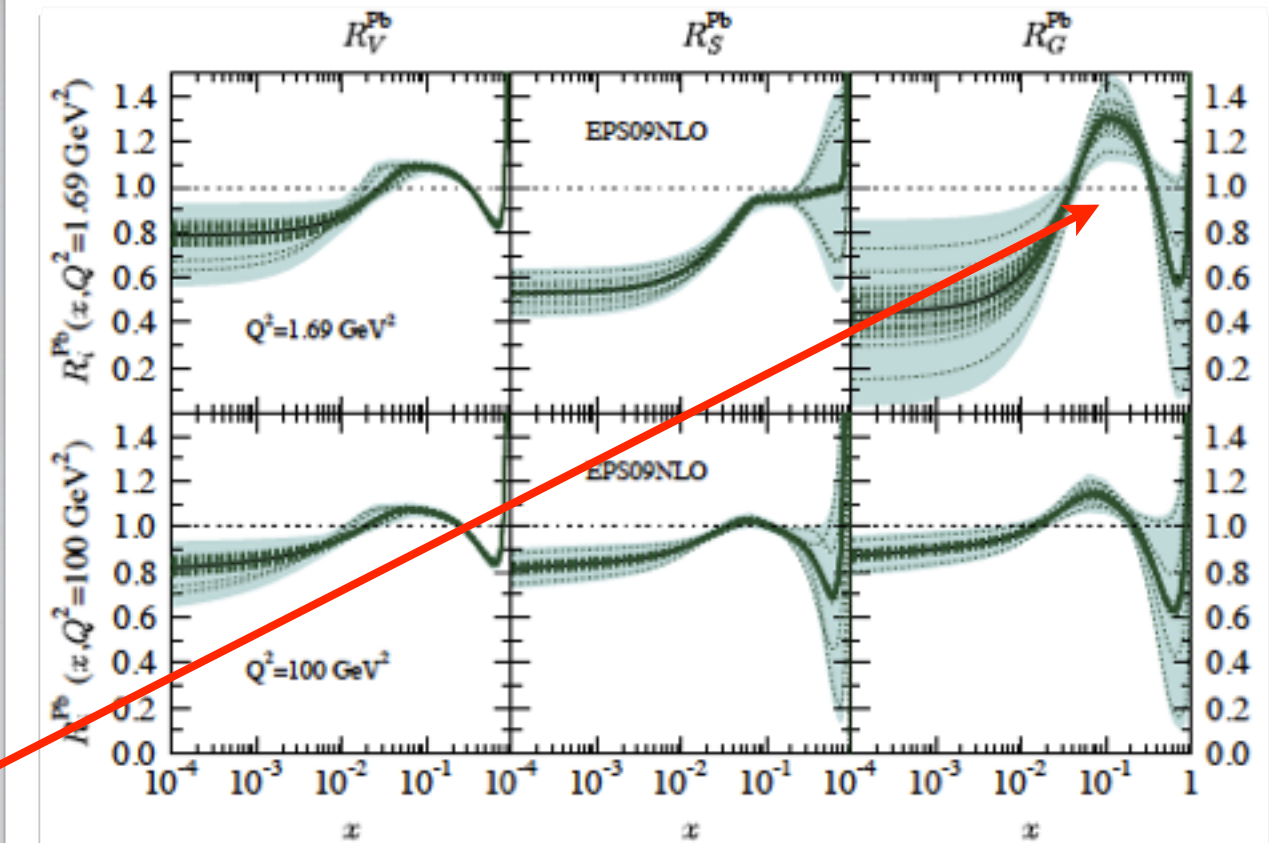
- ▶ NLO analysis $\chi^2/\text{d.o.f.} = 0.8$
- ▶ usual DIS & DY data
- ▶ **RHIC dAu data to constrain gluon better**
- ▶ complicated piecewise multipl. ansatz
- ▶ Hessian error analysis
- ▶ huge anti-shadowing/EMC effect for gluon



selected nPDF fits (cont'd)

EPS Eskola, Paukkunen, Salgado - arXiv:0902.4154

- ▶ NLO analysis $\chi^2/\text{d.o.f.} = 0.8$
- ▶ usual DIS & DY data
- ▶ **RHIC dAu data to constrain gluon better**
- ▶ complicated piecewise multipl. ansatz
- ▶ Hessian error analysis
- ▶ huge anti-shadowing/EMC effect for gluon



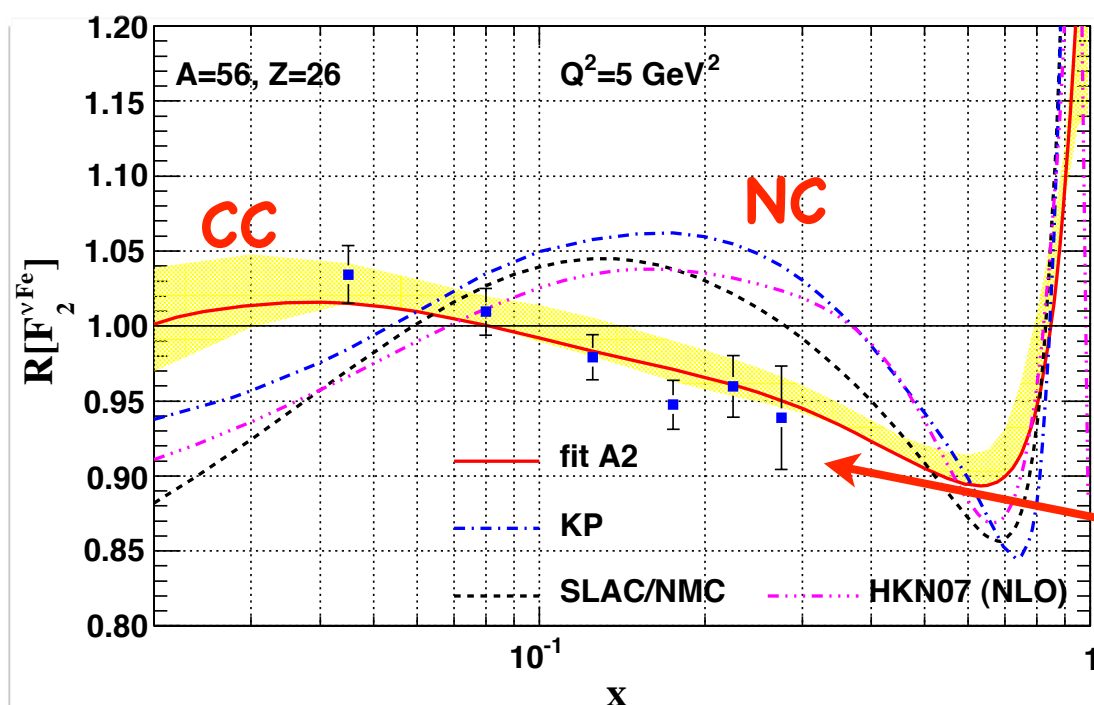
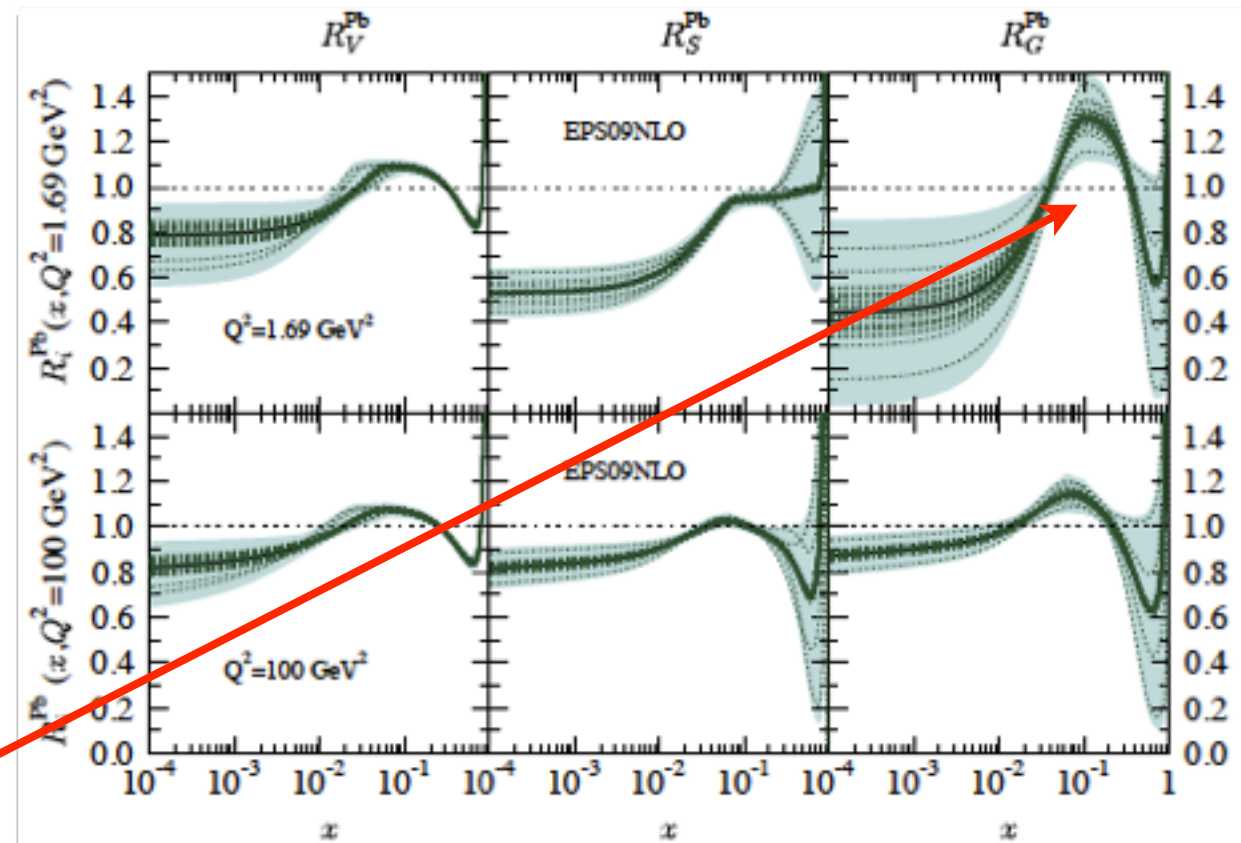
nCTEQ Keppel, Kovarik, ... - arXiv:0907.2357

- ▶ direct ansatz a la CTEQ
- ▶ DIS & DY plus **CC neutrino DIS data**

selected nPDF fits (cont'd)

EPS Eskola, Paukkunen, Salgado - arXiv:0902.4154

- ▶ NLO analysis $\chi^2/\text{d.o.f.} = 0.8$
- ▶ usual DIS & DY data
- ▶ **RHIC dAu data to constrain gluon better**
- ▶ complicated piecewise multipl. ansatz
- ▶ Hessian error analysis
- ▶ huge anti-shadowing/EMC effect for gluon



nCTEQ Keppel, Kovarik, ... - arXiv:0907.2357

- ▶ direct ansatz a la CTEQ
- ▶ DIS & DY plus **CC neutrino DIS data**
- ▶ find tension between NC and CC DIS data

breakdown of factorization

DSSZ global analysis

de Florian, Sassot, MS, Zurita - arXiv:1112.6324

why do we need yet another set of nPDFs ?

DSSZ global analysis

de Florian, Sassot, MS, Zurita - arXiv:1112.6324

why do we need yet another set of nPDFs ?

☐ no truly global analysis yet

▶ include charged lepton DIS, Drell-Yan, CC neutrino DIS, and RHIC dAu data

DSSZ global analysis

de Florian, Sassot, MS, Zurita - arXiv:1112.6324

why do we need yet another set of nPDFs ?

- no truly global analysis yet

 - ▶ include charged lepton DIS, Drell-Yan, CC neutrino DIS, and RHIC dAu data

- use up-to-date proton PDFs as reference set

 - ▶ many different sets to choose from - take MSTW

Martin, Stirling, Thorne, Watt - arXiv:0901.0002

DSSZ global analysis

de Florian, Sassot, MS, Zurita - arXiv:1112.6324

why do we need yet another set of nPDFs ?

- ☐ no truly global analysis yet
 - ▶ include charged lepton DIS, Drell-Yan, CC neutrino DIS, and RHIC dAu data
- ☐ use up-to-date proton PDFs as reference set
 - ▶ many different sets to choose from - take MSTW

Martin, Stirling, Thorne, Watt - arXiv:0901.0002
- ☐ improve on the treatment of heavy flavors
 - ▶ e.g. NLO massive Wilson coefficients for CC DIS

Blumlein, Hasselhuhn, Kovacikova, Moch - arXiv:1104.3449
- ☐ provide some estimate of nPDF uncertainties

DSSZ global analysis

de Florian, Sassot, MS, Zurita - arXiv:1112.6324

why do we need yet another set of nPDFs ?

- ☐ no truly global analysis yet
 - ▶ include charged lepton DIS, Drell-Yan, CC neutrino DIS, and RHIC dAu data
- ☐ use up-to-date proton PDFs as reference set
 - ▶ many different sets to choose from - take MSTW

Martin, Stirling, Thorne, Watt - arXiv:0901.0002
- ☐ improve on the treatment of heavy flavors
 - ▶ e.g. NLO massive Wilson coefficients for CC DIS

Blumlein, Hasselhuhn, Kovacikova, Moch - arXiv:1104.3449
- ☐ provide some estimate of nPDF uncertainties

main questions to address

- do we really see a tension between charged lepton and neutrino DIS data
- do RHIC dAu data imply strong modifications of the nuclear gluon distribution

DSSZ global analysis – preliminaries

► use multiplicative nuclear modification factor $f_i^A(\mathbf{x}, Q_0) = R_i^A(\mathbf{x}, Q_0) \times f_i^P(\mathbf{x}, Q_0)$

► initial scale $Q_0 = 1 \text{ GeV}$, NLO DGLAP evolution to all other scales $Q > Q_0$

► parametrize both valence distributions as needs to be flexible enough to accommodate (anti-)shadowing, EMC effect, Fermi motion

$$R_v^A(\mathbf{x}, Q_0) = \epsilon_1 \mathbf{x}^{\alpha_v} (1 - \mathbf{x})^{\beta_1} \times [1 + \epsilon_2 (1 - \mathbf{x})^{\beta_2}] \times [1 + \mathbf{a}_v (1 - \mathbf{x})^{\beta_3}]$$

DSSZ global analysis – preliminaries

► use multiplicative nuclear modification factor $f_i^A(x, Q_0) = R_i^A(x, Q_0) \times f_i^P(x, Q_0)$

► initial scale $Q_0 = 1 \text{ GeV}$, NLO DGLAP evolution to all other scales $Q > Q_0$

► parametrize both valence distributions as needs to be flexible enough to accommodate (anti-)shadowing, EMC effect, Fermi motion

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_v} (1-x)^{\beta_1} \times [1 + \epsilon_2 (1-x)^{\beta_2}] \times [1 + a_v (1-x)^{\beta_3}]$$

► data do not allow to discriminate different sea quark flavors (tried in analysis)

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{a_s + 1}$$

► need another modification factor for gluons

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{a_g + 1}$$

DSSZ global analysis – preliminaries

► use multiplicative nuclear modification factor $f_i^A(x, Q_0) = R_i^A(x, Q_0) \times f_i^P(x, Q_0)$

► initial scale $Q_0 = 1 \text{ GeV}$, NLO DGLAP evolution to all other scales $Q > Q_0$

► parametrize both valence distributions as needs to be flexible enough to accommodate (anti-)shadowing, EMC effect, Fermi motion

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_v} (1-x)^{\beta_1} \times [1 + \epsilon_2 (1-x)^{\beta_2}] \times [1 + a_v (1-x)^{\beta_3}]$$

► data do not allow to discriminate different sea quark flavors (tried in analysis)

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{a_s + 1}$$

► need another modification factor for gluons

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{a_g + 1}$$



quality of the fit unchanged
by relating $R_{s,g}$ to common R_v

but need different
normalization and small- x behavior

DSSZ global analysis – preliminaries

► use multiplicative nuclear modification factor $f_i^A(x, Q_0) = R_i^A(x, Q_0) \times f_i^P(x, Q_0)$

► initial scale $Q_0 = 1 \text{ GeV}$, NLO DGLAP evolution to all other scales $Q > Q_0$

► parametrize both valence distributions as needs to be flexible enough to accommodate (anti-)shadowing, EMC effect, Fermi motion

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_v} (1-x)^{\beta_1} \times [1 + \epsilon_2 (1-x)^{\beta_2}] \times [1 + a_v (1-x)^{\beta_3}]$$

► data do not allow to discriminate different sea quark flavors (tried in analysis)

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{a_s + 1}$$

► need another modification factor for gluons

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{a_g + 1}$$



quality of the fit unchanged by relating $R_{s,g}$ to common R_v

but need different normalization and small- x behavior

resulting “EMC effect” and “Fermi motion” for sea and gluons not constrained by data

DSSZ global analysis – preliminaries

► use multiplicative nuclear modification factor $f_i^A(x, Q_0) = R_i^A(x, Q_0) \times f_i^P(x, Q_0)$

► initial scale $Q_0 = 1 \text{ GeV}$, NLO DGLAP evolution to all other scales $Q > Q_0$

► parametrize both valence distributions as needs to be flexible enough to accommodate (anti-)shadowing, EMC effect, Fermi motion

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_v} (1-x)^{\beta_1} \times [1 + \epsilon_2 (1-x)^{\beta_2}] \times [1 + a_v (1-x)^{\beta_3}]$$

► data do not allow to discriminate different sea quark flavors (tried in analysis)

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{a_s + 1}$$

► need another modification factor for gluons

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{a_g + 1}$$



quality of the fit unchanged
by relating $R_{s,g}$ to common R_v

but need different
normalization and small- x behavior

resulting “EMC effect” and “Fermi motion” for sea and gluons not constrained by data

► 3 parameters constrained by charge & momentum conservation

also, fit unchanged if
 $\epsilon_g = \epsilon_s$

DSSZ global analysis – preliminaries

► use multiplicative nuclear modification factor $f_i^A(x, Q_0) = R_i^A(x, Q_0) \times f_i^P(x, Q_0)$

► initial scale $Q_0 = 1 \text{ GeV}$, NLO DGLAP evolution to all other scales $Q > Q_0$

► parametrize both valence distributions as needs to be flexible enough to accommodate (anti-)shadowing, EMC effect, Fermi motion

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_v} (1-x)^{\beta_1} \times [1 + \epsilon_2 (1-x)^{\beta_2}] \times [1 + a_v (1-x)^{\beta_3}]$$

► data do not allow to discriminate different sea quark flavors (tried in analysis)

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{a_s + 1}$$

► need another modification factor for gluons

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{a_g + 1}$$



quality of the fit unchanged
by relating $R_{s,g}$ to common R_v

but need different
normalization and small- x behavior

resulting “EMC effect” and “Fermi motion” for sea and gluons not constrained by data

► 3 parameters constrained by charge & momentum conservation

also, fit unchanged if
 $\epsilon_g = \epsilon_s$

total of 9 parameters per nucleus

$$\xi \in \{\alpha_v, \alpha_s, \alpha_g, \beta_1, \beta_2, \beta_3, a_v, a_s, a_g\}$$

parametrizing the A dependence

total of 9 parameters per nucleus

$$\xi \in \{\alpha_v, \alpha_s, \alpha_g, \beta_1, \beta_2, \beta_3, \mathbf{a}_v, \mathbf{a}_s, \mathbf{a}_g\}$$

► A dependence implemented as

$$\xi = \gamma_\xi + \lambda_\xi \mathbf{A}^{\delta_\xi}$$

► fit does not fix all parameters, assume

$$\delta_{\mathbf{a}_g} = \delta_{\mathbf{a}_s} \quad \delta_{\alpha_g} = \delta_{\alpha_s}$$

parametrizing the A dependence

total of 9 parameters per nucleus

$$\xi \in \{\alpha_v, \alpha_s, \alpha_g, \beta_1, \beta_2, \beta_3, a_v, a_s, a_g\}$$

► A dependence implemented as

$$\xi = \gamma_\xi + \lambda_\xi A^{\delta_\xi}$$

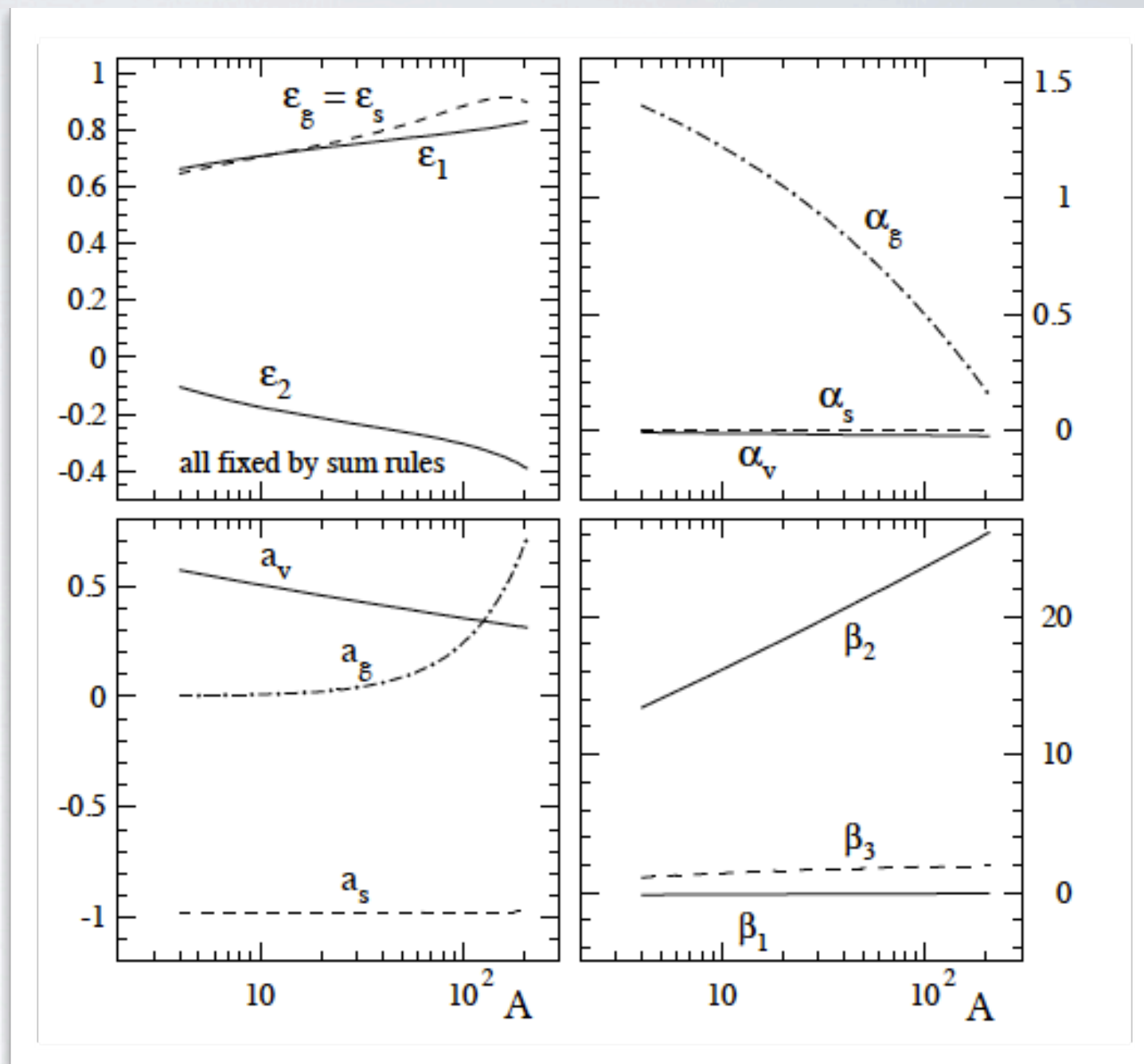
► fit does not fix all parameters, assume

$$\delta_{a_g} = \delta_{a_s} \quad \delta_{\alpha_g} = \delta_{\alpha_s}$$

**25 free parameters
in total**

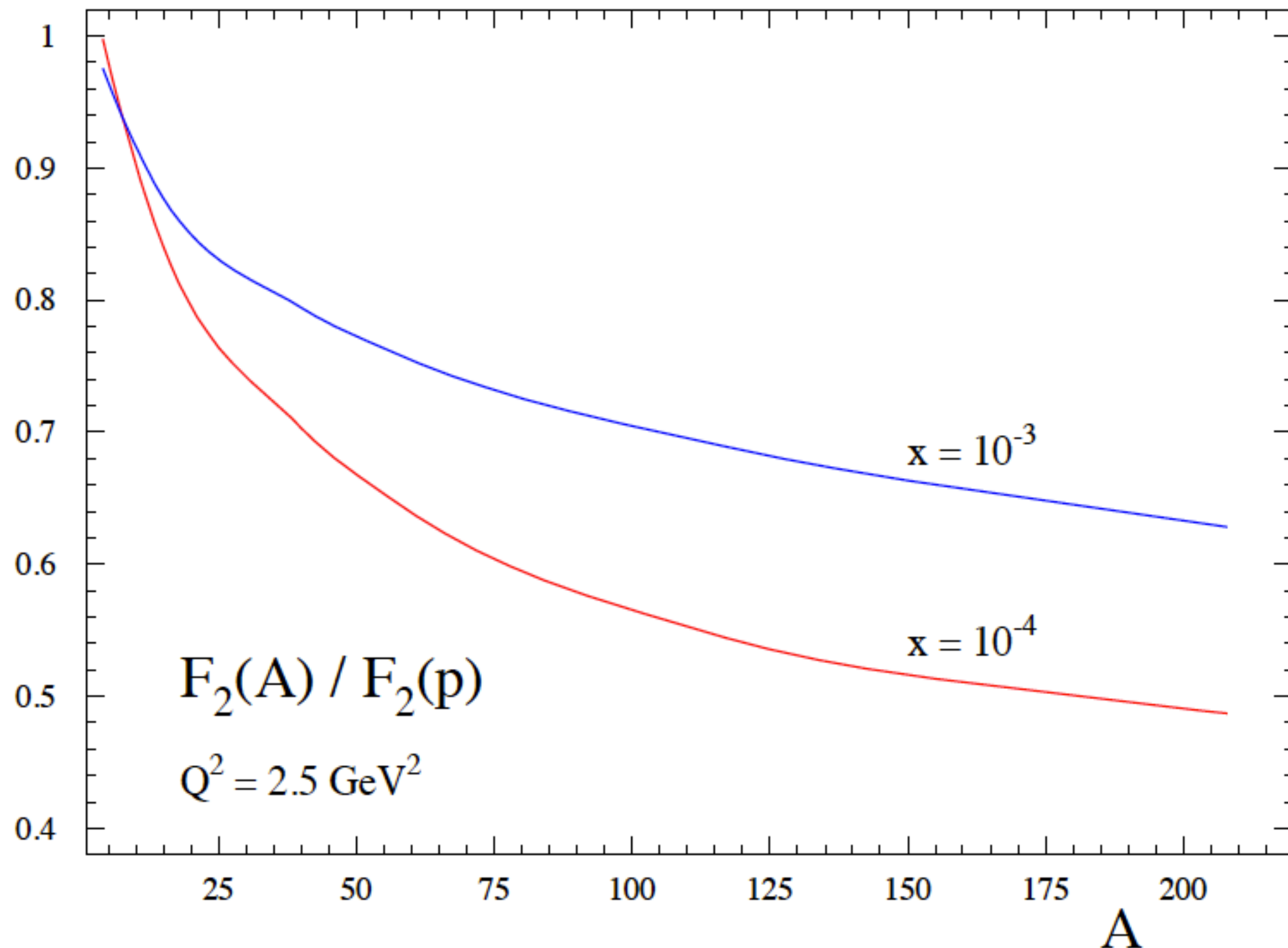
parameter	γ	λ	δ
α_v	-0.256	0.252	-0.017
α_s	0.001	-6.89×10^{-4}	0.286
α_g	1.994	-0.401	0.286
β_1	-5.564	5.36	0.0042
β_2	-59.62	69.01	0.0407
β_3	2.099	-1.878	-0.436
a_v	-0.622	1.302	-0.062
a_s	-0.980	2.33×10^{-6}	1.505
a_g	0.0018	2.35×10^{-4}	1.505

A dependence of fit parameters

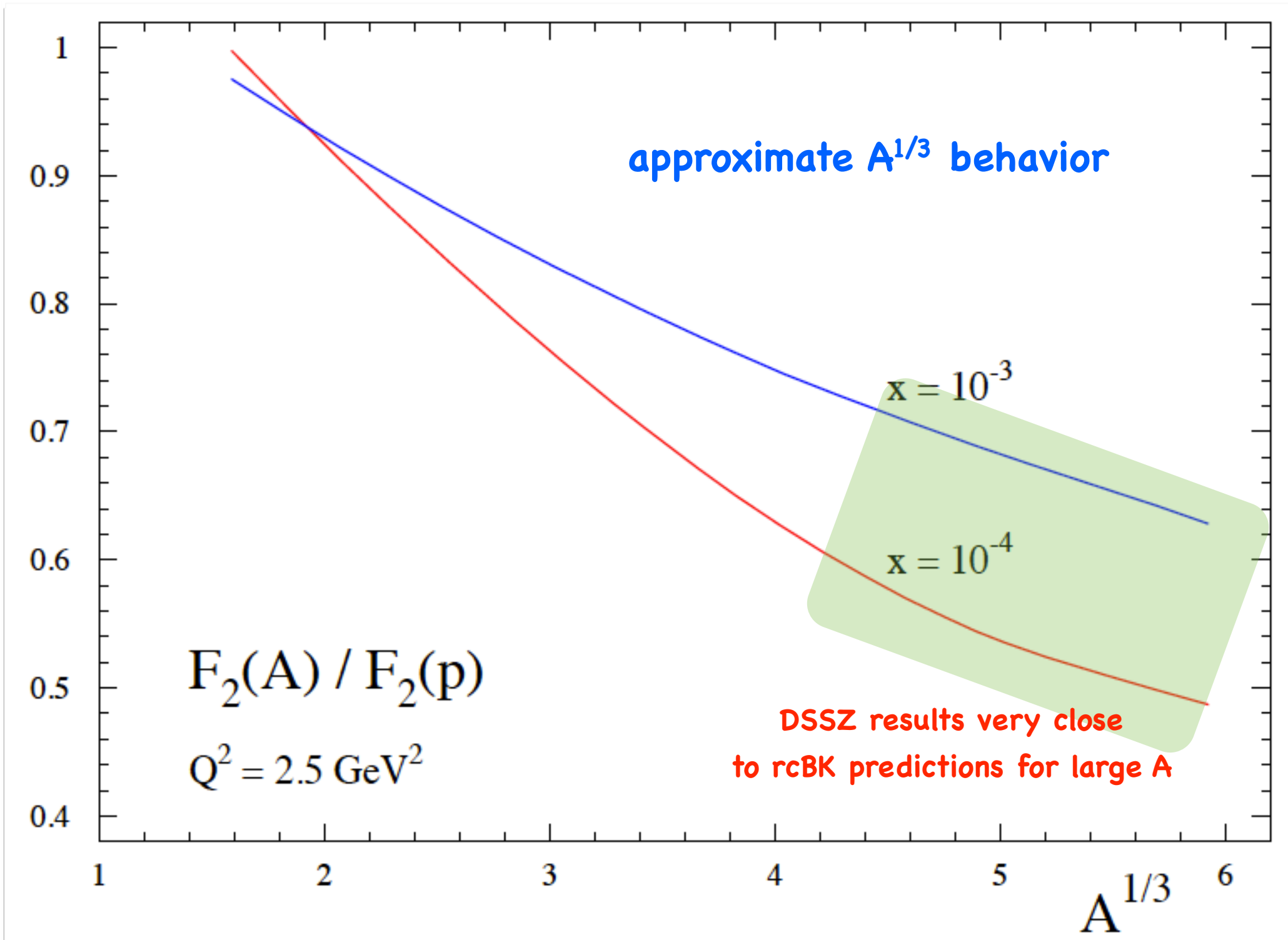


optimum NLO parameters
at the input scale

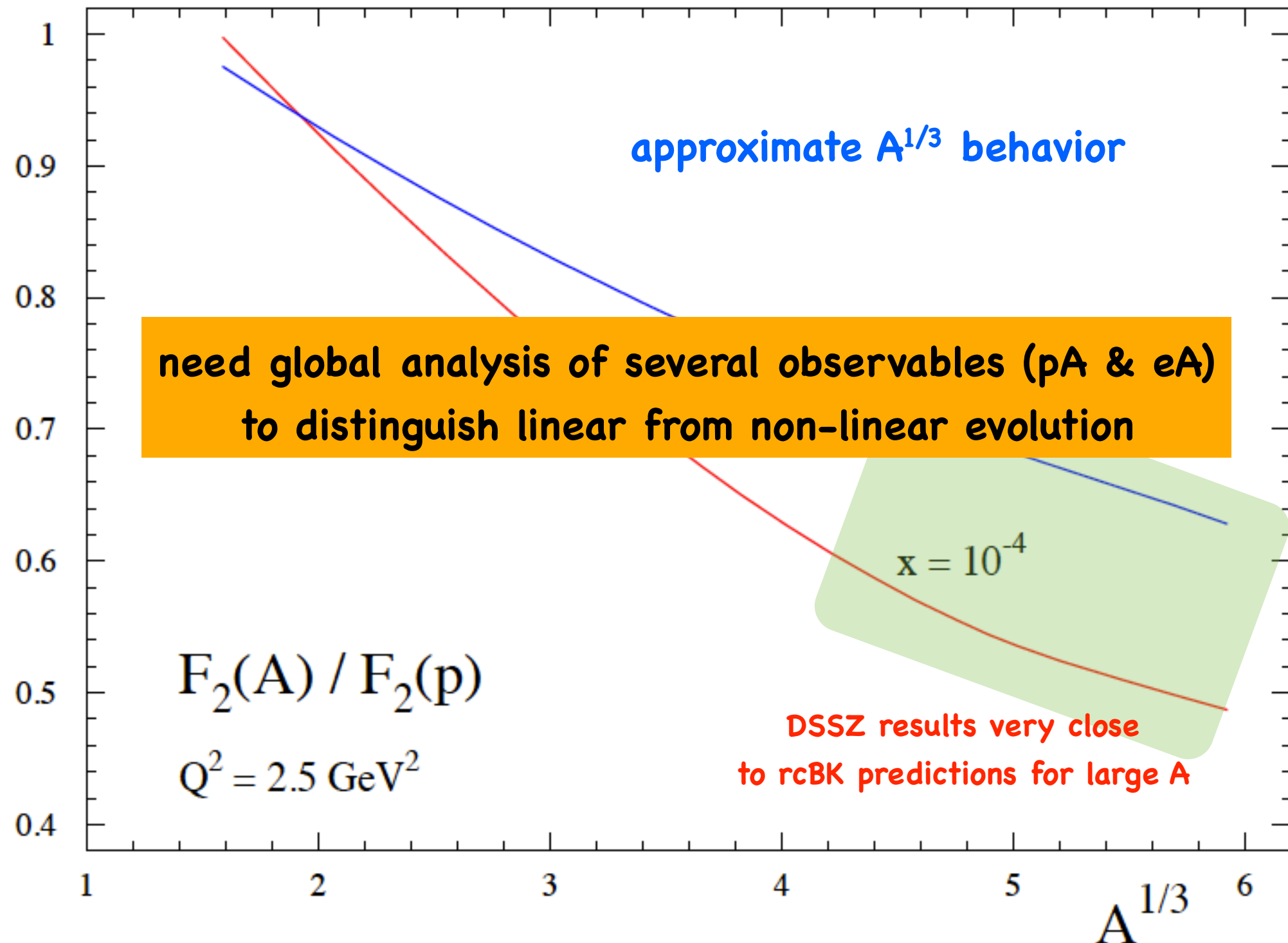
aside: A dependence of F_2^A/F_2^p @ eRHIC



aside: A dependence of F_2^A/F_2^p @ eRHIC



aside: A dependence of F_2^A/F_2^p @ eRHIC



overall quality of the fit

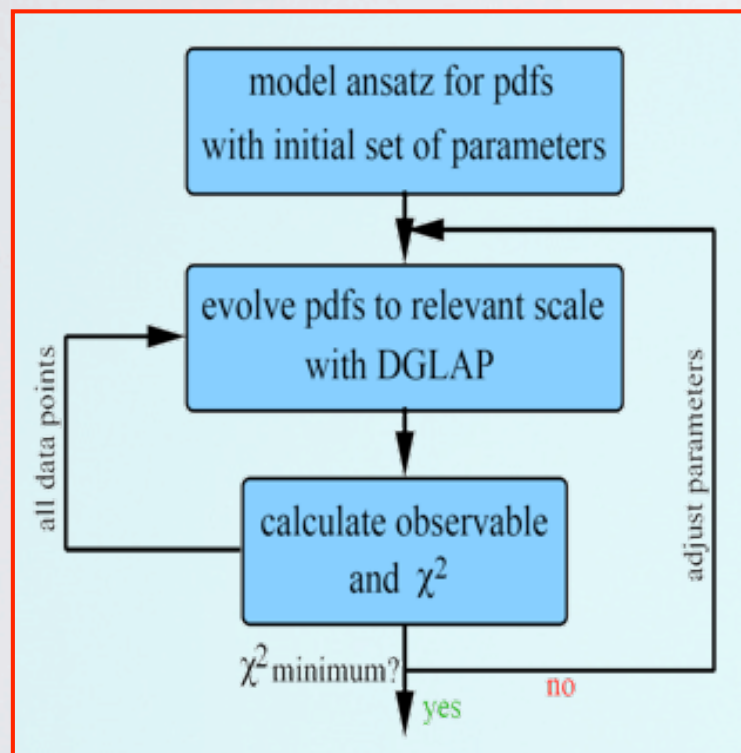
- optimum parameters determined from standard chi-squared optimization

$$\chi^2 \equiv \sum_i \omega_i \frac{(\text{d}\sigma_i^{\text{exp}} - \text{d}\sigma_i^{\text{th}})^2}{\Delta_i^2}$$

relative normalization or artificial weights for certain data sets **not needed/used in DSSZ analysis**

uncertainty for each point

DSSZ: add sys + stat in quadrature [+ theor. unc.]



optimum set of parameters

total $\chi^2 : 1544.7/1579\text{pts.}$
 $\chi^2/\text{d.o.f} : 0.994$

measurement	collaboration	# points	χ^2
$F_2^{\text{He}}/F_2^{\text{D}}$	NMC	17	18.18
	E139	18	2.71
$F_2^{\text{Li}}/F_2^{\text{D}}$	NMC	17	17.35
$F_2^{\text{Li}}/F_2^{\text{D}} Q^2 \text{ dep.}$	NMC	179	197.36
$F_2^{\text{Be}}/F_2^{\text{D}}$	E139	17	44.17
$F_2^{\text{C}}/F_2^{\text{D}}$	NMC	17	27.85
	E139	7	9.66
	EMC	9	6.41
$F_2^{\text{C}}/F_2^{\text{D}} Q^2 \text{ dep.}$	NMC	191	201.63
$F_2^{\text{Al}}/F_2^{\text{D}}$	E139	17	13.22
$F_2^{\text{Ca}}/F_2^{\text{D}}$	NMC	16	18.60
	E139	7	12.13
$F_2^{\text{Cu}}/F_2^{\text{D}}$	EMC	19	18.62
$F_2^{\text{Fe}}/F_2^{\text{D}}$	E139	23	34.95
$F_2^{\text{Ag}}/F_2^{\text{D}}$	E139	7	9.71
$F_2^{\text{Sn}}/F_2^{\text{D}}$	EMC	8	16.59
$F_2^{\text{Au}}/F_2^{\text{D}}$	E139	18	10.46
$F_2^{\text{C}}/F_2^{\text{Li}}$	NMC	24	33.17
$F_2^{\text{Ca}}/F_2^{\text{Li}}$	NMC	24	25.31
$F_2^{\text{Be}}/F_2^{\text{C}}$	NMC	15	11.76
$F_2^{\text{Al}}/F_2^{\text{C}}$	NMC	15	6.93
$F_2^{\text{Ca}}/F_2^{\text{C}}$	NMC	15	7.71
$F_2^{\text{Ca}}/F_2^{\text{C}}$	NMC	24	26.09
$F_2^{\text{Fe}}/F_2^{\text{C}}$	NMC	15	10.38
$F_2^{\text{Sn}}/F_2^{\text{C}}$	NMC	15	4.69
$F_2^{\text{Sn}}/F_2^{\text{C}} Q^2 \text{ dep.}$	NMC	145	102.31
$F_2^{\text{Pb}}/F_2^{\text{C}}$	NMC	15	9.57
F_2^{Fe}	NuTeV	78	109.65
F_3^{Fe}	NuTeV	75	79.78
F_2^{Fe}	CDHSW	120	108.20
F_3^{Fe}	CDHSW	133	90.57
F_2^{Pb}	CHORUS	63	20.42
F_3^{Pb}	CHORUS	63	79.58
$d\sigma_{\text{DY}}^{\text{C}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	9.87
$d\sigma_{\text{DY}}^{\text{Ca}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	5.38
$d\sigma_{\text{DY}}^{\text{Fe}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	9.77
$d\sigma_{\text{DY}}^{\text{W}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	19.29
$d\sigma_{\text{DY}}^{\text{Fe}}/d\sigma_{\text{DY}}^{\text{Be}}$	E866	28	20.34
$d\sigma_{\text{DY}}^{\text{W}}/d\sigma_{\text{DY}}^{\text{Be}}$	E866	28	26.07
$d\sigma_{\pi^0}^{\text{dAu}}/d\sigma_{\pi^0}^{\text{pp}}$	PHENIX	20	27.71
$d\sigma_{\pi^0}^{\text{dAu}}/d\sigma_{\pi^0}^{\text{pp}}$	STAR	11	3.92
$d\sigma_{\pi^\pm}^{\text{dAu}}/d\sigma_{\pi^\pm}^{\text{pp}}$	STAR	30	36.63
Total		1579	1544.70

NC DIS
897.5/894

CC DIS
488.2/532

Drell Yan
90.7/92

dAu->piX 68.3/61

overall quality of the fit

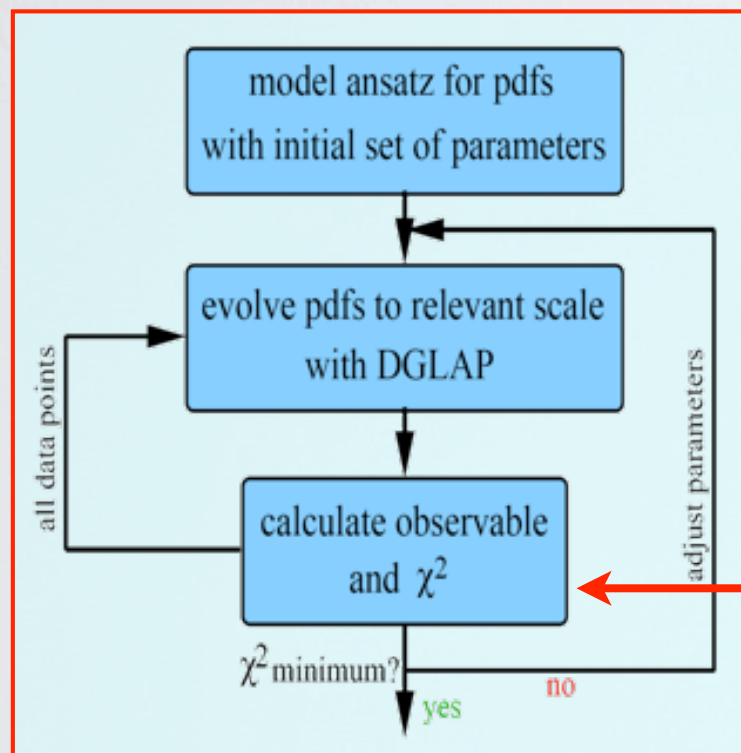
- optimum parameters determined from standard chi-squared optimization

$$\chi^2 \equiv \sum_i \omega_i \frac{(\text{d}\sigma_i^{\text{exp}} - \text{d}\sigma_i^{\text{th}})^2}{\Delta_i^2}$$

relative normalization or artificial weights for certain data sets **not needed/used in DSSZ analysis**

uncertainty for each point

DSSZ: add sys + stat in quadrature [+ theor. unc.]



optimum set of parameters

total $\chi^2 : 1544.7/1579\text{pts.}$
 $\chi^2/\text{d.o.f} : 0.994$

measurement	collaboration	# points	χ^2
$F_2^{\text{He}}/F_2^{\text{D}}$	NMC	17	18.18
	E139	18	2.71
$F_2^{\text{Li}}/F_2^{\text{D}}$	NMC	17	17.35
$F_2^{\text{Li}}/F_2^{\text{D}} Q^2 \text{ dep.}$	NMC	179	197.36
$F_2^{\text{Be}}/F_2^{\text{D}}$	E139	17	44.17
$F_2^{\text{C}}/F_2^{\text{D}}$	NMC	17	27.85
	E139	7	9.66
	EMC	9	6.41
$F_2^{\text{C}}/F_2^{\text{D}} Q^2 \text{ dep.}$	NMC	191	201.63
$F_2^{\text{Al}}/F_2^{\text{D}}$	E139	17	13.22
$F_2^{\text{Ca}}/F_2^{\text{D}}$	NMC	16	18.60
	E139	7	12.13
$F_2^{\text{Cu}}/F_2^{\text{D}}$	EMC	19	18.62
$F_2^{\text{Fe}}/F_2^{\text{D}}$	E139	23	34.95
$F_2^{\text{Ag}}/F_2^{\text{D}}$	E139	7	9.71
$F_2^{\text{Sn}}/F_2^{\text{D}}$	EMC	8	16.59
$F_2^{\text{Au}}/F_2^{\text{D}}$	E139	18	10.46
$F_2^{\text{C}}/F_2^{\text{Li}}$	NMC	24	33.17
$F_2^{\text{Ca}}/F_2^{\text{Li}}$	NMC	24	25.31
$F_2^{\text{Be}}/F_2^{\text{C}}$	NMC	15	11.76
$F_2^{\text{Al}}/F_2^{\text{C}}$	NMC	15	6.93
$F_2^{\text{Ca}}/F_2^{\text{C}}$	NMC	15	7.71
$F_2^{\text{Ca}}/F_2^{\text{C}}$	NMC	24	26.09
$F_2^{\text{Fe}}/F_2^{\text{C}}$	NMC	15	10.38
$F_2^{\text{Sn}}/F_2^{\text{C}}$	NMC	15	4.69
$F_2^{\text{Sn}}/F_2^{\text{C}} Q^2 \text{ dep.}$	NMC	145	102.31
$F_2^{\text{Pb}}/F_2^{\text{C}}$	NMC	15	9.57
F_2^{vFe}	NuTeV	78	109.65
F_3^{vFe}	NuTeV	75	79.78
F_2^{vFe}	CDHSW	120	108.20
F_3^{vFe}	CDHSW	133	90.57
F_2^{vPb}	CHORUS	63	20.42
F_3^{vPb}	CHORUS	63	79.58
$d\sigma_{\text{DY}}^{\text{C}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	9.87
$d\sigma_{\text{DY}}^{\text{Ca}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	5.38
$d\sigma_{\text{DY}}^{\text{Fe}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	9.77
$d\sigma_{\text{DY}}^{\text{W}}/d\sigma_{\text{DY}}^{\text{D}}$	E772	9	19.29
$d\sigma_{\text{DY}}^{\text{Fe}}/d\sigma_{\text{DY}}^{\text{Be}}$	E866	28	20.34
$d\sigma_{\text{DY}}^{\text{W}}/d\sigma_{\text{DY}}^{\text{Be}}$	E866	28	26.07
$d\sigma_{\pi^0}^{\text{dAu}}/d\sigma_{\pi^0}^{\text{pp}}$	PHENIX	20	27.71
$d\sigma_{\pi^0}^{\text{dAu}}/d\sigma_{\pi^0}^{\text{pp}}$	STAR	11	3.92
$d\sigma_{\pi^\pm}^{\text{dAu}}/d\sigma_{\pi^\pm}^{\text{pp}}$	STAR	30	36.63
Total		1579	1544.70

NC DIS
897.5/894

CC DIS
488.2/532

Drell Yan
90.7/92

dAu->piX 68.3/61

technical aspects: Mellin technique

source of trouble: ubiquitous convolutions

$$d\sigma_{\text{DIS}}^A = \sum_i f_i^A \otimes d\hat{\sigma}_{i\gamma^* \rightarrow X}$$

$$d\sigma_{\text{DY}}^A = \sum_{ij} f_i^p \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow l\bar{l}X}$$

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

$$\otimes: g(x) = \int_x^1 \frac{dy}{y} f(y) P\left(\frac{x}{y}\right)$$

increasing level of painfulness

technical aspects: Mellin technique

source of trouble: ubiquitous convolutions

$$d\sigma_{\text{DIS}}^A = \sum_i f_i^A \otimes d\hat{\sigma}_{i\gamma^* \rightarrow X}$$

$$d\sigma_{\text{DY}}^A = \sum_{ij} f_i^p \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow l\bar{l}X}$$

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

$$\otimes: g(x) = \int_x^1 \frac{dy}{y} f(y) P\left(\frac{x}{y}\right)$$

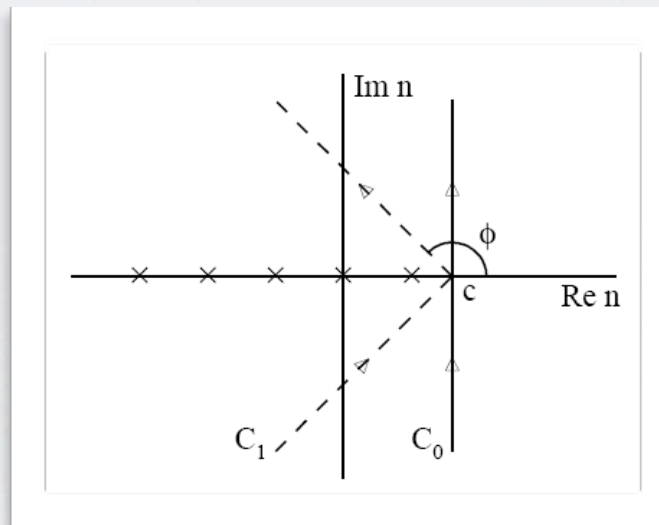
increasing level of painfulness

“natural language” for pQCD calculations: **Mellin moments**

$$\phi(N) \equiv \int_0^1 dx x^{N-1} \phi(x)$$

integral transformation
complex Mellin N space

$$\phi(x) \equiv \frac{1}{2\pi i} \int_{C_N} dN x^{-N} \phi(N)$$



R.H. Mellin
Finnish mathematician
1854 - 1933

technical aspects: Mellin technique

source of trouble: ubiquitous convolutions

$$d\sigma_{\text{DIS}}^A = \sum_i f_i^A \otimes d\hat{\sigma}_{i\gamma^* \rightarrow X}$$

$$d\sigma_{\text{DY}}^A = \sum_{ij} f_i^p \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow l\bar{l}X}$$

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

$$\otimes: g(x) = \int_x^1 \frac{dy}{y} f(y) P\left(\frac{x}{y}\right)$$

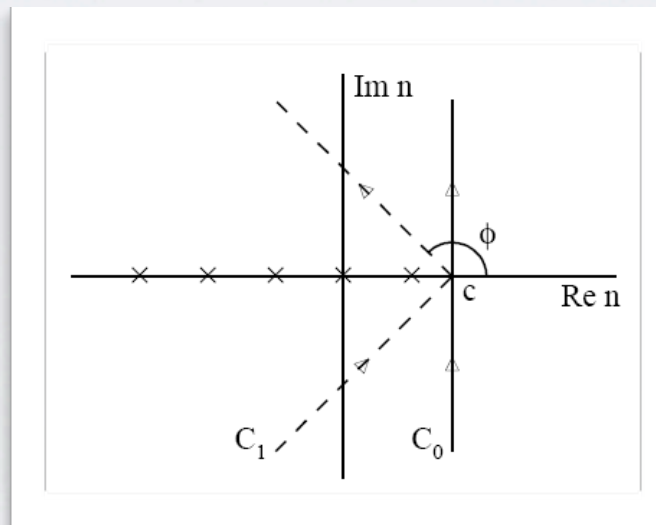
increasing level of painfulness

“natural language” for pQCD calculations: **Mellin moments**

$$\phi(N) \equiv \int_0^1 dx x^{N-1} \phi(x)$$

integral transformation
complex Mellin N space

$$\phi(x) \equiv \frac{1}{2\pi i} \int_{C_N} dN x^{-N} \phi(N)$$



R.H. Mellin
Finnish mathematician
1854 - 1933

well-known property: convolutions factorize into simple products

$$g(n) = f(n) \times P(n)$$

- ✓ analytic solution to DGLAP evolution equations in Mellin space
- ✓ analytic expressions for DIS coefficient functions in Mellin space
- ✓ efficient numerical way to deal with complicated pp/pA cross sections

MS, Vogelsang - hep-ph/0108241

numerically very efficient
no K factor approximations needed

technical aspects: heavy flavors in CC DIS



charm production in CC DIS is of particular interest

idea: at LO $W^+ s' \rightarrow c$ $s' \equiv |V_{cs}|^2 s + |V_{cd}|^2 d$

- ▶ important to include charm mass through **slow rescaling prescription** $\xi = x(1 + m^2/Q^2)$ Barnett '76
- ▶ prescription also needed for consistent factorization of collinear singularities in NLO Gottschalk '81

technical aspects: heavy flavors in CC DIS



charm production in CC DIS is of particular interest

idea: at LO $W^+ s' \rightarrow c$ $s' \equiv |V_{cs}|^2 s + |V_{cd}|^2 d$

- ▶ important to include charm mass through **slow rescaling prescription** $\xi = x(1 + m^2/Q^2)$ Barnett '76
- ▶ prescription also needed for consistent factorization of collinear singularities in NLO Gottschalk '81

used to extract strangeness from CC neutrino data in proton PDF fits

need to control nuclear corrections for Fe and Pb targets

technical aspects: heavy flavors in CC DIS



charm production in CC DIS is of particular interest

idea: at LO $W^+ s' \rightarrow c$ $s' \equiv |V_{cs}|^2 s + |V_{cd}|^2 d$

- ▶ important to include charm mass through **slow rescaling prescription** $\xi = x(1 + m^2/Q^2)$ Barnett '76
- ▶ prescription also needed for consistent factorization of collinear singularities in NLO Gottschalk '81

used to extract strangeness from CC neutrino data in proton PDF fits

need to control nuclear corrections for Fe and Pb targets

complication: gluonic contributions in NLO Gottschalk '81; Gluck, Kretzer, Reya '96; Kretzer, MS '99

- ▶ dilute sensitivity to strangeness $W g \rightarrow c \bar{s}'$
- ▶ keeping charm mass gets more complicated

$$\mathcal{F}_i^c(\mathbf{x}) = s'(\xi) + \frac{\alpha_s}{2\pi} \int_{\xi}^1 \frac{d\zeta}{\zeta} \left[\mathbf{H}_i^{(1),q}(\zeta) s'(\frac{\xi}{\zeta}) + \mathbf{H}_i^{(1),g}(\zeta) g(\frac{\xi}{\zeta}) \right]$$

- ▶ make use of recently obtained expressions in Mellin space Blumlein, Hasselhuhn, Kovacikova, Moch

$$\mathcal{F}_i^c(\mathbf{N}) = s'(\mathbf{N}) + \frac{\alpha_s}{2\pi} \left[\mathbf{H}_i^{(1),q}(\mathbf{N}) s'(\mathbf{N}) + \mathbf{H}_i^{(1),g}(\mathbf{N}) g(\mathbf{N}) \right]$$

technical aspects: heavy flavors in CC DIS



charm production in CC DIS is of particular interest

idea: at LO $W^+ s' \rightarrow c$ $s' \equiv |V_{cs}|^2 s + |V_{cd}|^2 d$

- ▶ important to include charm mass through **slow rescaling prescription** $\xi = x(1 + m^2/Q^2)$ Barnett '76
- ▶ prescription also needed for consistent factorization of collinear singularities in NLO Gottschalk '81

used to extract strangeness from CC neutrino data in proton PDF fits

need to control nuclear corrections for Fe and Pb targets

complication: gluonic contributions in NLO Gottschalk '81; Gluck, Kretzer, Reya '96; Kretzer, MS '99

- ▶ dilute sensitivity to strangeness $W g \rightarrow c \bar{s}'$
- ▶ keeping charm mass gets more complicated

$$\mathcal{F}_i^c(\mathbf{x}) = s'(\xi) + \frac{\alpha_s}{2\pi} \int_{\xi}^1 \frac{d\zeta}{\zeta} \left[\mathbf{H}_i^{(1),q}(\zeta) s'(\frac{\xi}{\zeta}) + \mathbf{H}_i^{(1),g}(\zeta) g(\frac{\xi}{\zeta}) \right]$$

- ▶ make use of recently obtained expressions in Mellin space Blumlein, Hasselhuhn, Kovacikova, Moch

$$\mathcal{F}_i^c(\mathbf{N}) = s'(\mathbf{N}) + \frac{\alpha_s}{2\pi} \left[\mathbf{H}_i^{(1),q}(\mathbf{N}) s'(\mathbf{N}) + \mathbf{H}_i^{(1),g}(\mathbf{N}) g(\mathbf{N}) \right]$$

positive impact on quality of our fit to CC DIS data: 26% gain in χ^2

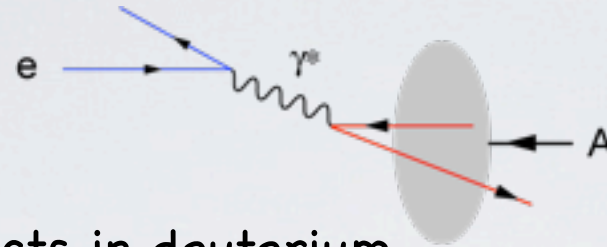
review of charged lepton DIS data

fit all “classic” EMC, NMC, and E-139 DIS data

► impose cut $Q^2 > 1 \text{ GeV}^2$

► $\chi^2 = 857.5/894\text{pts.}$

► neglect, as usual, nuclear effects in deuterium
found to be small in Hirai, Kumano, Nagai



recall

main constraint
from DIS data $0.01 \lesssim x \lesssim 0.8$

$$F_2^A(N) = x \sum_q e_q^2 \left[(q^A(N) + \bar{q}^A(N)) \left(1 + \frac{\alpha_s}{2\pi} C_2^q(N) \right) + \frac{\alpha_s}{2\pi} C_2^g(N) g^A(N) \right]$$

weak indirect constraint
from scale evolution

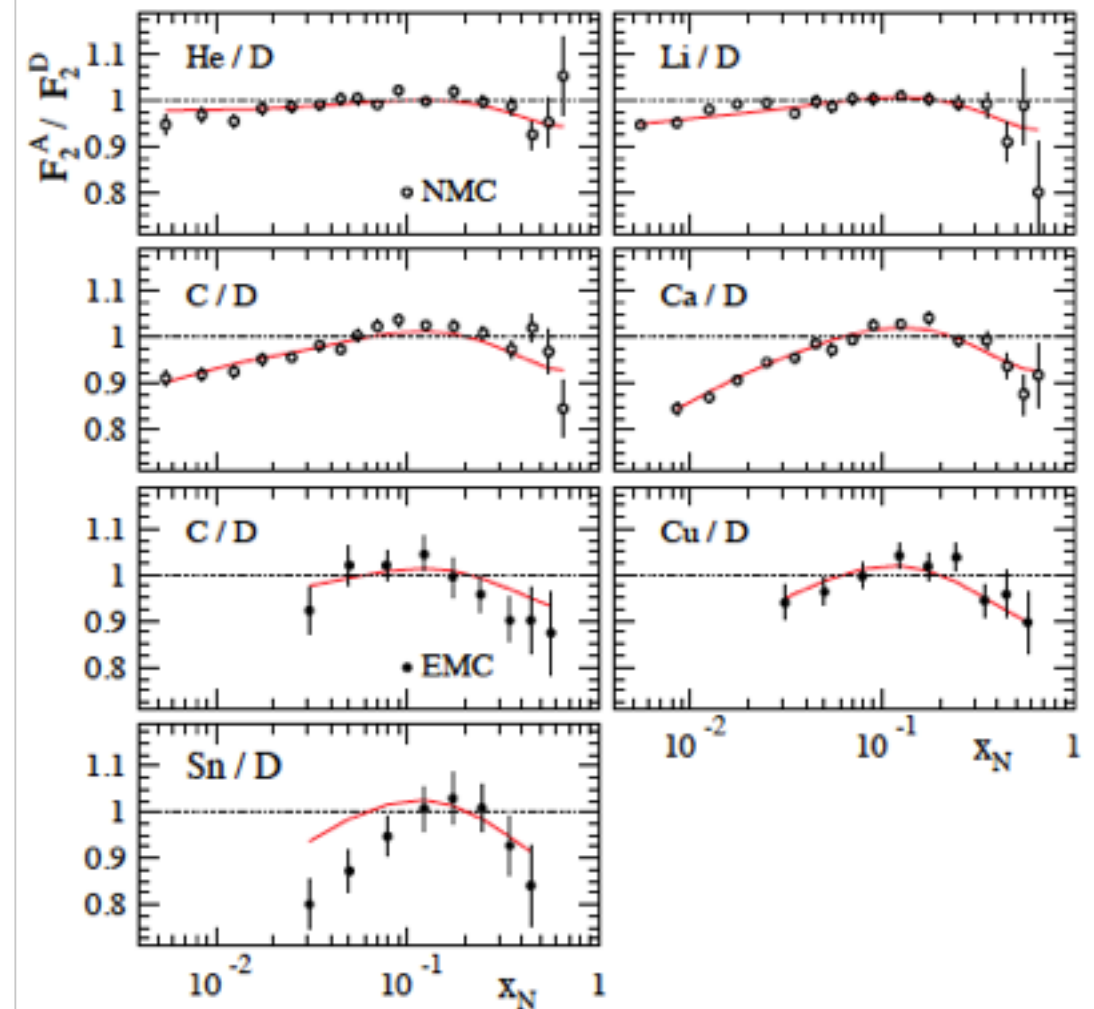
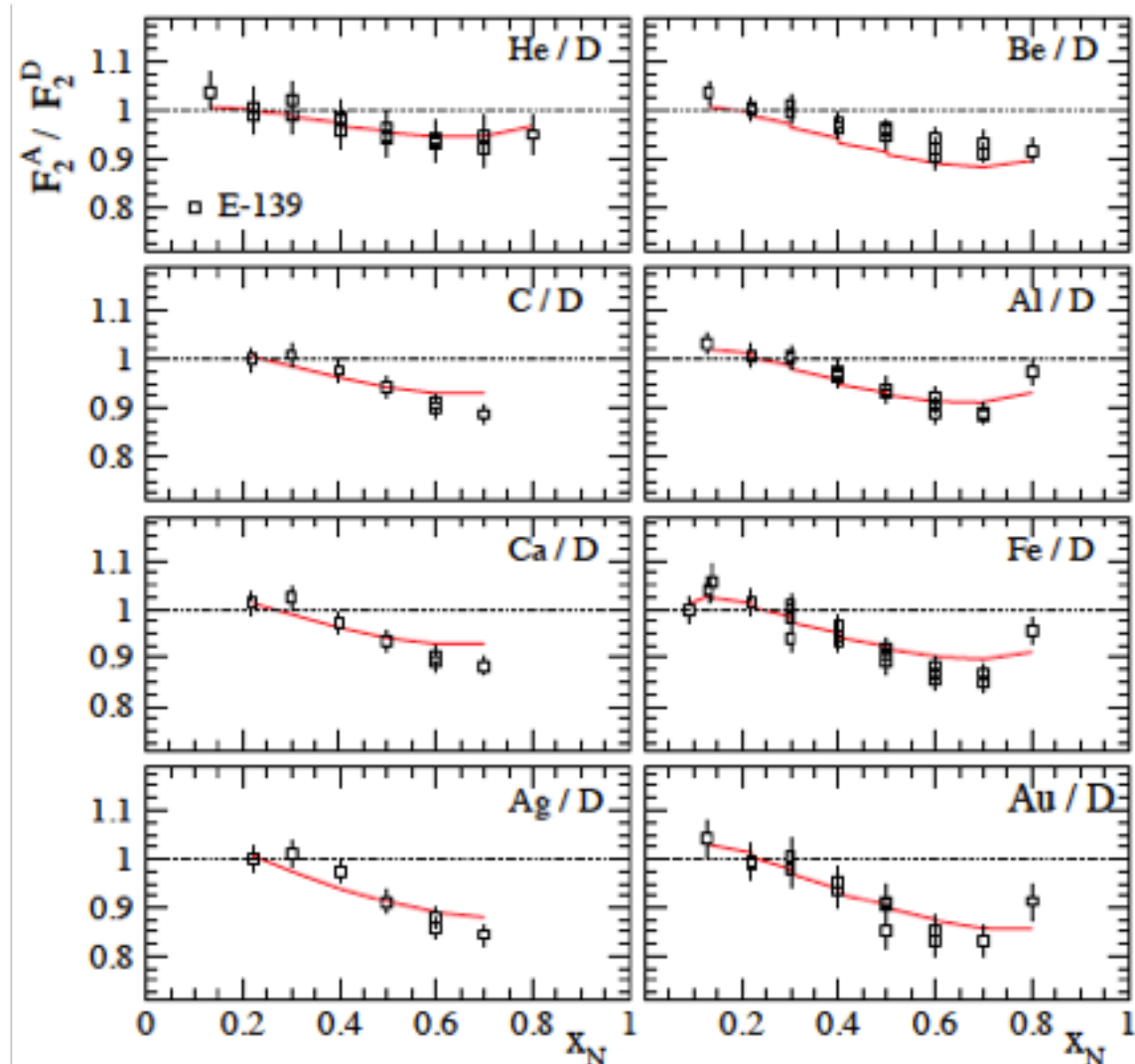
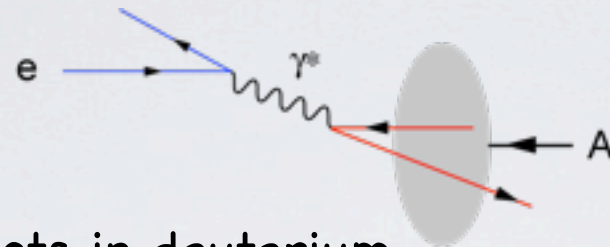
review of charged lepton DIS data

fit all "classic" EMC, NMC, and E-139 DIS data

► impose cut $Q^2 > 1 \text{ GeV}^2$

► $\chi^2 = 857.5/894\text{pts.}$

► neglect, as usual, nuclear effects in deuterium found to be small in Hirai, Kumano, Nagai



recall

main constraint
from DIS data $0.01 \lesssim x \lesssim 0.8$

$$F_2^A(N) = x \sum_q e_q^2 \left[(q^A(N) + \bar{q}^A(N)) \left(1 + \frac{\alpha_s}{2\pi} C_2^q(N) \right) + \frac{\alpha_s}{2\pi} C_2^g(N) g^A(N) \right]$$

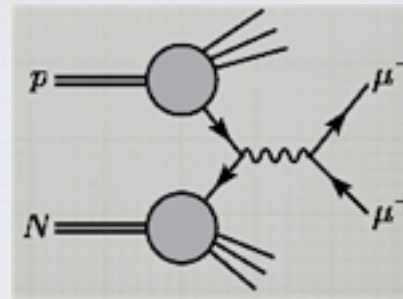
weak indirect constraint
from scale evolution

Drell Yan di-muon data

fit all **E772** and **E866** DY pA data

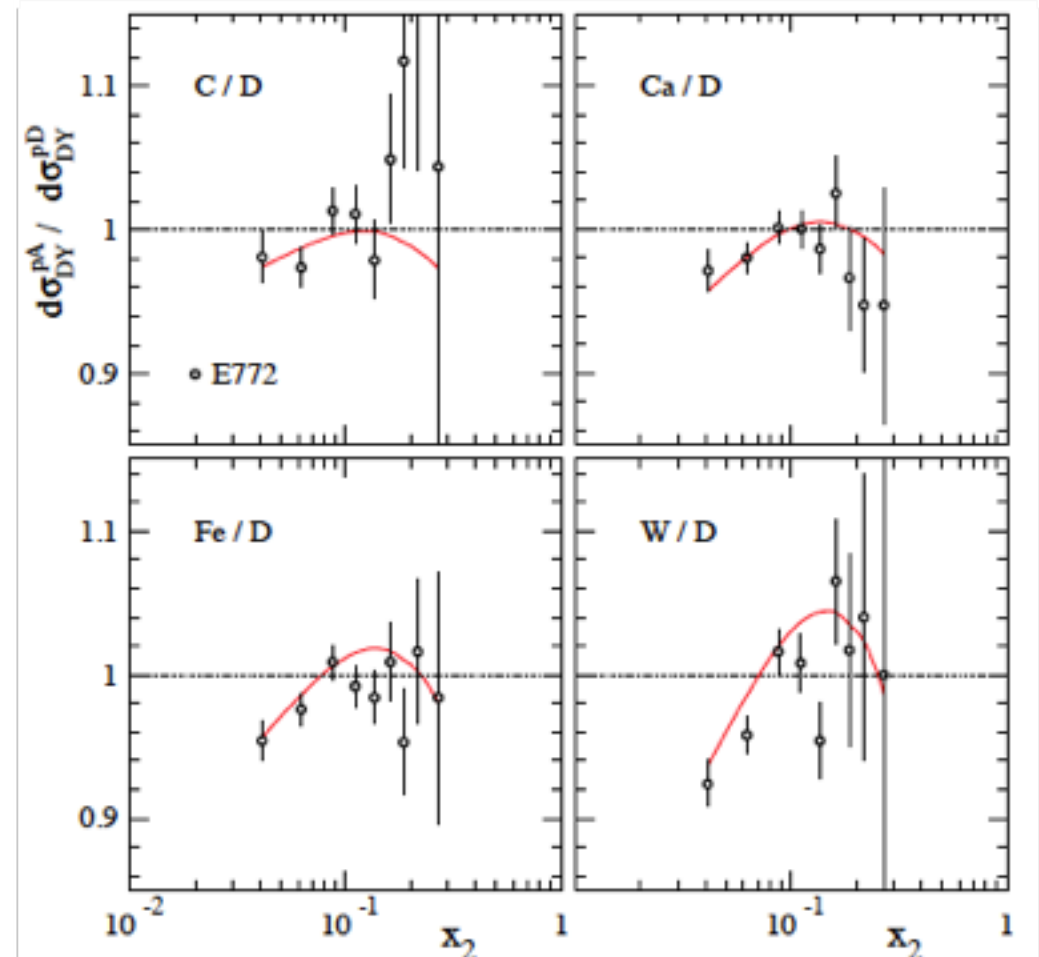
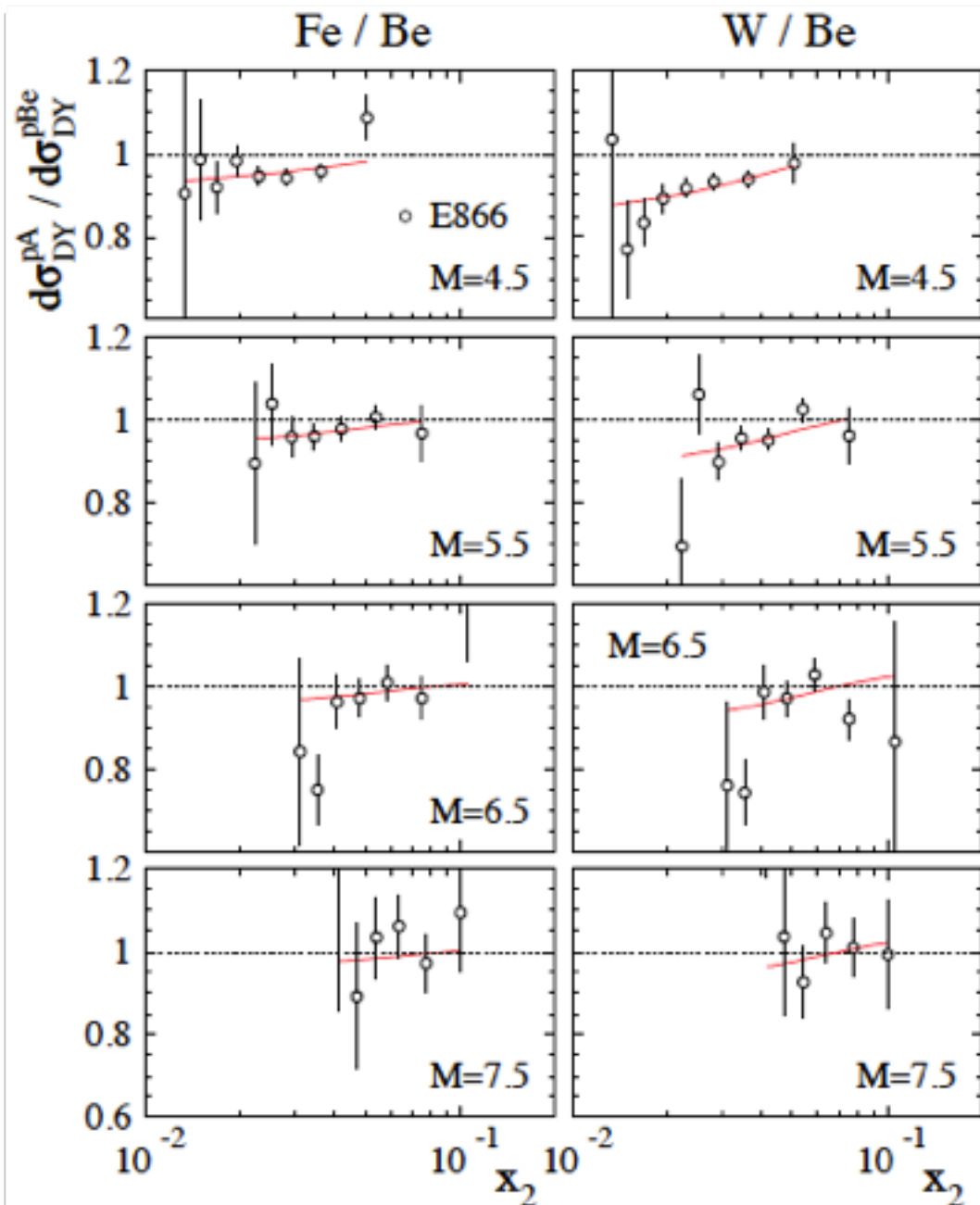
► di-muons have inv. mass $M > 4$ GeV (sets scale)

► $\chi^2 = 90.7/92\text{pts.}$



$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$

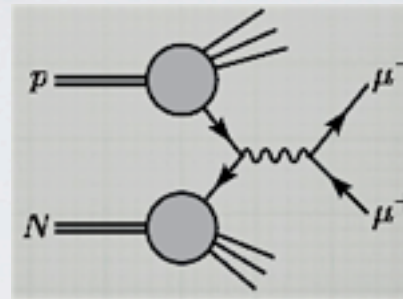
$$\frac{d^2\sigma}{dM dy} = \frac{4\pi\alpha^2}{9M^3} \sum_{ij} \int dx_1 dx_2 f_i^p(x_1) f_j^A(x_2) \frac{d\hat{\sigma}_{ij}}{dM dy}$$



Drell Yan di-muon data

fit all **E772** and **E866** DY pA data

- ▶ di-muons have inv. mass $M > 4$ GeV (sets scale)
- ▶ $\chi^2 = 90.7/92\text{pts.}$

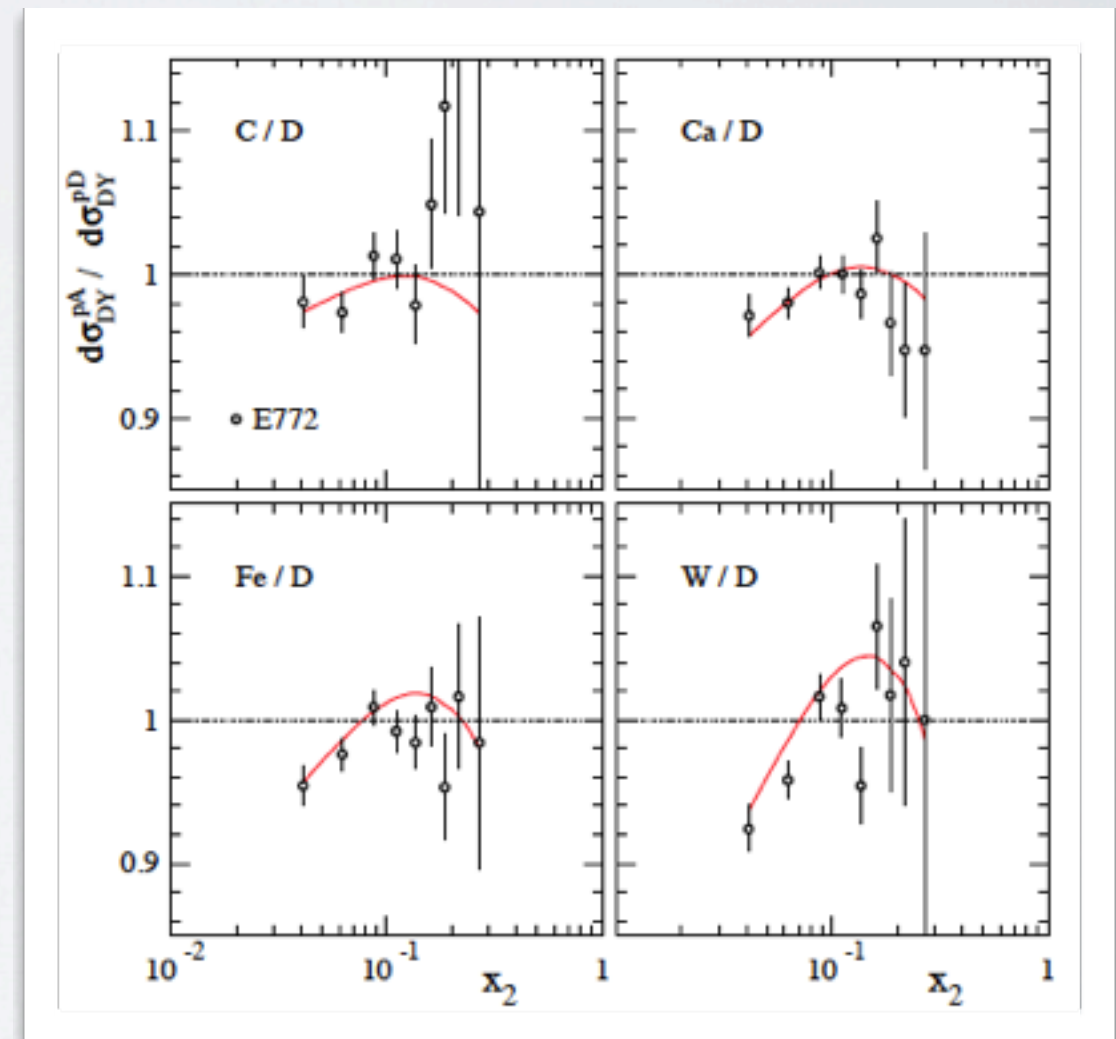
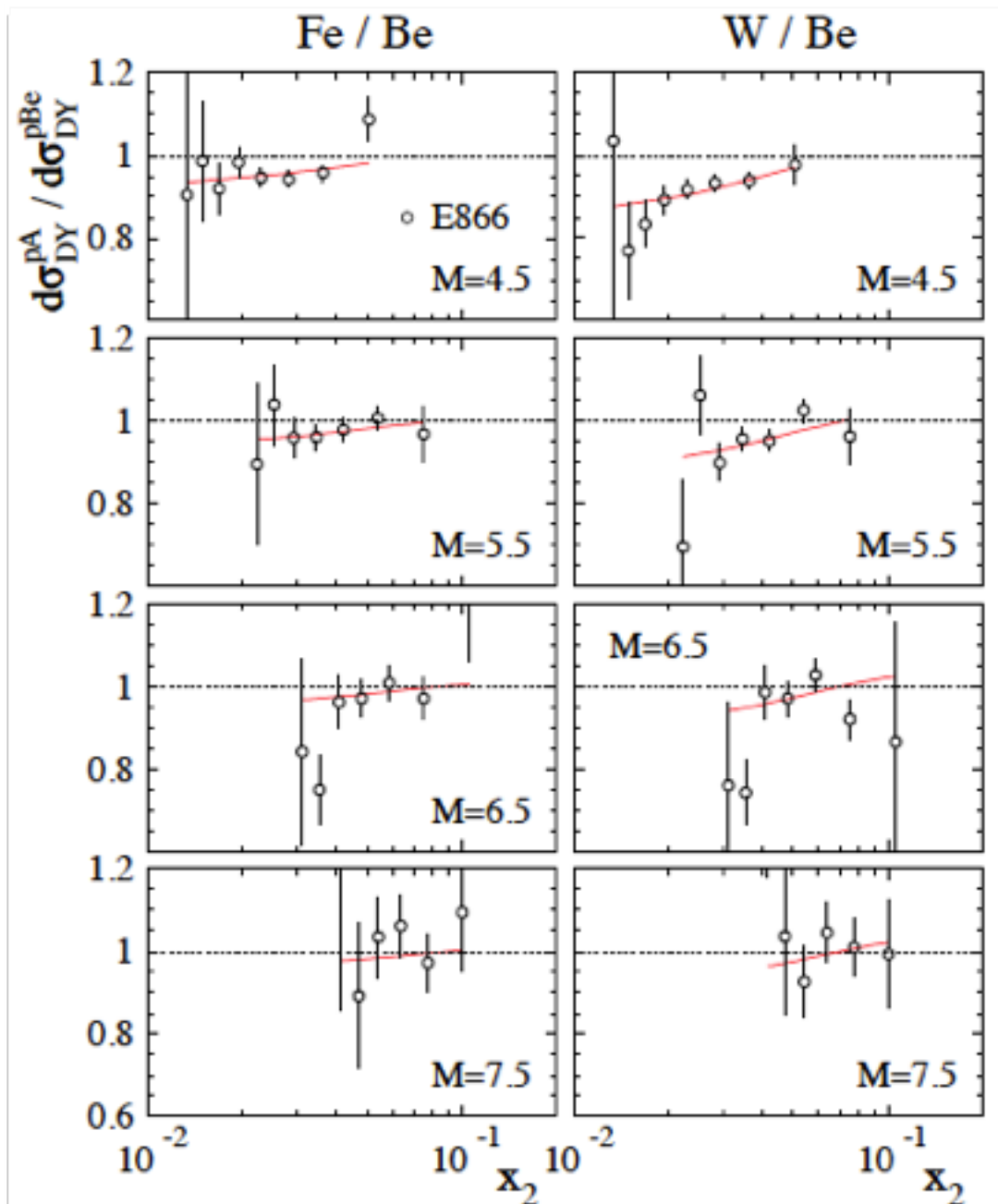


$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$

DY data mainly help to
disentangle val/sea quarks
gluons through evolution

$$\frac{d^2\sigma}{dMdy} = \frac{4\pi\alpha^2}{9M^3} \sum_{ij} \int dx_1 dx_2 f_i^p(x_1) f_j^A(x_2) \frac{d\hat{\sigma}_{ij}}{dMdy}$$

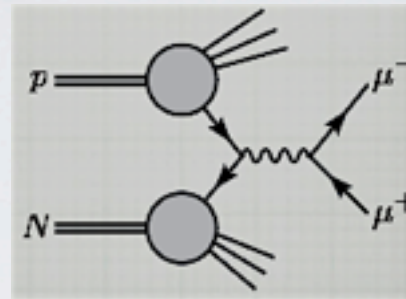
$x_2 \in [0.01, 0.2]$



Drell Yan di-muon data

fit all **E772** and **E866** DY pA data

- ▶ di-muons have inv. mass $M > 4$ GeV (sets scale)
- ▶ $\chi^2 = 90.7/92\text{pts.}$



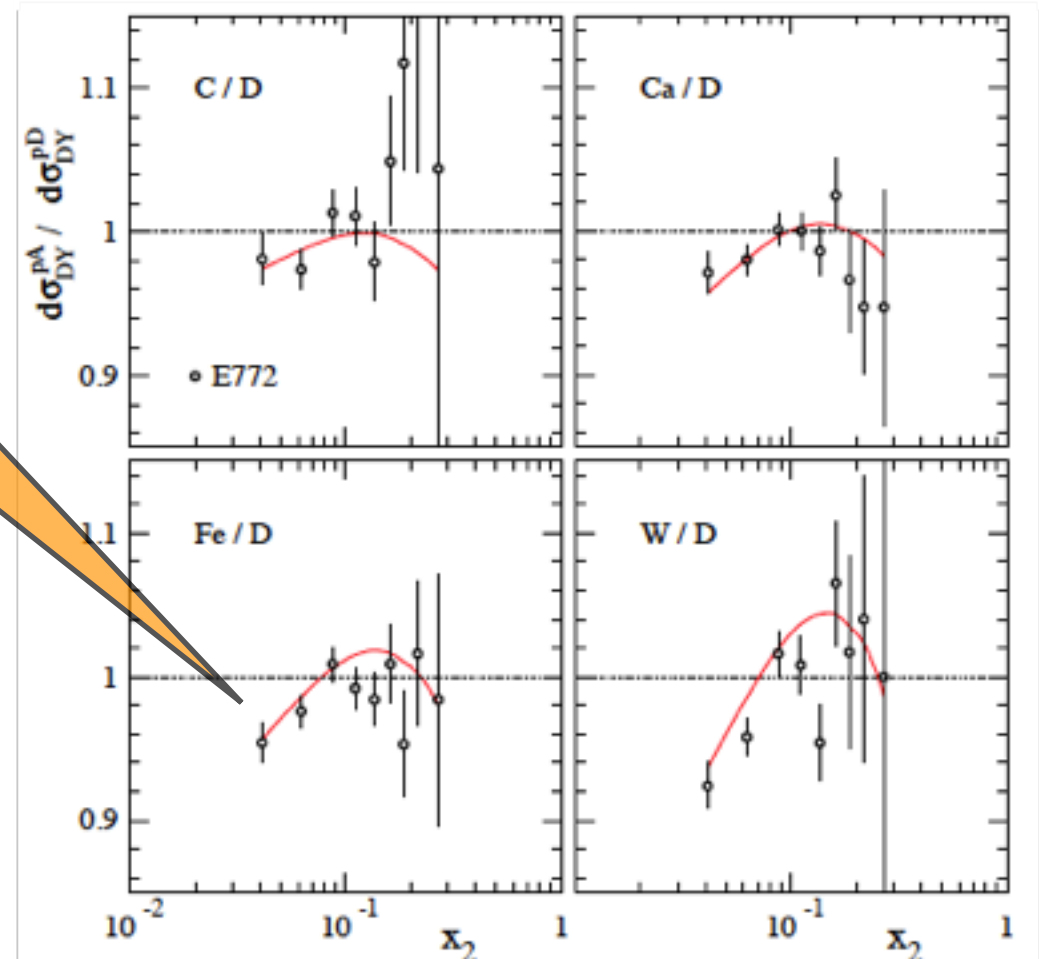
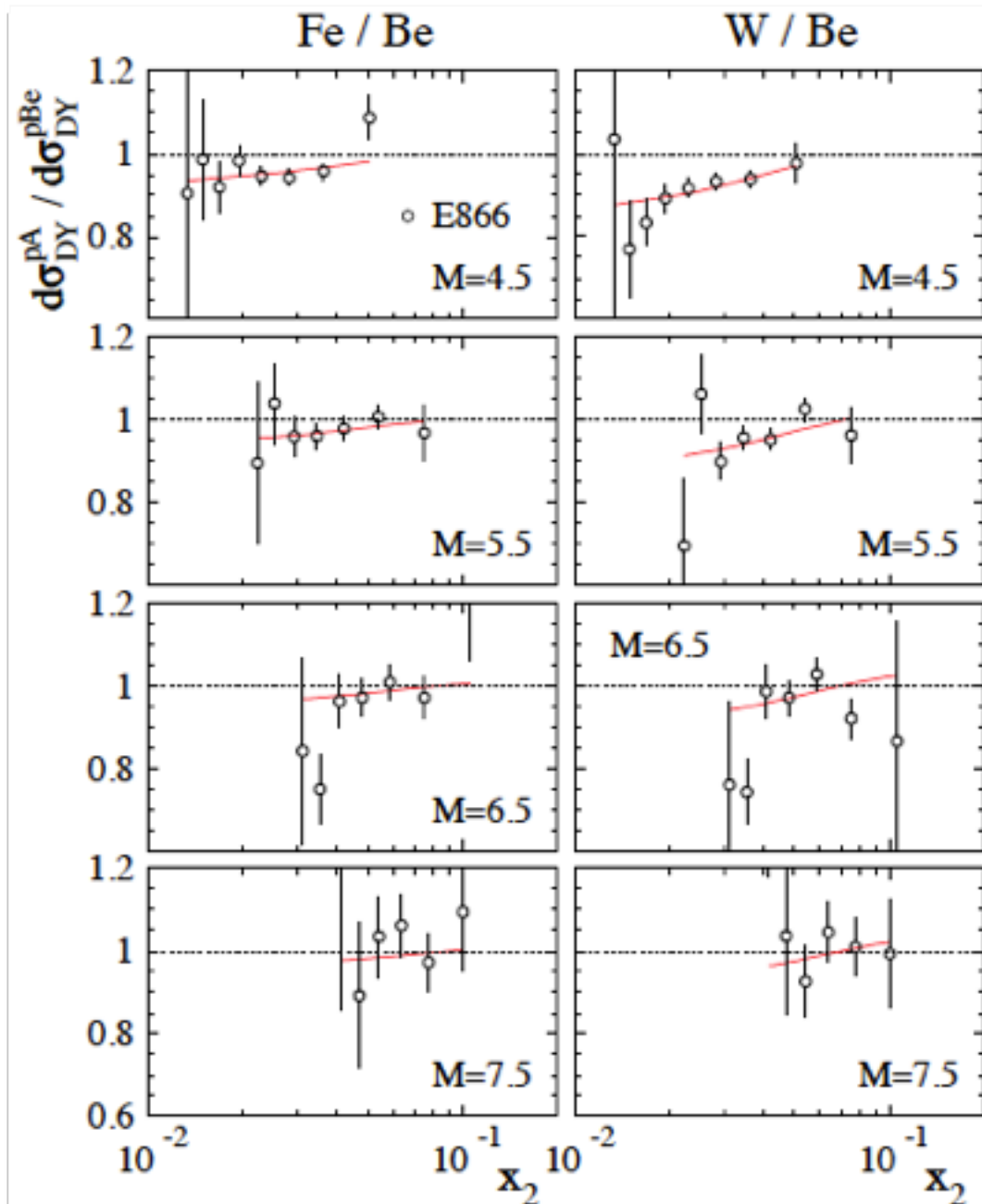
$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$

DY data mainly help to
disentangle val/sea quarks
gluons through evolution

$$\frac{d^2\sigma}{dMdy} = \frac{4\pi\alpha^2}{9M^3} \sum_{ij} \int dx_1 dx_2 f_i^p(x_1) f_j^A(x_2) \frac{d\hat{\sigma}_{ij}}{dMdy}$$

$x_2 \in [0.01, 0.2]$

"evidence"
for shadowing
of sea quarks

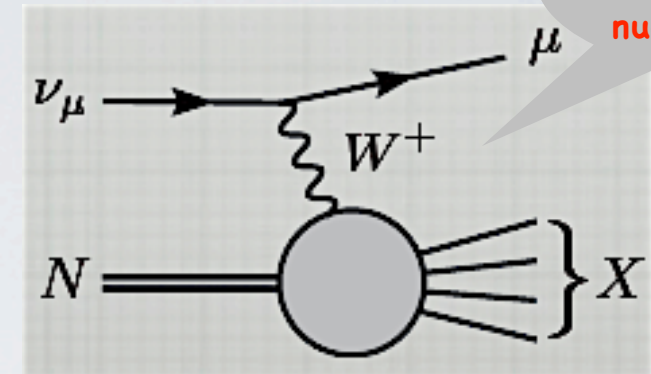


CC neutrino DIS data

fit CDHSW, NuTeV, and CHORUS str. fct. data

substantial interest:

- nCTEQ claim of “**factorization breaking**” for nPDFs
- neutrino data are a vital constraint on strangeness (and help to separate quark flavors) in proton PDF fits



does a W interact differently with nuclear matter?

$$\frac{d^2\sigma^{\nu A, \bar{\nu} A}}{dx dy} \simeq xy^2 F_1^{\nu A, \bar{\nu} A} + (1-y) F_2^{\nu A, \bar{\nu} A} \pm xy\left(1 - \frac{y}{2}\right) F_3^{\nu A, \bar{\nu} A}$$

CC neutrino DIS data

fit **CDHSW**, **NuTeV**, and **CHORUS** str. fct. data

substantial interest:

- ▶ **nCTEQ** claim of “**factorization breaking**” for nPDFs
- ▶ neutrino data are a vital constraint on strangeness (and help to separate quark flavors) in proton PDF fits

here is how the “tension” story goes

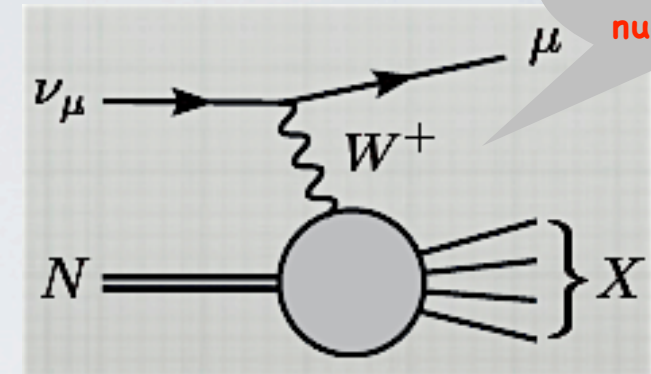
- ▶ CC DIS data probe different combinations of up-/down-type quarks than charged-lepton DIS
- ▶ neutrino and antineutrino beams probe 4 different structure functions

$$F_2^{\nu A}(\mathbf{x}_N) \simeq \mathbf{x}_N [\bar{\mathbf{u}}^A + \bar{\mathbf{c}}^A + \mathbf{d}^A + \mathbf{s}^A] (\mathbf{x}_N)$$

$$F_2^{\bar{\nu} A}(\mathbf{x}_N) \simeq \mathbf{x}_N [\mathbf{u}^A + \mathbf{c}^A + \bar{\mathbf{d}}^A + \bar{\mathbf{s}}^A] (\mathbf{x}_N)$$

$$F_3^{\nu A}(\mathbf{x}_N) \simeq [-(\bar{\mathbf{u}}^A + \bar{\mathbf{c}}^A) + \mathbf{d}^A + \mathbf{s}^A] (\mathbf{x}_N)$$

$$F_3^{\bar{\nu} A}(\mathbf{x}_N) \simeq [\mathbf{u}^A + \mathbf{c}^A - (\bar{\mathbf{d}}^A + \bar{\mathbf{s}}^A)] (\mathbf{x}_N)$$



does a W interact differently with nuclear matter?

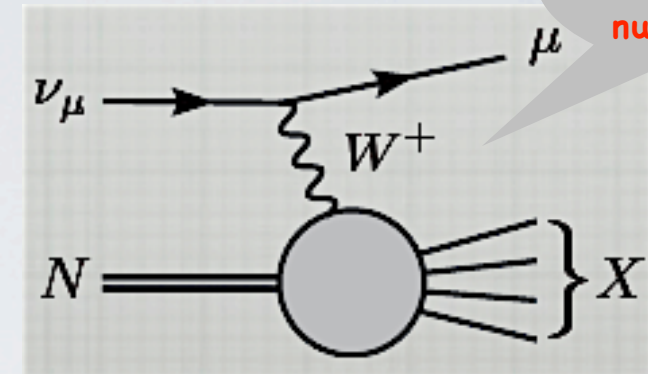
$$\frac{d^2 \sigma^{\nu A, \bar{\nu} A}}{dx dy} \simeq xy^2 F_1^{\nu A, \bar{\nu} A} + (1-y) F_2^{\nu A, \bar{\nu} A} \pm xy \left(1 - \frac{y}{2}\right) F_3^{\nu A, \bar{\nu} A}$$

CC neutrino DIS data

fit **CDHSW**, **NuTeV**, and **CHORUS** str. fct. data

substantial interest:

- ▶ **nCTEQ** claim of “**factorization breaking**” for nPDFs
- ▶ neutrino data are a vital constraint on strangeness (and help to separate quark flavors) in proton PDF fits



$$\frac{d^2\sigma^{\nu A, \bar{\nu} A}}{dx dy} \simeq xy^2 F_1^{\nu A, \bar{\nu} A} + (1-y) F_2^{\nu A, \bar{\nu} A} \pm xy(1 - \frac{y}{2}) F_3^{\nu A, \bar{\nu} A}$$

here is how the “tension” story goes

- ▶ CC DIS data probe different combinations of up-/down-type quarks than charged-lepton DIS
- ▶ neutrino and antineutrino beams probe 4 different structure functions

$$F_2^{\nu A}(\mathbf{x}_N) \simeq \mathbf{x}_N [\bar{u}^A + \bar{c}^A + d^A + s^A] (\mathbf{x}_N)$$

$$F_2^{\bar{\nu} A}(\mathbf{x}_N) \simeq \mathbf{x}_N [u^A + c^A + \bar{d}^A + \bar{s}^A] (\mathbf{x}_N)$$

$$F_3^{\nu A}(\mathbf{x}_N) \simeq [-(\bar{u}^A + \bar{c}^A) + d^A + s^A] (\mathbf{x}_N)$$

$$F_3^{\bar{\nu} A}(\mathbf{x}_N) \simeq [u^A + c^A - (\bar{d}^A + \bar{s}^A)] (\mathbf{x}_N)$$

- ▶ experiments extract (under certain assumptions)

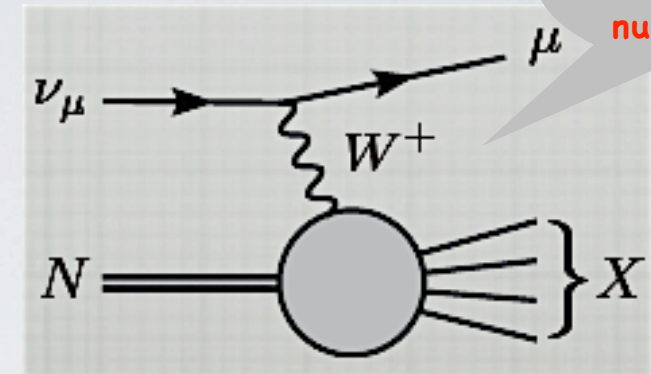
$$\mathbf{F}_{2,3} \equiv (\mathbf{F}_{2,3}^{\nu A} + \mathbf{F}_{2,3}^{\bar{\nu} A})/2 \longrightarrow \begin{cases} \bullet F_2 \text{ probes total quark singlet} \\ \bullet F_3 \text{ probes sum of valence PDFs} \end{cases}$$

CC neutrino DIS data

fit **CDHSW**, **NuTeV**, and **CHORUS** str. fct. data

substantial interest:

- **nCTEQ** claim of “**factorization breaking**” for nPDFs
- neutrino data are a vital constraint on strangeness (and help to separate quark flavors) in proton PDF fits



does a W interact differently with nuclear matter?

$$\frac{d^2\sigma^{\nu A, \bar{\nu} A}}{dx dy} \simeq xy^2 F_1^{\nu A, \bar{\nu} A} + (1-y) F_2^{\nu A, \bar{\nu} A} \pm xy(1 - \frac{y}{2}) F_3^{\nu A, \bar{\nu} A}$$

here is how the “tension” story goes

- CC DIS data probe different combinations of up-/down-type quarks than charged-lepton DIS
- neutrino and antineutrino beams probe 4 different structure functions

$$F_2^{\nu A}(\mathbf{x}_N) \simeq \mathbf{x}_N [\bar{u}^A + \bar{c}^A + d^A + s^A](\mathbf{x}_N)$$

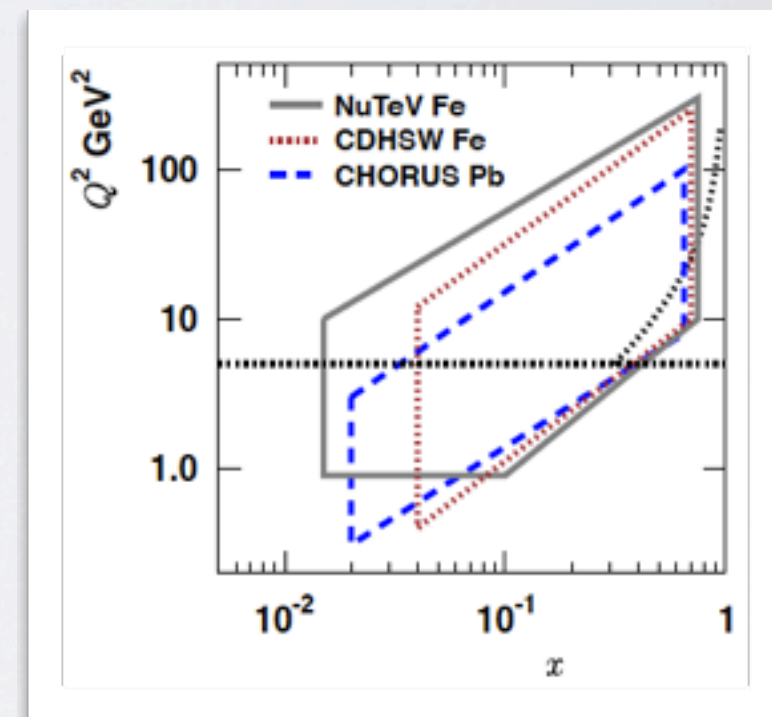
$$F_2^{\bar{\nu} A}(\mathbf{x}_N) \simeq \mathbf{x}_N [u^A + c^A + \bar{d}^A + \bar{s}^A](\mathbf{x}_N)$$

$$F_3^{\nu A}(\mathbf{x}_N) \simeq [-(\bar{u}^A + \bar{c}^A) + d^A + s^A](\mathbf{x}_N)$$

$$F_3^{\bar{\nu} A}(\mathbf{x}_N) \simeq [u^A + c^A - (\bar{d}^A + \bar{s}^A)](\mathbf{x}_N)$$

- experiments extract (under certain assumptions)

$$\mathbf{F}_{2,3} \equiv (\mathbf{F}_{2,3}^{\nu A} + \mathbf{F}_{2,3}^{\bar{\nu} A})/2 \longrightarrow \begin{cases} \bullet F_2 \text{ probes total quark singlet} \\ \bullet F_3 \text{ probes sum of valence PDFs} \end{cases}$$



kinematics overlaps with charged lepton DIS data

CC neutrino DIS data

fit **CDHSW**, **NuTeV**, and **CHORUS** str. fct. data

substantial interest:

- **nCTEQ** claim of “**factorization breaking**” for nPDFs
- neutrino data are a vital constraint on strangeness (and help to separate quark flavors) in proton PDF fits

here is how the “tension” story goes

- CC DIS data probe different combinations of up-/down-type quarks than charged-lepton DIS
- neutrino and antineutrino beams probe 4 different structure functions

$$F_2^{\nu A}(\mathbf{x}_N) \simeq \mathbf{x}_N [\bar{u}^A + \bar{c}^A + d^A + s^A](\mathbf{x}_N)$$

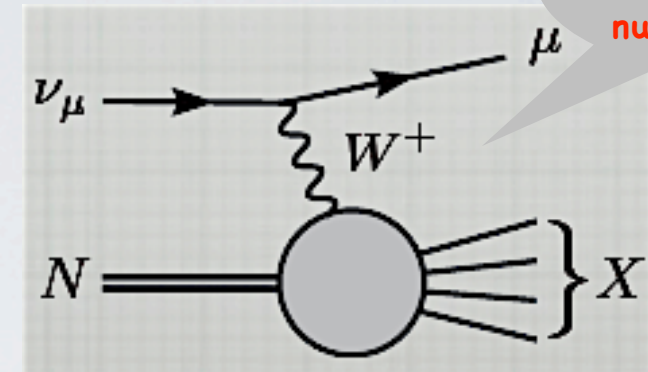
$$F_2^{\bar{\nu} A}(\mathbf{x}_N) \simeq \mathbf{x}_N [u^A + c^A + \bar{d}^A + \bar{s}^A](\mathbf{x}_N)$$

$$F_3^{\nu A}(\mathbf{x}_N) \simeq [-(\bar{u}^A + \bar{c}^A) + d^A + s^A](\mathbf{x}_N)$$

$$F_3^{\bar{\nu} A}(\mathbf{x}_N) \simeq [u^A + c^A - (\bar{d}^A + \bar{s}^A)](\mathbf{x}_N)$$

- experiments extract (under certain assumptions)

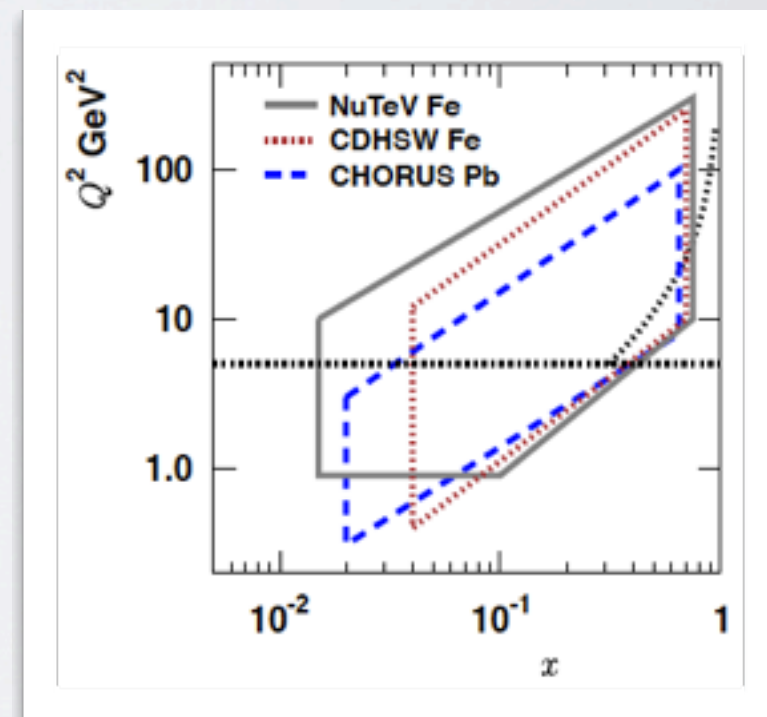
$$\mathbf{F}_{2,3} \equiv (\mathbf{F}_{2,3}^{\nu A} + \mathbf{F}_{2,3}^{\bar{\nu} A})/2 \rightarrow \begin{cases} \bullet F_2 \text{ probes total quark singlet} \\ \bullet F_3 \text{ probes sum of valence PDFs} \end{cases}$$



does a W interact differently with nuclear matter?

$$\frac{d^2 \sigma^{\nu A, \bar{\nu} A}}{dx dy} \simeq xy^2 F_1^{\nu A, \bar{\nu} A} + (1-y) F_2^{\nu A, \bar{\nu} A} \pm xy(1 - \frac{y}{2}) F_3^{\nu A, \bar{\nu} A}$$

potential tension
with what we have
learned from NC DIS

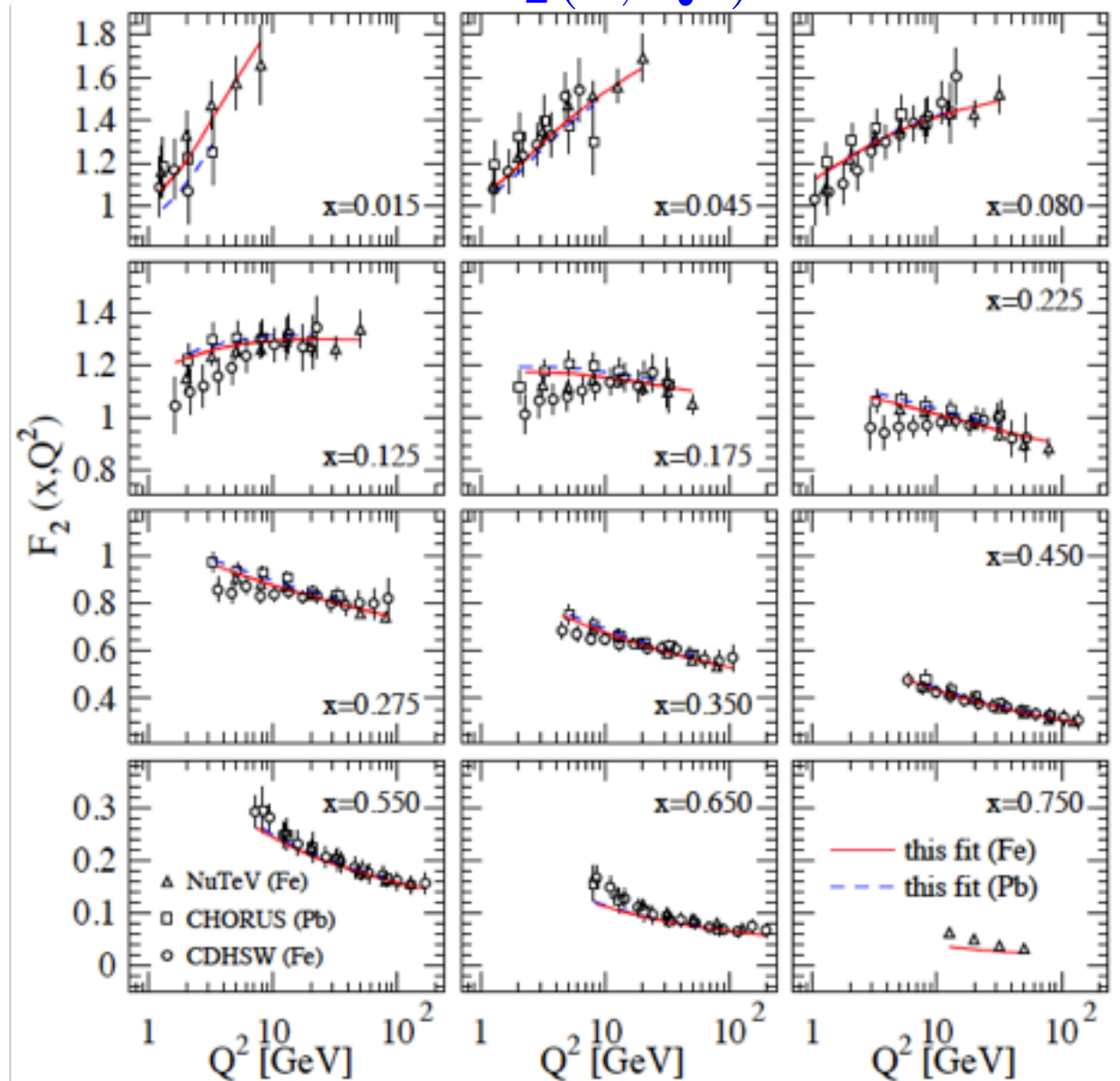


kinematics overlaps with
charged lepton DIS data

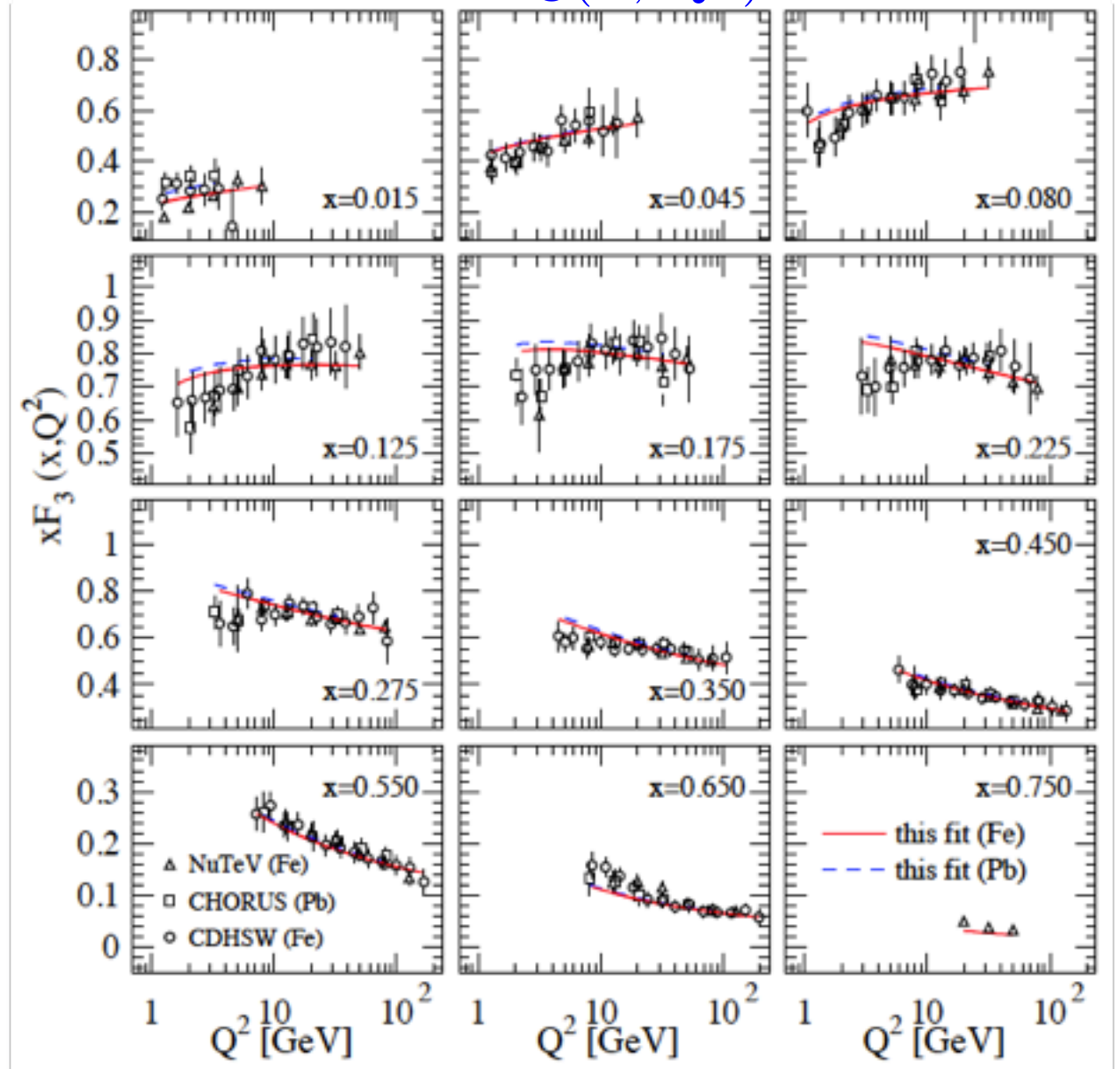
CC neutrino DIS data (cont'd)

find: data remarkably well reproduced by fit $\chi^2 = 488.2/532\text{pts.}$

$F_2(x, Q^2)$



$xF_3(x, Q^2)$

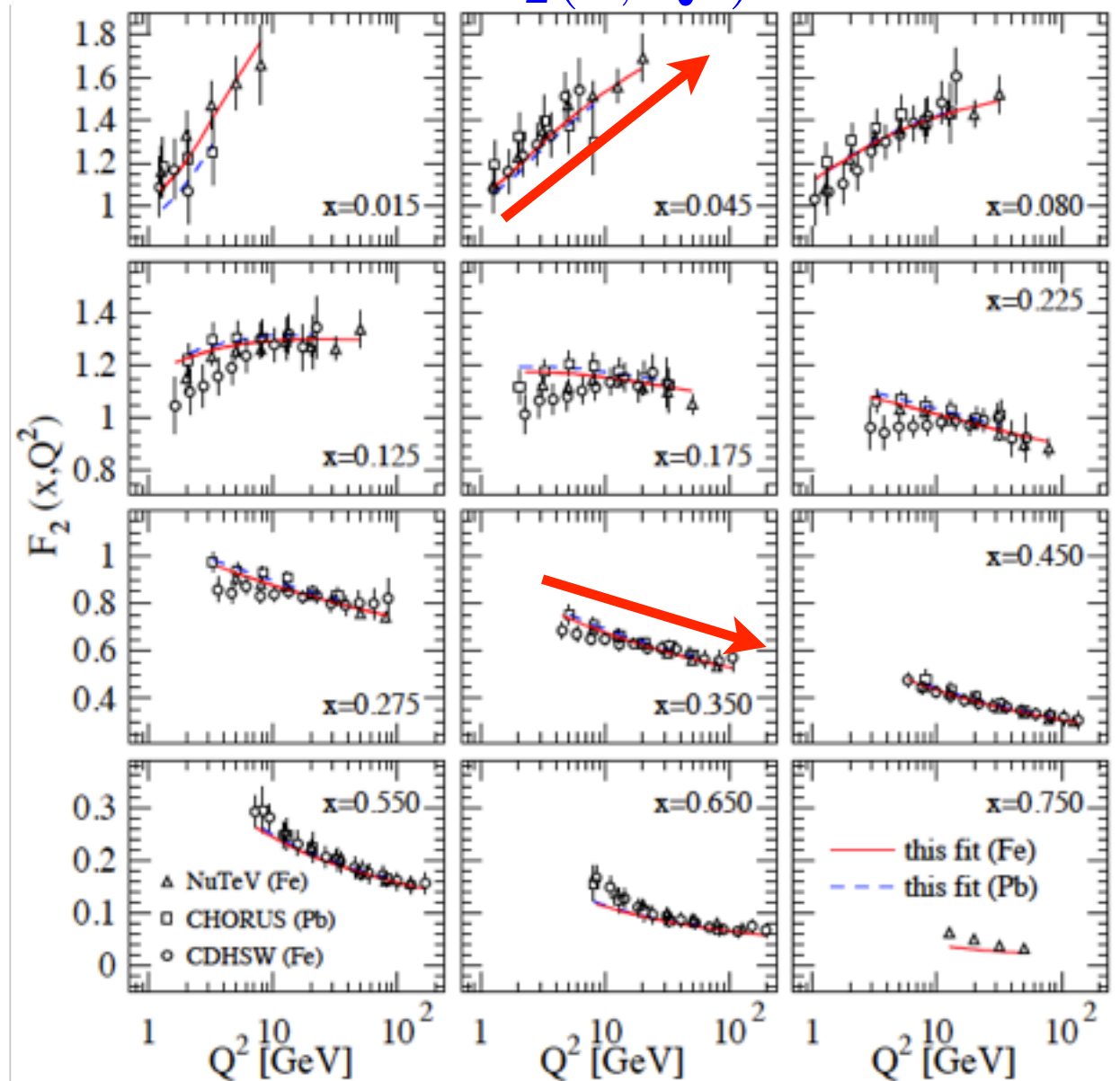


► absolute cross sections rather than ratios -> more sensitive to set of proton PDF in R_i^A (incl. as theor. uncertainty)

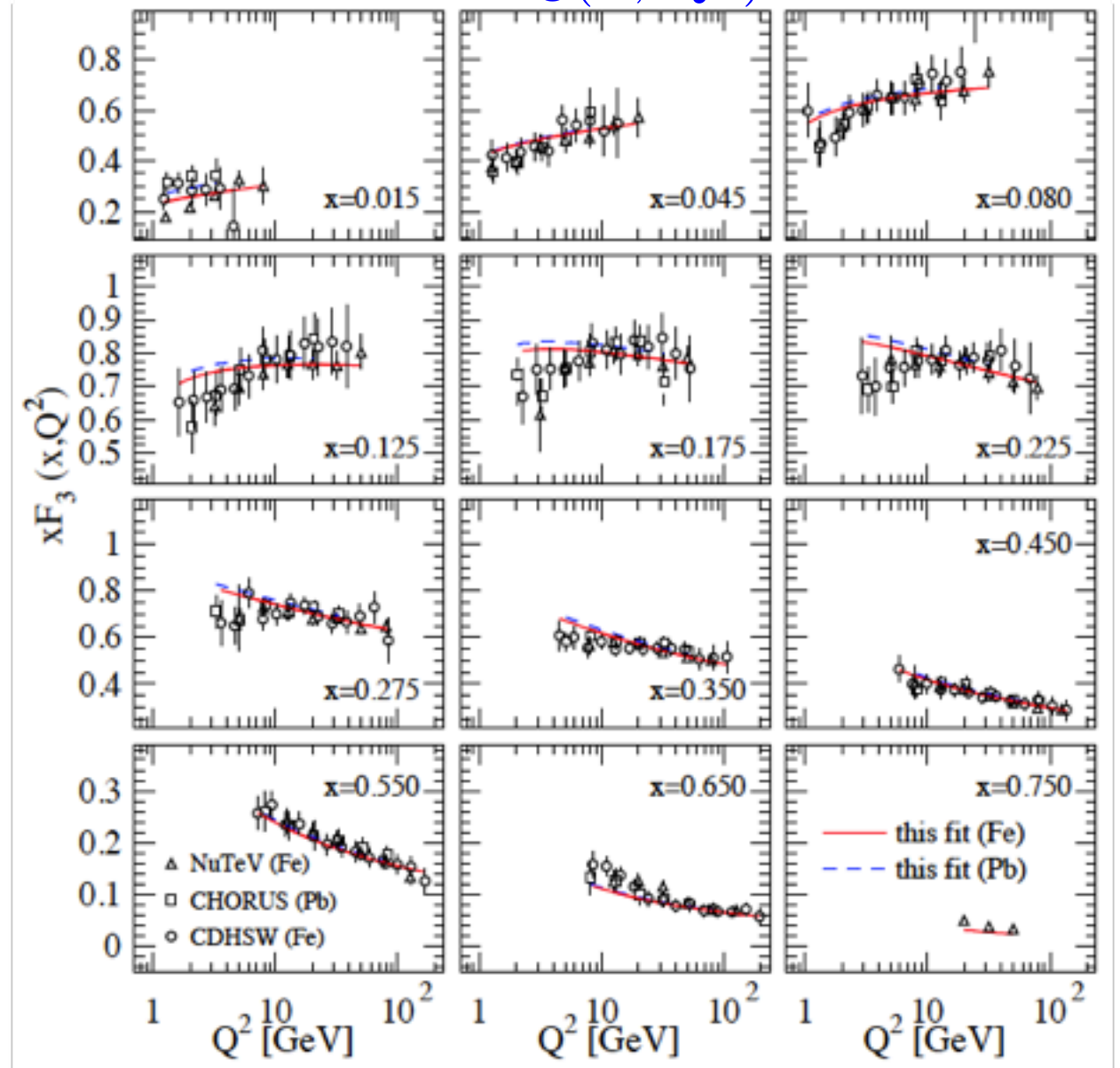
CC neutrino DIS data (cont'd)

find: data remarkably well reproduced by fit $\chi^2 = 488.2/532\text{pts.}$

$F_2(x, Q^2)$



$xF_3(x, Q^2)$

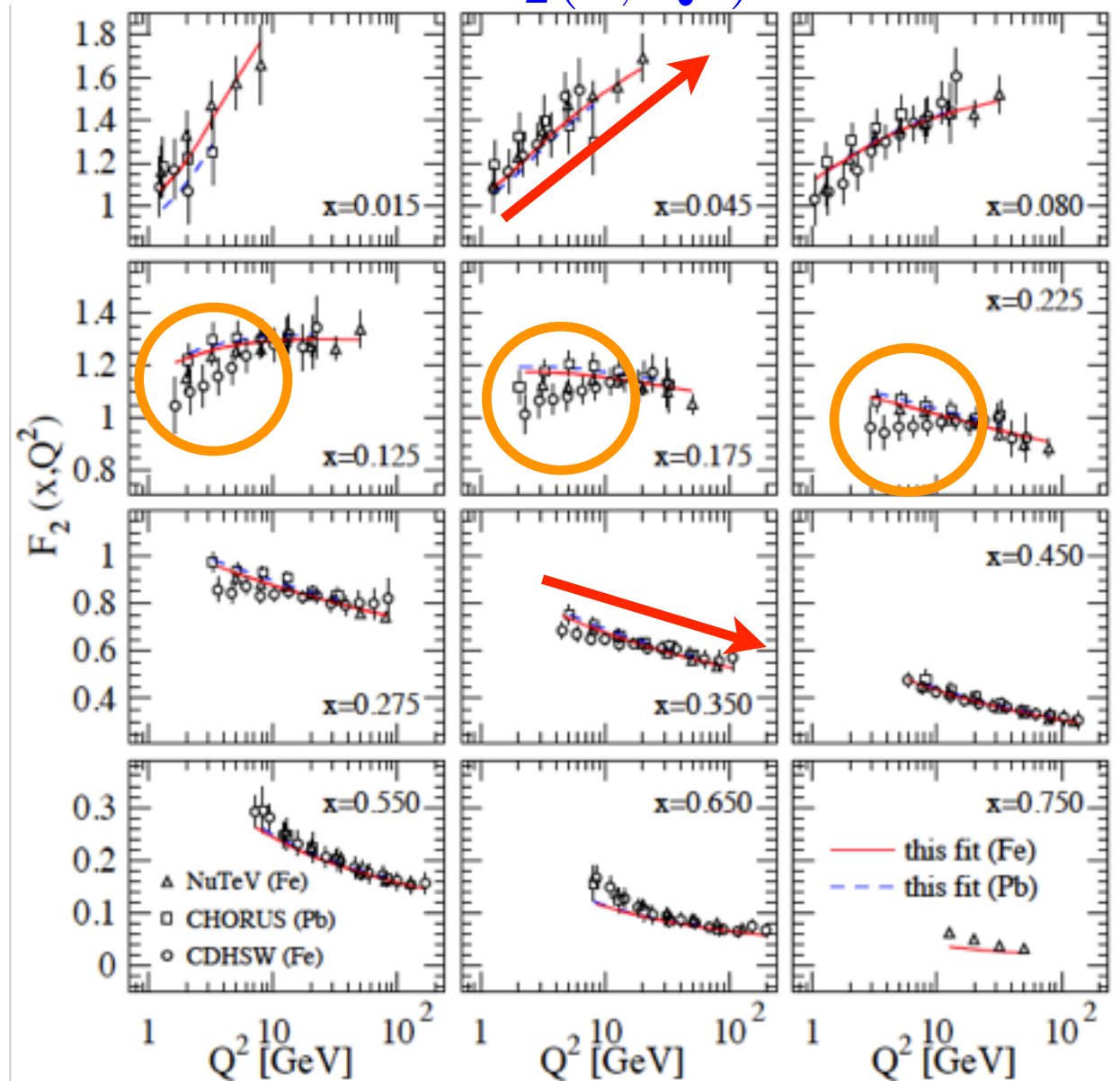


- ▶ absolute cross sections rather than ratios -> more sensitive to set of proton PDF in R_i^A (incl. as theor. uncertainty)
- ▶ data feature typical pattern of scaling violations

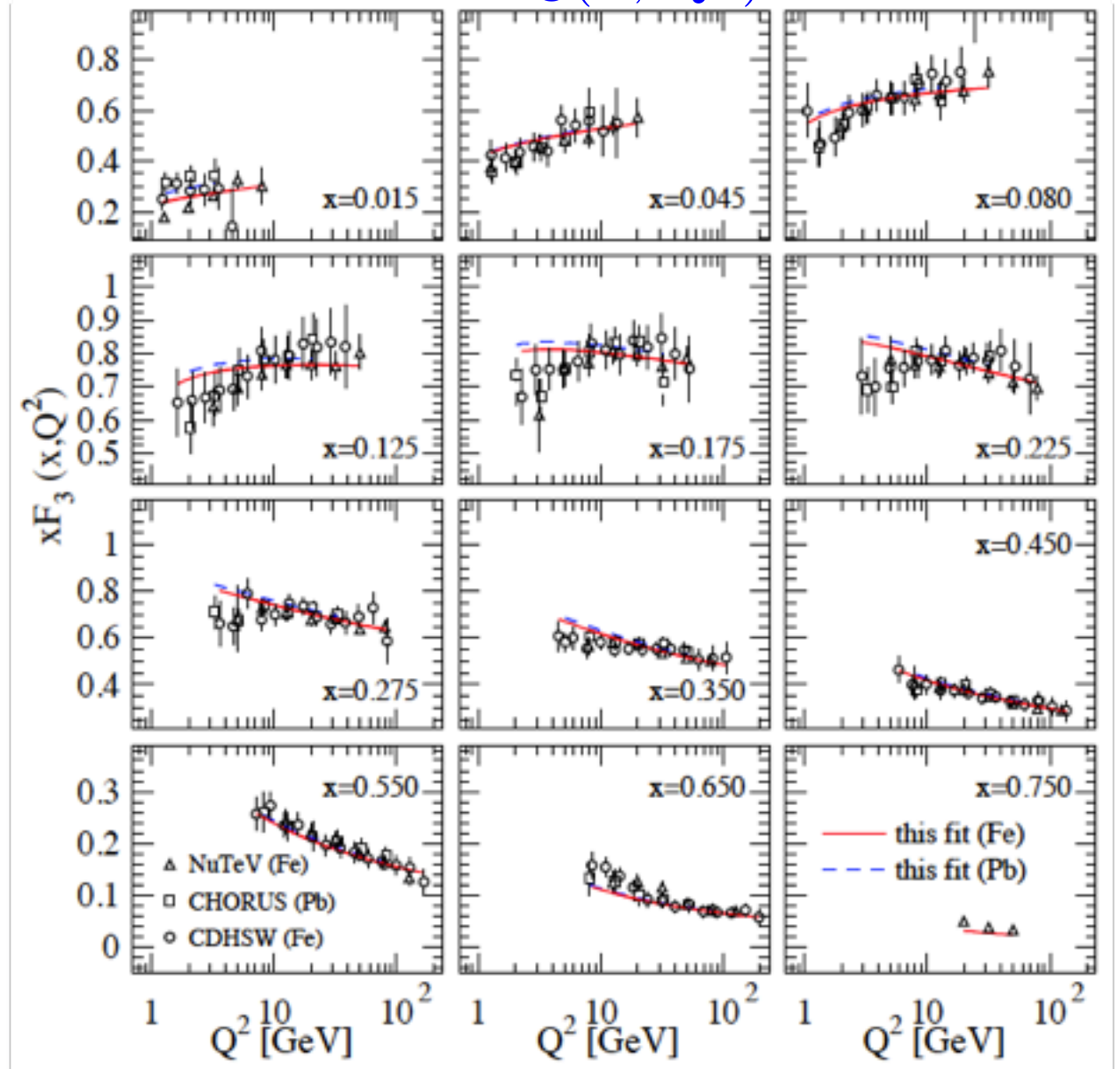
CC neutrino DIS data (cont'd)

find: data remarkably well reproduced by fit $\chi^2 = 488.2/532\text{pts.}$

$F_2(x, Q^2)$



$xF_3(x, Q^2)$

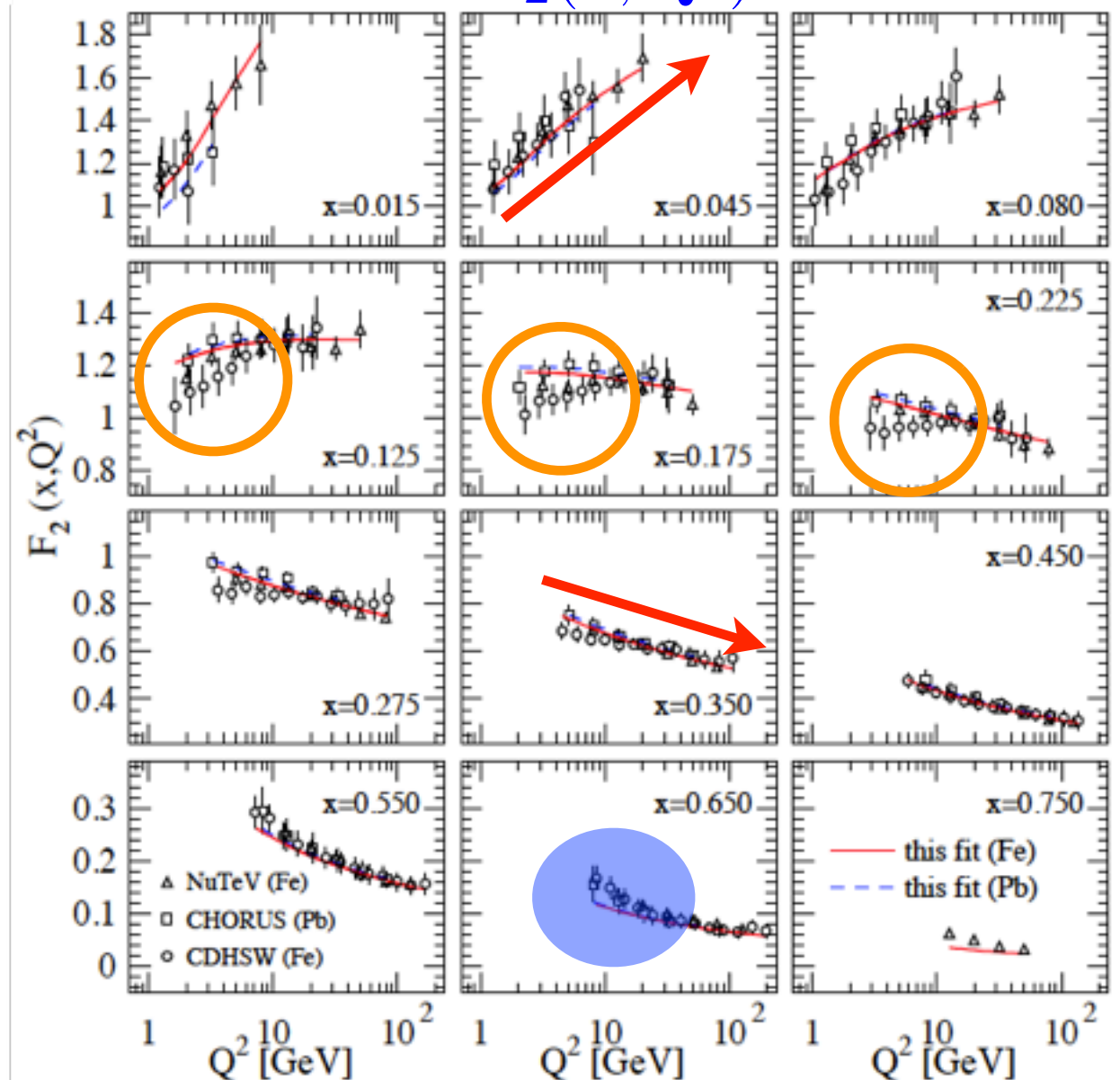


- ▶ absolute cross sections rather than ratios -> more sensitive to set of proton PDF in R_i^A (incl. as theor. uncertainty)
- ▶ data feature typical pattern of scaling violations
- ▶ slope of CDHSW data does not match with other data

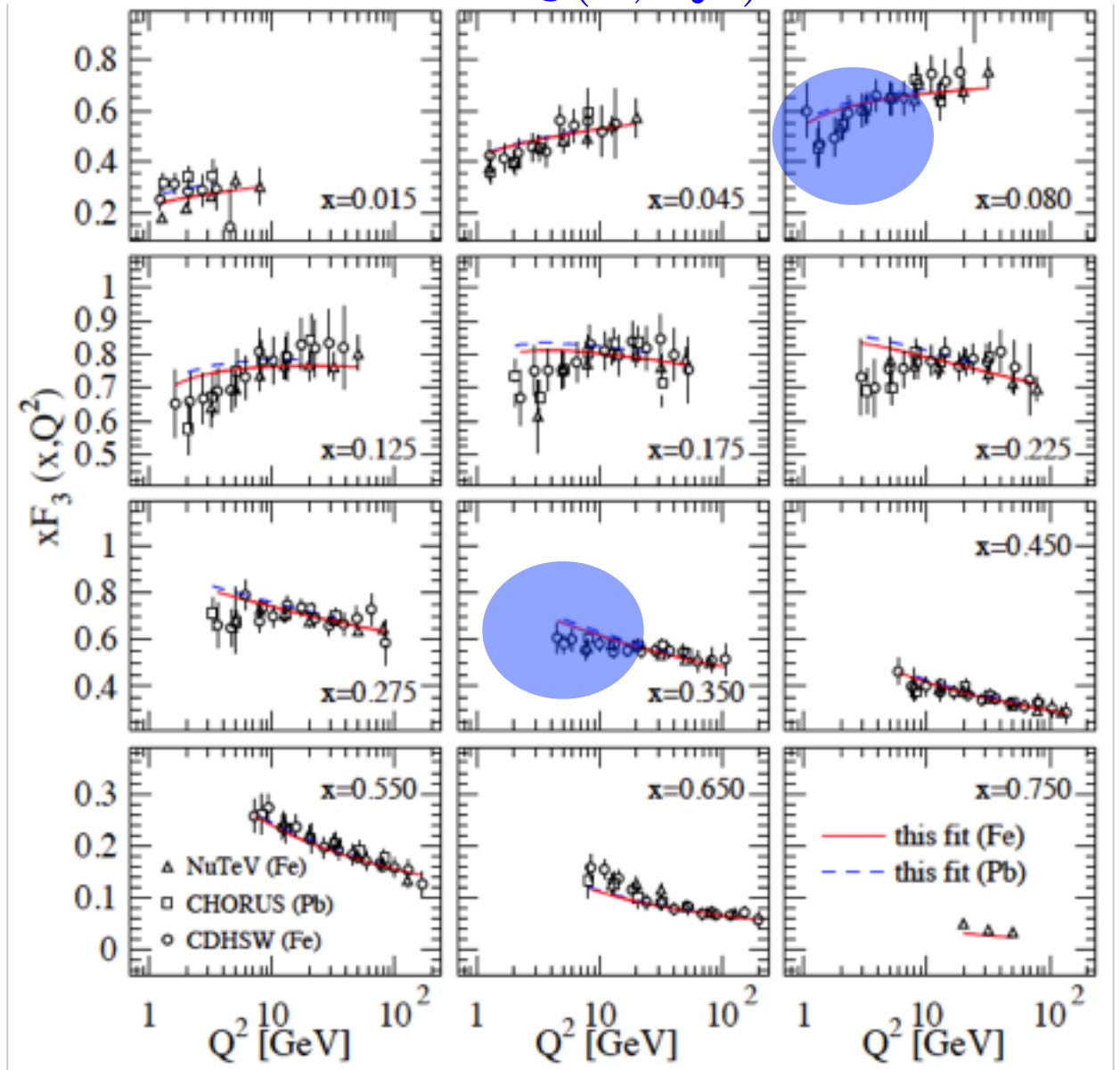
CC neutrino DIS data (cont'd)

find: data remarkably well reproduced by fit $\chi^2 = 488.2/532\text{pts.}$

$F_2(x, Q^2)$



$xF_3(x, Q^2)$



- ▶ absolute cross sections rather than ratios -> more sensitive to set of proton PDF in R_i^A (incl. as theor. uncertainty)
- ▶ data feature typical pattern of scaling violations
- ▶ slope of CDHSW data does not match with other data

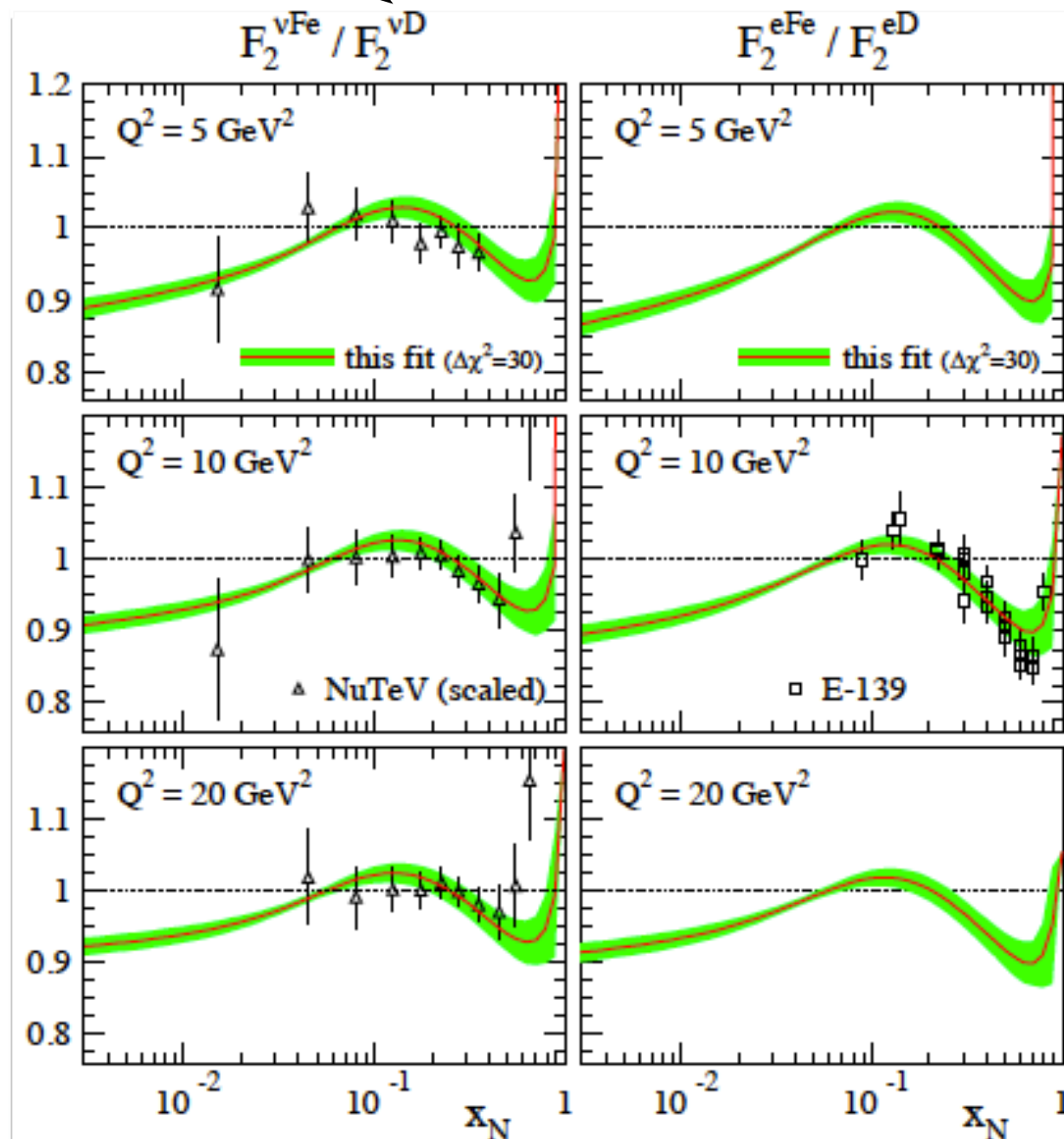
some mild tensions

often with CDHSW data

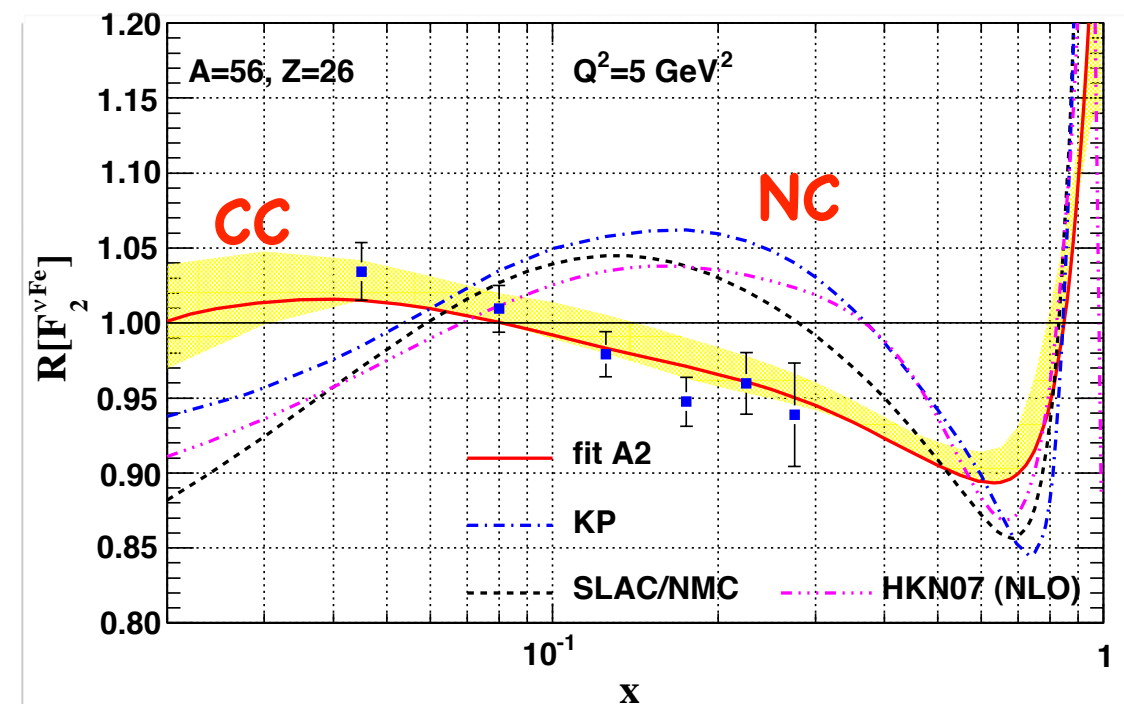
CC neutrino DIS data (cont'd)

no indication for factorization breaking

find same pattern of nuclear effects for CC and NC DIS



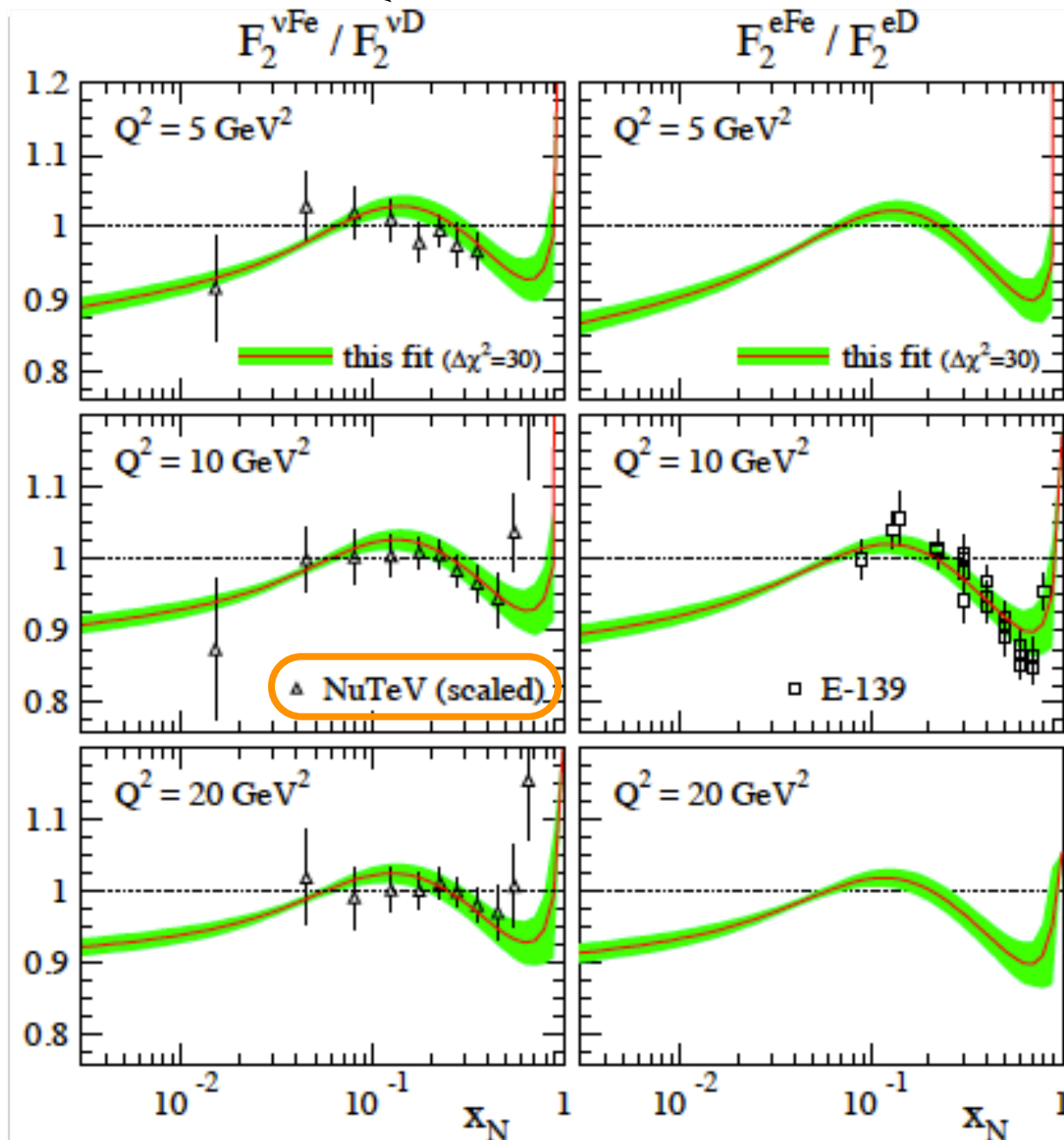
at variance with nCTEQ result



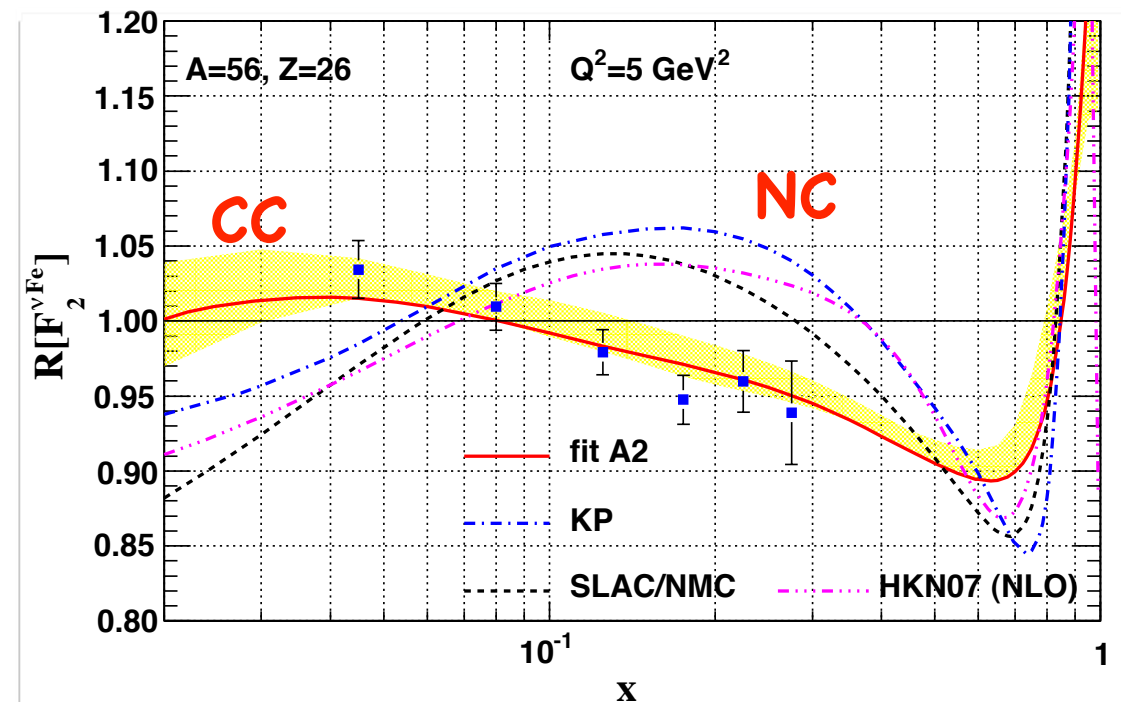
CC neutrino DIS data (cont'd)

no indication for factorization breaking

find same pattern of nuclear effects for CC and NC DIS



at variance with nCTEQ result

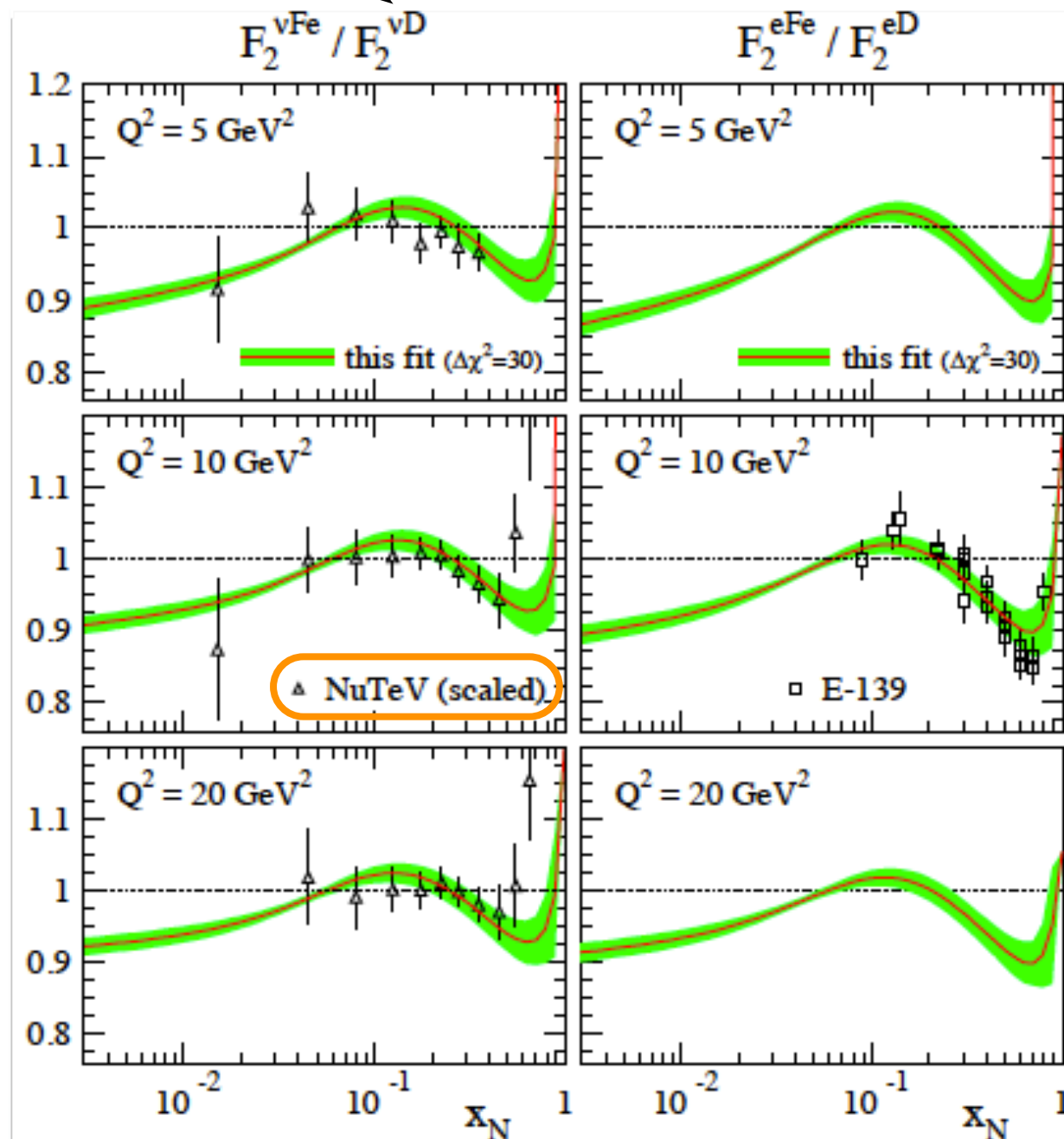


► “theoretical data”: $F_2^{\nu D}$ not measured

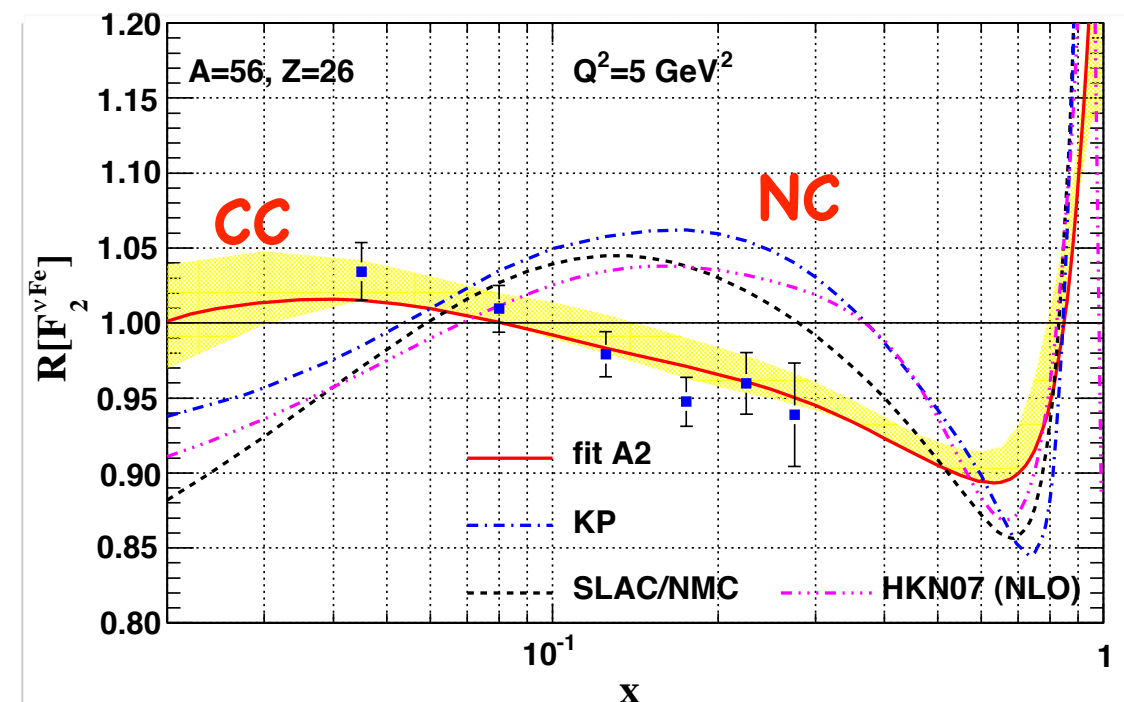
CC neutrino DIS data (cont'd)

no indication for factorization breaking

find same pattern of nuclear effects for CC and NC DIS



at variance with nCTEQ result

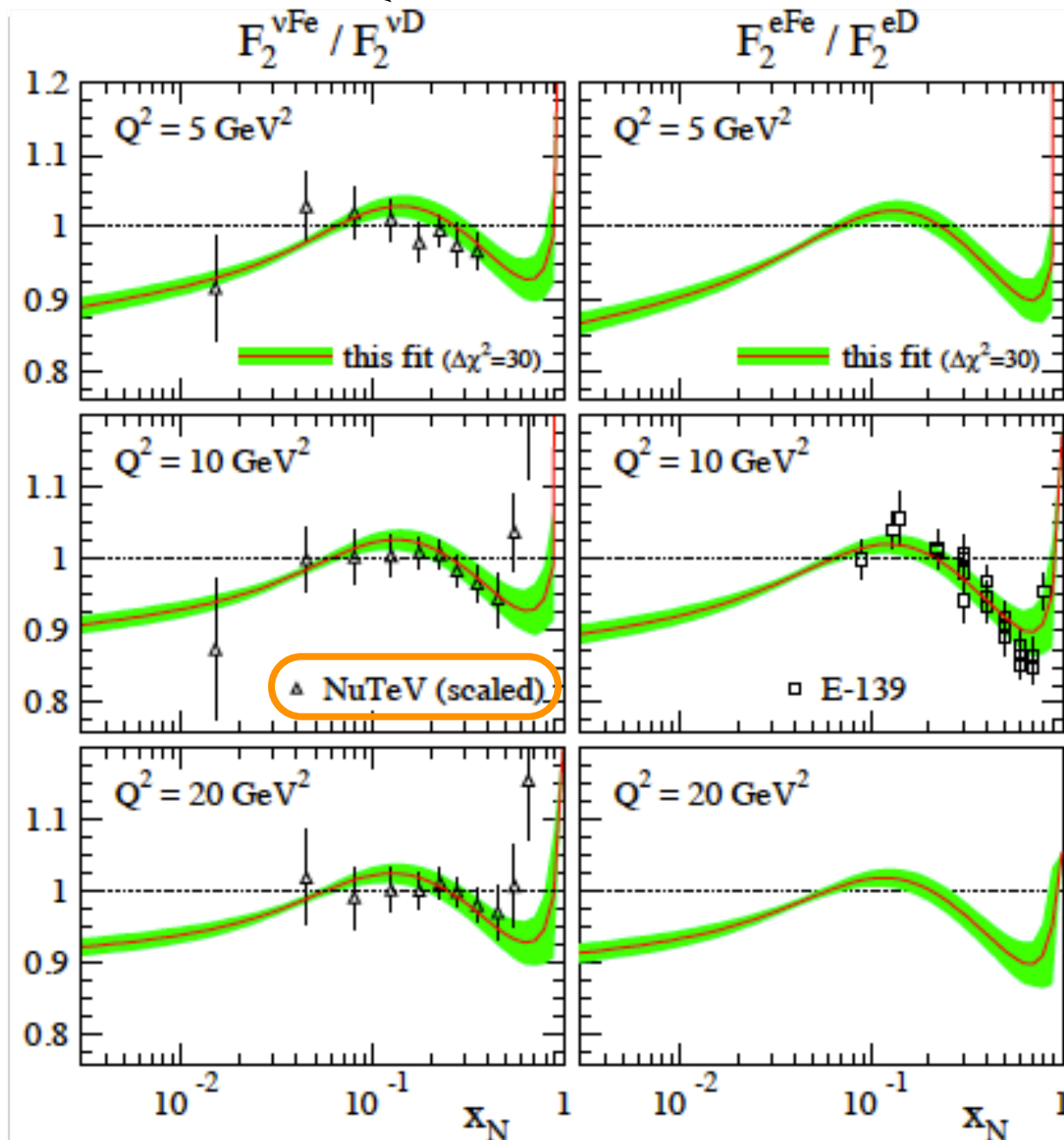


- ▶ “theoretical data”: $F_2^{\nu D}$ not measured
- ▶ nCTEQ fits to cross sections not str. fcts.

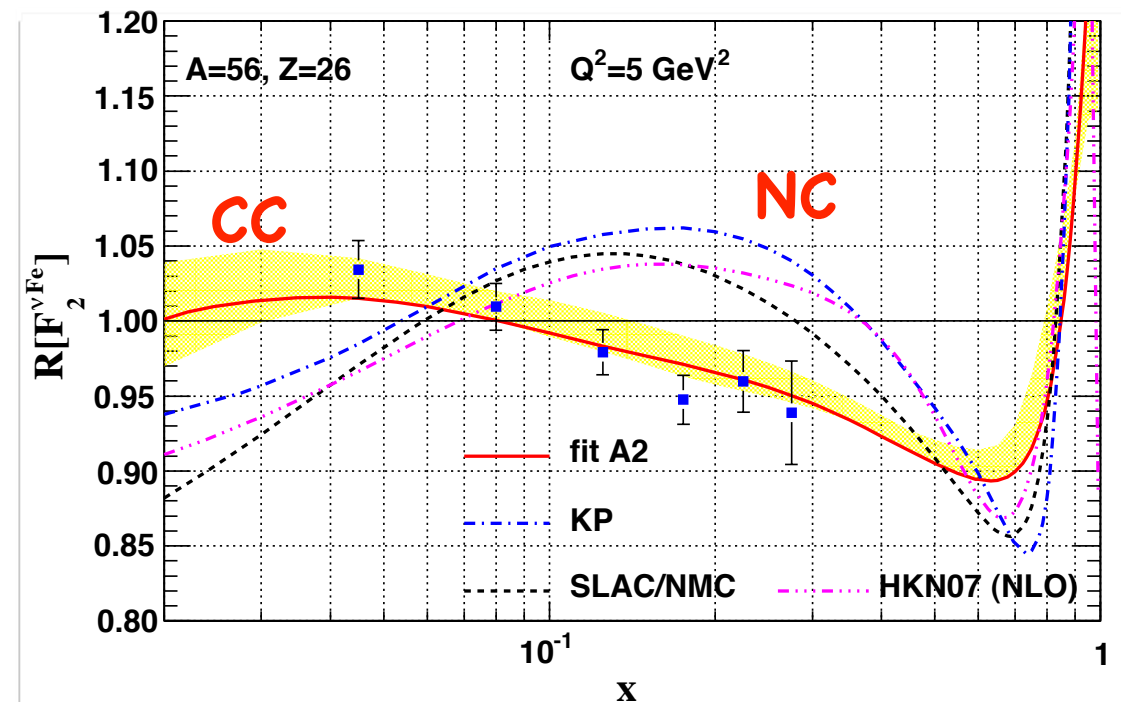
CC neutrino DIS data (cont'd)

no indication for factorization breaking

find same pattern of nuclear effects for CC and NC DIS



at variance with nCTEQ result



- ▶ “theoretical data”: $F_2^{\nu D}$ not measured
- ▶ nCTEQ fits to cross sections not str. fcts.
- ▶ also EPS finds compatible nuclear effects (no re-fit including CC DIS yet)

pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

wanted

pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

free proton PDF
"known"

wanted

known to NLO
[plus certain all-order resummations]
many contributing subprocesses

fragmentation functions
fairly well known for pions
but what about possible nuclear modifications?
can have an impact even if small

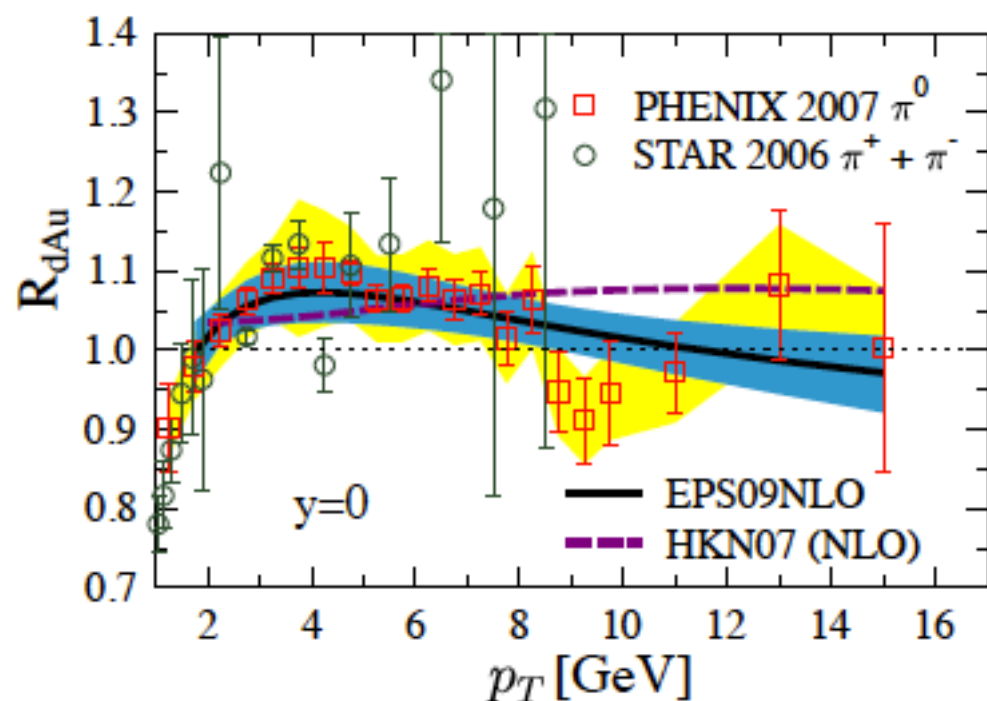
pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

f_i^d : free proton PDF "known"
 f_j^A : **wanted**
 $d\hat{\sigma}_{ij \rightarrow kX}$: known to NLO [plus certain all-order resummations] many contributing subprocesses
 $D_k^{A,\pi}$: fragmentation functions fairly well known for pions **but what about possible nuclear modifications?** can have an impact even if small

mid-rapidity neutral pion data from PHENIX and STAR first analyzed in EPS fit



- fit to min. bias ratio $R_{dAu}^\pi = \frac{\frac{1}{2A} d^2\sigma_{dAu}/dp_T dy}{d^2\sigma_{pp}/dp_T dy}$
- use up-to-date vacuum fragmentation functions
DSS: de Florian, Sassot, MS - include RHIC pp data

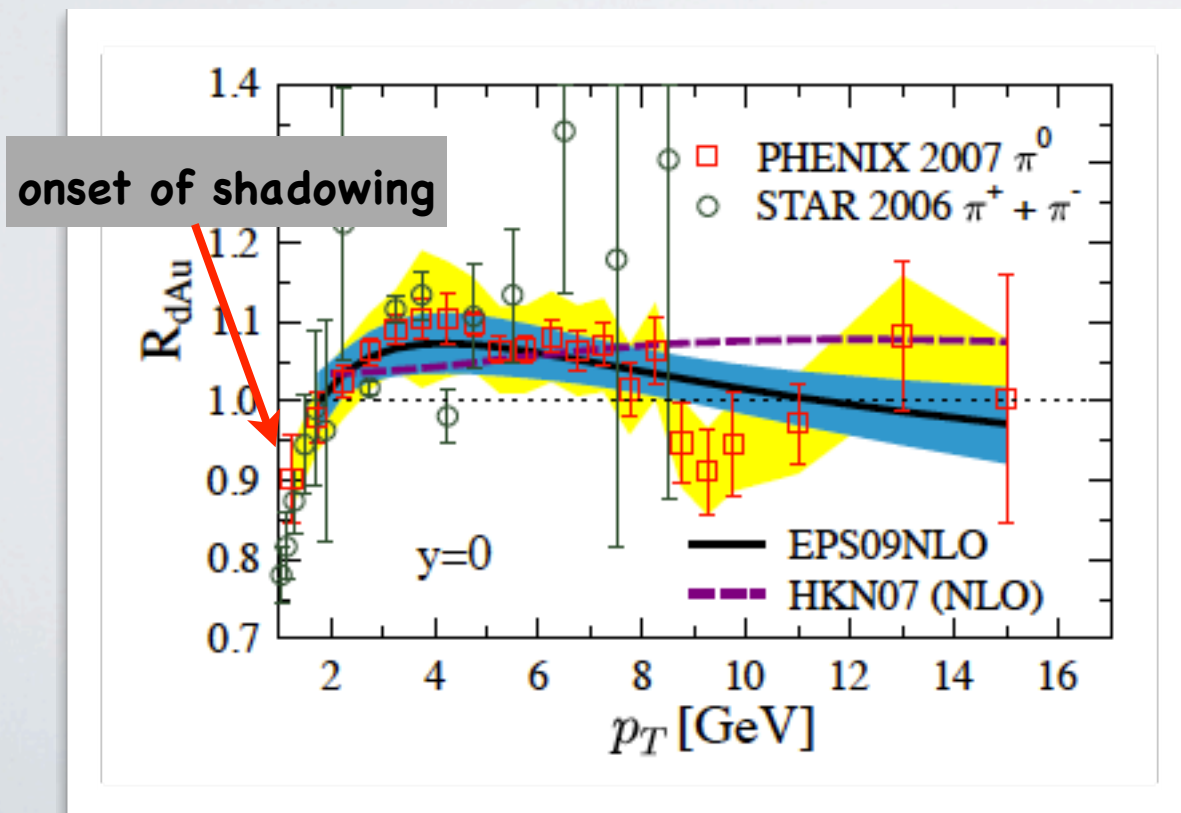
pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

free proton PDF "known"
 wanted
 known to NLO [plus certain all-order resummations] many contributing subprocesses
 fragmentation functions fairly well known for pions
 but what about possible nuclear modifications? can have an impact even if small

mid-rapidity neutral pion data from PHENIX and STAR first analyzed in EPS fit



- fit to min. bias ratio $R_{dAu}^\pi = \frac{\frac{1}{2A} d^2\sigma_{dAu}/dp_T dy}{d^2\sigma_{pp}/dp_T/dy}$
- use up-to-date vacuum fragmentation functions
DSS: de Florian, Sassot, MS - include RHIC pp data
- find BIG impact on gluon nPDF

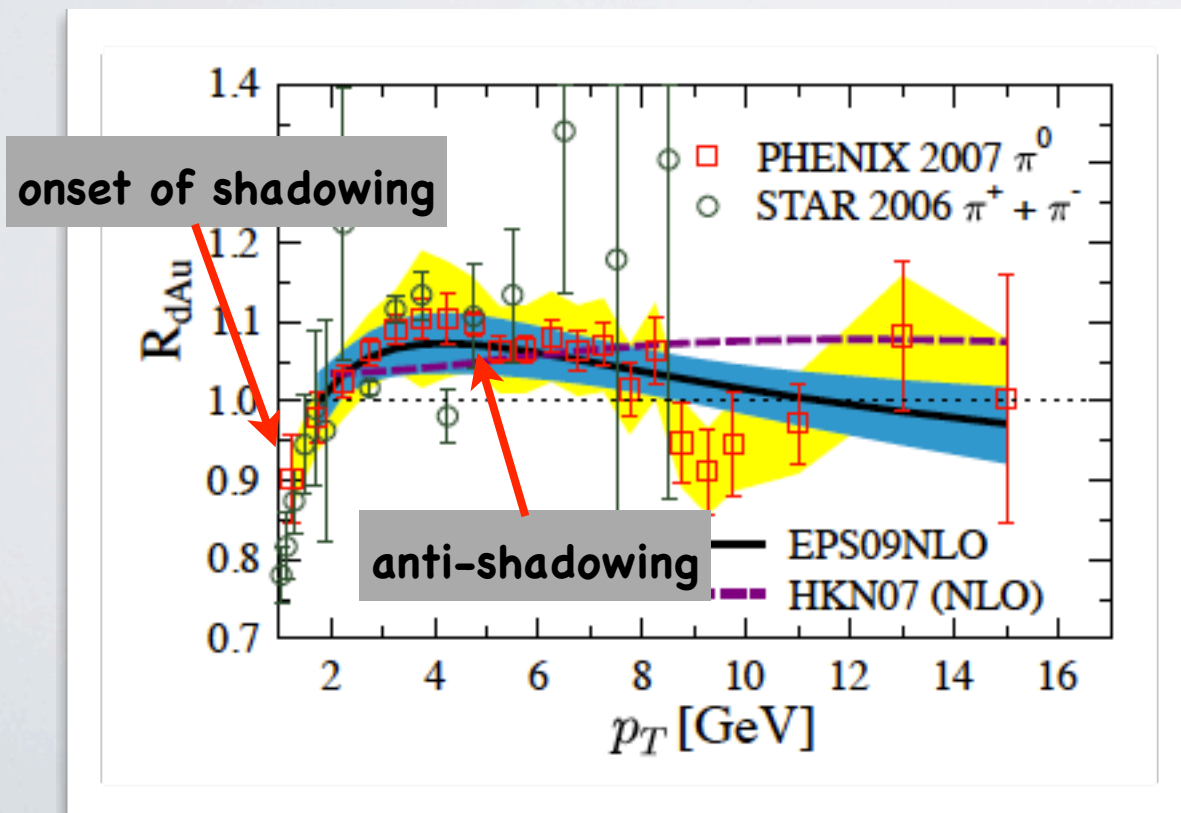
pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

f_i^d : free proton PDF "known"
 f_j^A : **wanted**
 $d\hat{\sigma}_{ij \rightarrow kX}$: known to NLO [plus certain all-order resummations] many contributing subprocesses
 $D_k^{A,\pi}$: fragmentation functions fairly well known for pions **but what about possible nuclear modifications?** can have an impact even if small

mid-rapidity neutral pion data from PHENIX and STAR first analyzed in EPS fit



- fit to min. bias ratio $R_{dAu}^\pi = \frac{\frac{1}{2A} d^2\sigma_{dAu}/dp_T dy}{d^2\sigma_{pp}/dp_T dy}$
- use up-to-date vacuum fragmentation functions
DSS: de Florian, Sassot, MS - include RHIC pp data
- find BIG impact on gluon nPDF

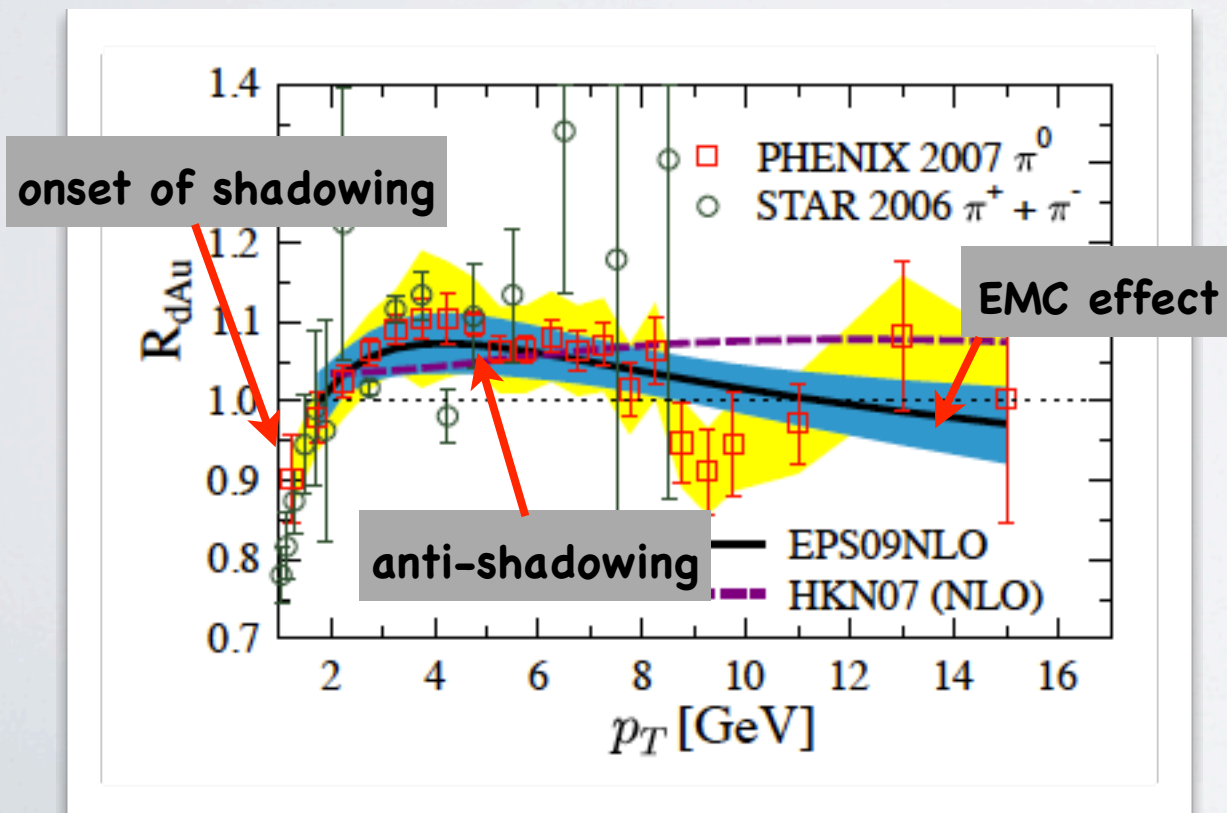
pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

f_i^d : free proton PDF "known"
 f_j^A : **wanted**
 $d\hat{\sigma}_{ij \rightarrow kX}$: known to NLO [plus certain all-order resummations] many contributing subprocesses
 $D_k^{A,\pi}$: fragmentation functions fairly well known for pions **but what about possible nuclear modifications?** can have an impact even if small

mid-rapidity neutral pion data from PHENIX and STAR first analyzed in EPS fit



- fit to min. bias ratio $R_{dAu}^{\pi} = \frac{\frac{1}{2A} d^2\sigma_{dAu}/dp_T dy}{d^2\sigma_{pp}/dp_T dy}$
- use up-to-date vacuum fragmentation functions
DSS: de Florian, Sassot, MS - include RHIC pp data
- find BIG impact on gluon nPDF

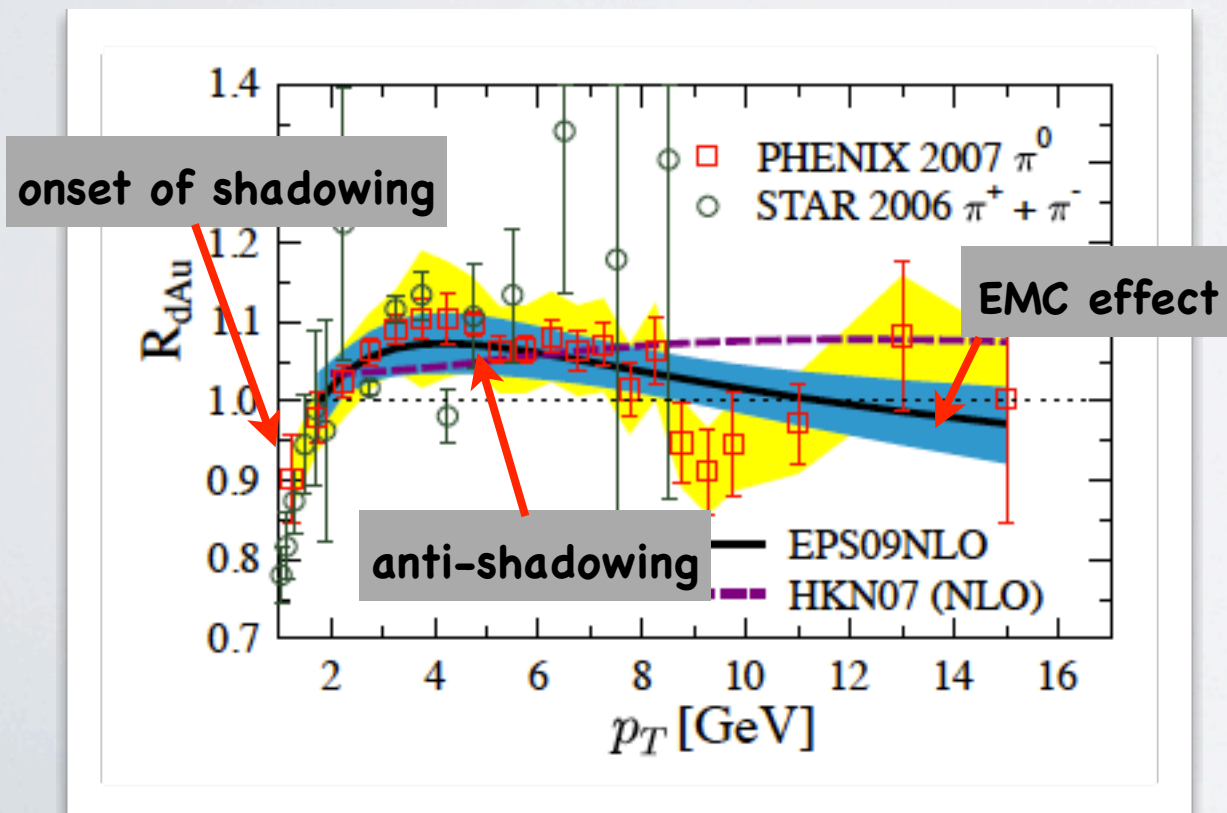
pion production in dA

most difficult probe to analyze (yet, perhaps one of the most interesting ones)

$$d\sigma_{dA \rightarrow \pi X}^A = \sum_{ijk} f_i^d \otimes f_j^A \otimes d\hat{\sigma}_{ij \rightarrow kX} \otimes D_k^{A,\pi}$$

f_i^d : free proton PDF "known"
 f_j^A : **wanted**
 $d\hat{\sigma}_{ij \rightarrow kX}$: known to NLO [plus certain all-order resummations] many contributing subprocesses
 $D_k^{A,\pi}$: fragmentation functions fairly well known for pions **but what about possible nuclear modifications?** can have an impact even if small

mid-rapidity neutral pion data from PHENIX and STAR first analyzed in EPS fit



- fit to min. bias ratio $R_{dAu}^\pi = \frac{\frac{1}{2A} d^2\sigma_{dAu}/dp_T dy}{d^2\sigma_{pp}/dp_T dy}$
- use up-to-date vacuum fragmentation functions
DSS: de Florian, Sassot, MS - include RHIC pp data
- find BIG impact on gluon nPDF

potential caveat: need to assign large weight to dAu data in fit

pion production in dA – cont'd

what is different in DSSZ analysis

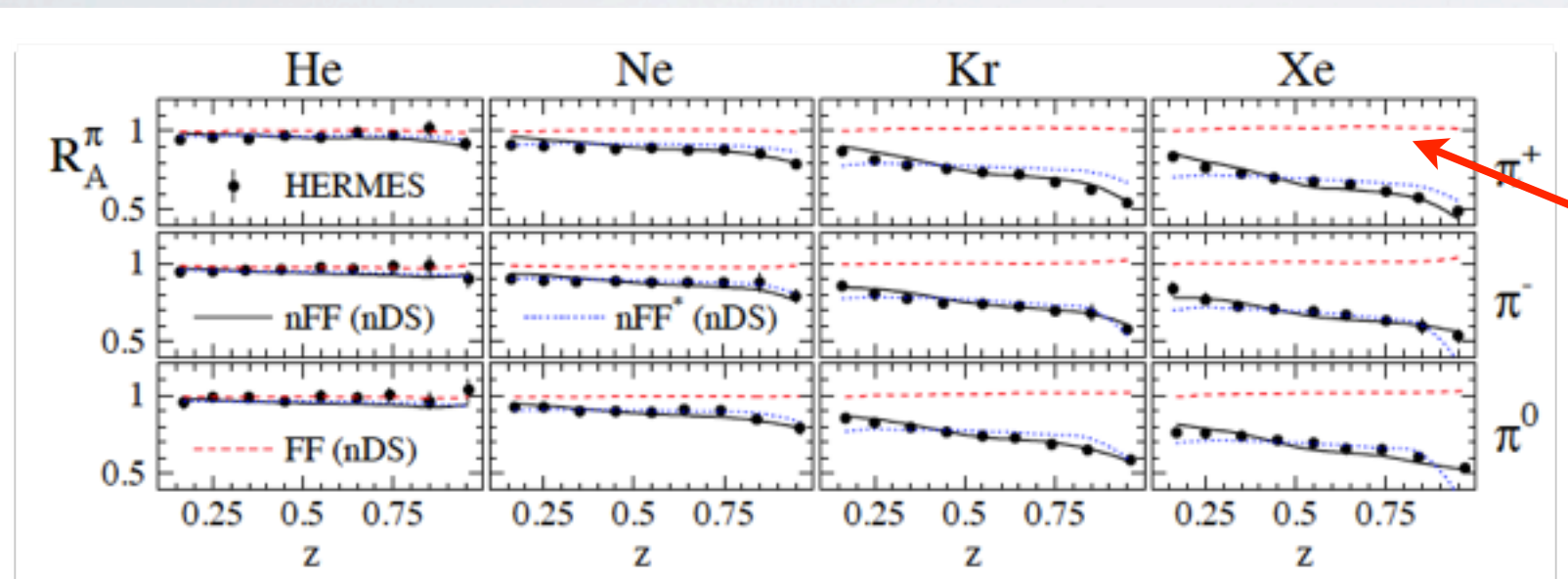
- ✓ more data, including also charged pions from STAR
- ✓ no artificially large weight w.r.t. other data sets
- ✓ try to estimate impact of modifications in hadronization

pion production in dA – cont'd

what is different in DSSZ analysis

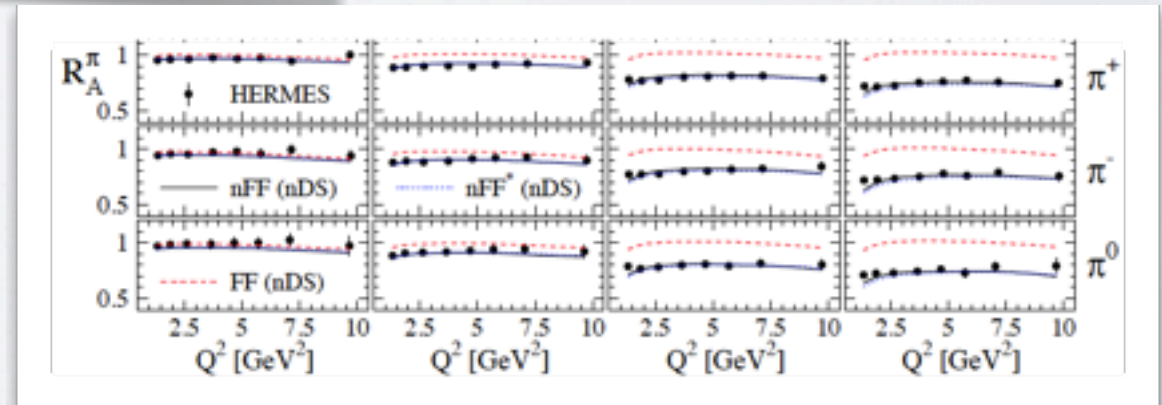
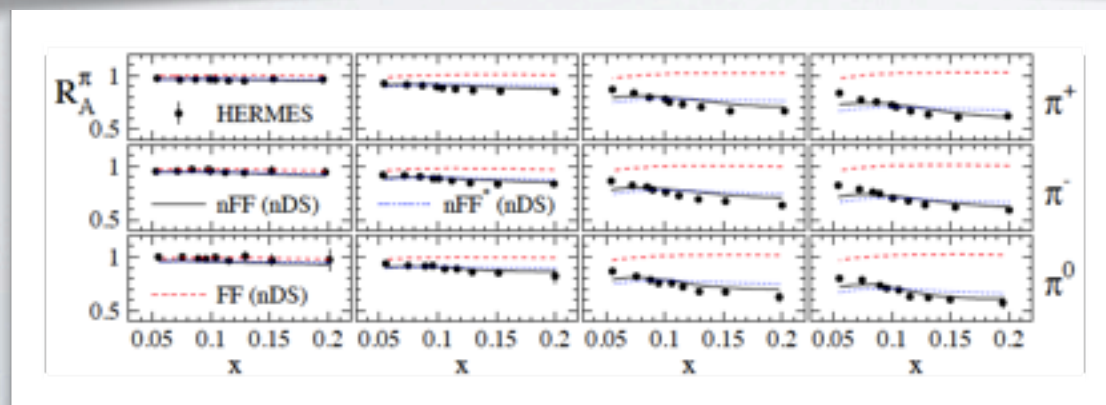
- ✓ more data, including also charged pions from STAR
- ✓ no artificially large weight w.r.t. other data sets
- ✓ try to estimate impact of modifications in hadronization

fragmentation in a medium – what is known ?



- effects known to be large in eA
- cannot be described as an initial-state effect (= nPDFs)
- hadron attenuation increases with A and z (rather flat in x and Q^2)

HERMES



medium modified fragmentation

how to model fragmentation in a medium ?

medium modified fragmentation

how to model fragmentation in a medium ?

bold attempt: extend FFs to medium modified FFs ("in the background of a nucleus A") Sassot, MS, Zurita 0912.1311

choose convolution ansatz to modify vacuum FFs

$$D_{i/A}^H(z, Q_0) = \int_z^1 \frac{dy}{y} W_i(y, A) D_i^H\left(\frac{z}{y}, Q_0\right)$$

DSS vacuum FFs

from fit to HERMES and RHIC dAu pion data

medium modified fragmentation

how to model fragmentation in a medium ?

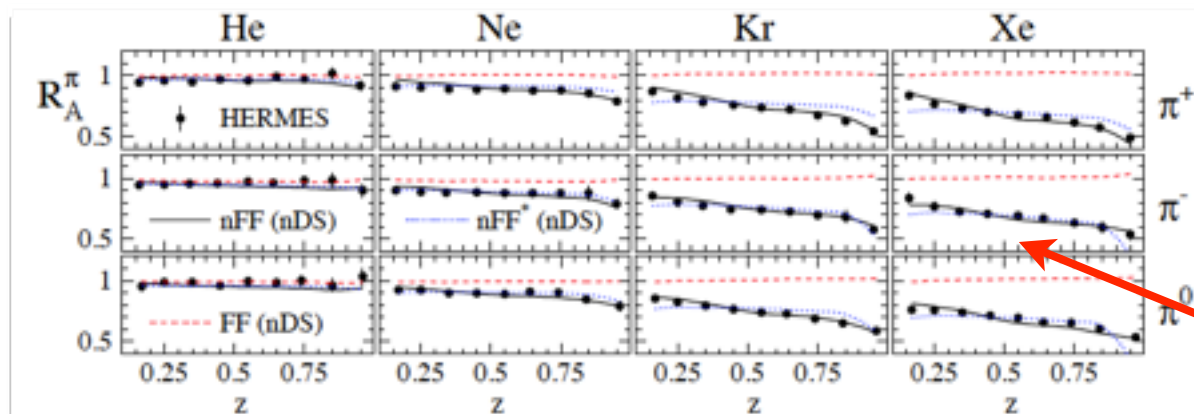
bold attempt: extend FFs to medium modified FFs ("in the background of a nucleus A") Sassot, MS, Zurita 0912.1311

choose convolution ansatz to modify vacuum FFs

$$D_{i/A}^H(z, Q_0) = \int_z^1 \frac{dy}{y} W_i(y, A) D_i^H\left(\frac{z}{y}, Q_0\right)$$

DSS vacuum FFs

from fit to HERMES and RHIC dAu pion data



works well

Experiment	A	H	Data type	Data points	χ^2
HERMES [6]	He,Ne,Kr,Xe	π^+	z	36	39.3
		π^-	z	36	23.0
		π^0	z	36	27.4
		π^+	x	36	69.4
		π^-	x	36	55.4
		π^0	x	36	49.7
		π^+	Q^2	32	21.0
		π^-	Q^2	32	27.1
		π^0	Q^2	32	34.7
PHENIX [14]	Au	π^0	p_T	22	13.7
STAR (prel.) [16]	Au	π^0	p_T	13	12.8
STAR [15]	Au	π^\pm	p_T	24	22.5
Total				381	396.0

medium modified fragmentation

how to model fragmentation in a medium ?

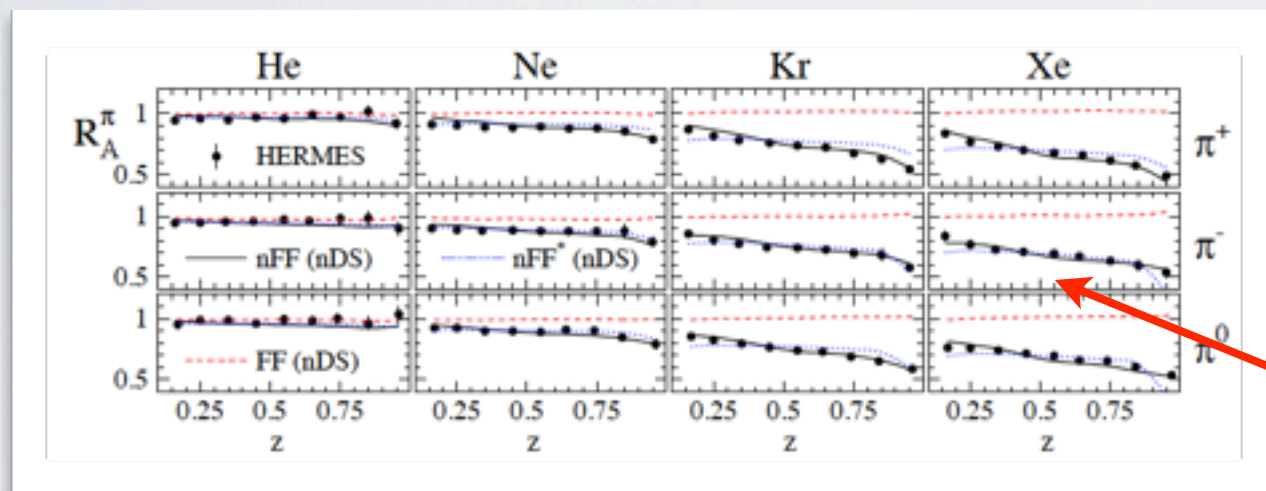
bold attempt: extend FFs to medium modified FFs ("in the background of a nucleus A") Sassot, MS, Zurita 0912.1311

choose convolution ansatz to modify vacuum FFs

$$D_{i/A}^H(z, Q_0) = \int_z^1 \frac{dy}{y} W_i(y, A) D_i^H\left(\frac{z}{y}, Q_0\right)$$

DSS vacuum FFs

from fit to HERMES and RHIC dAu pion data



works well

Experiment	A	H	Data type	Data points	χ^2
HERMES [6]	He,Ne,Kr,Xe	π^+	z	36	39.3
		π^-	z	36	23.0
		π^0	z	36	27.4
		π^+	x	36	69.4
		π^-	x	36	55.4
		π^0	x	36	49.7
		π^+	Q^2	32	21.0
		π^-	Q^2	32	27.1
		π^0	Q^2	32	34.7
PHENIX [14]	Au	π^0	p_T	22	13.7
STAR (prel.) [16]	Au	π^0	p_T	13	12.8
STAR [15]	Au	π^\pm	p_T	24	22.5
Total				381	396.0

find:

- ▶ suppressed quark \rightarrow pion fragmentation (incr. with A)
- ▶ mildly enhanced gluon fragmentation around $z=0.5$

medium modified fragmentation

how to model fragmentation in a medium ?

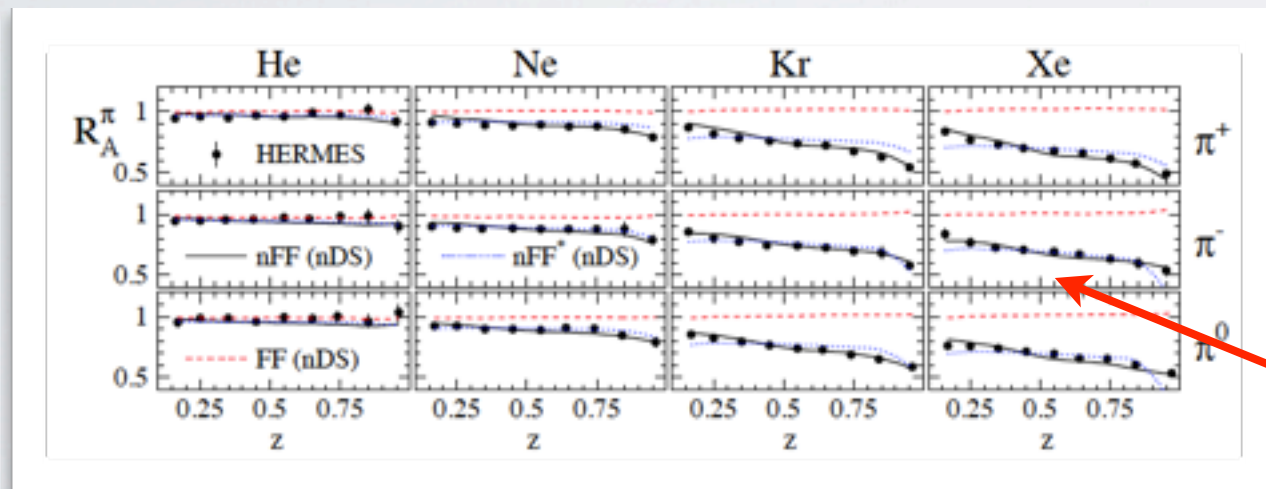
bold attempt: extend FFs to medium modified FFs ("in the background of a nucleus A") Sassot, MS, Zurita 0912.1311

choose convolution ansatz to modify vacuum FFs

$$D_{i/A}^H(z, Q_0) = \int_z^1 \frac{dy}{y} W_i(y, A) D_i^H\left(\frac{z}{y}, Q_0\right)$$

DSS vacuum FFs

from fit to HERMES and RHIC dAu pion data



works well

Experiment	A	H	Data type	Data points	χ^2
HERMES [6]	He,Ne,Kr,Xe	π^+	z	36	39.3
		π^-	z	36	23.0
		π^0	z	36	27.4
		π^+	x	36	69.4
		π^-	x	36	55.4
		π^0	x	36	49.7
		π^+	Q^2	32	21.0
		π^-	Q^2	32	27.1
		π^0	Q^2	32	34.7
		π^\pm	Q^2	32	22.5
PHENIX [14]	Au	π^0	p_T	22	13.7
STAR (prel.) [16]	Au	π^0	p_T	13	12.8
STAR [15]	Au	π^\pm	p_T	24	22.5
Total				381	396.0

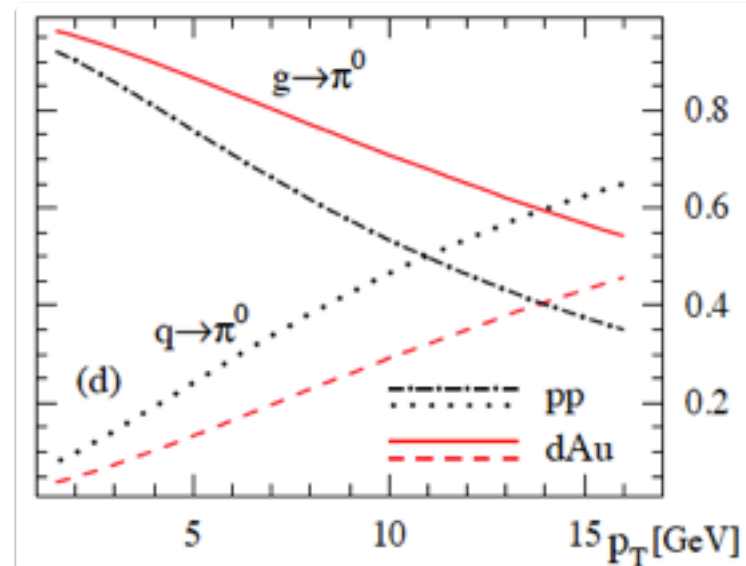
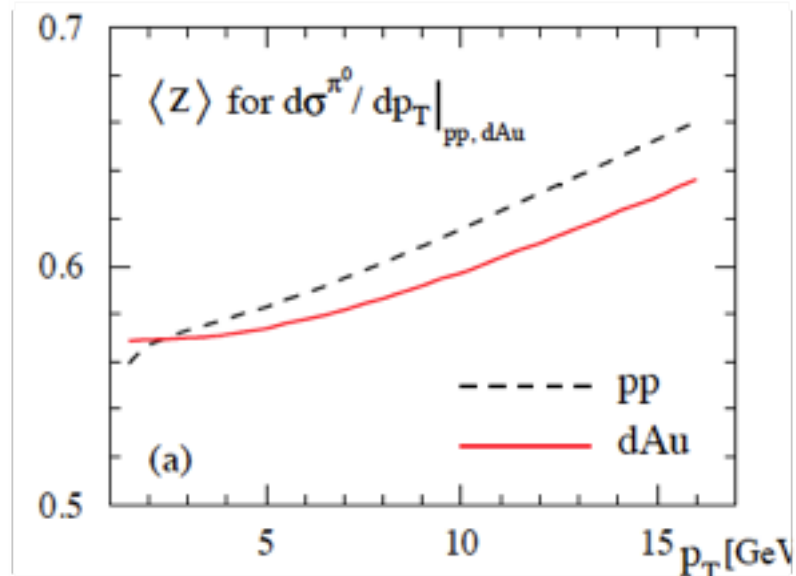
find:

- ▶ suppressed quark \rightarrow pion fragmentation (incr. with A)
- ▶ mildly enhanced gluon fragmentation around $z=0.5$

use both DSS vacuum and effective nuclear FFs in DSSZ nPDF analysis

more on mid rapidity pions

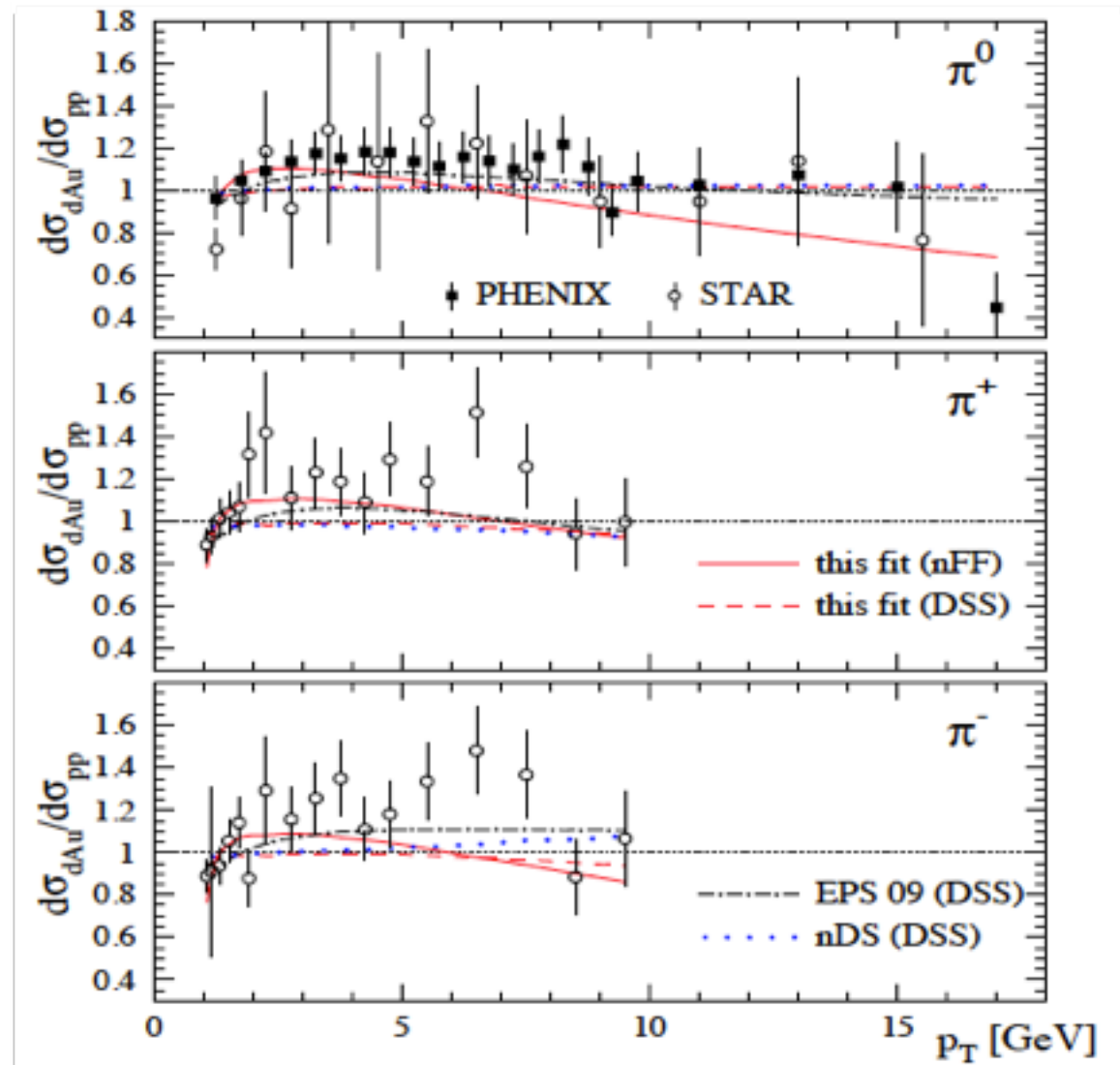
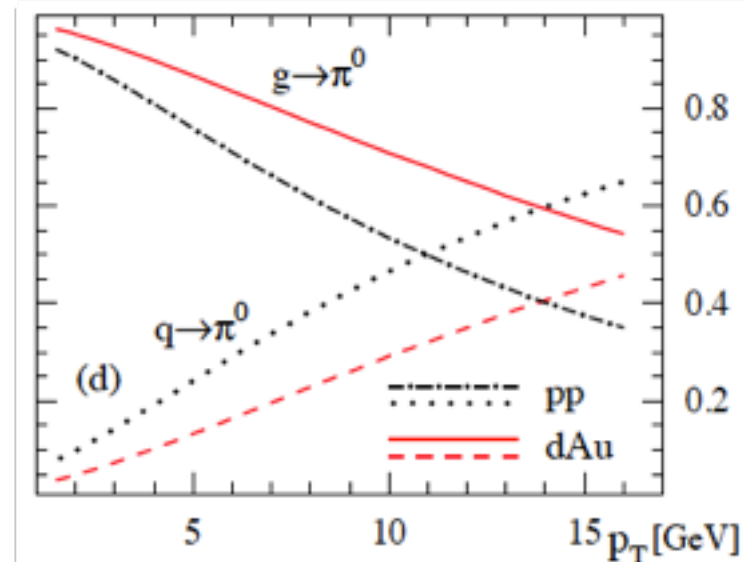
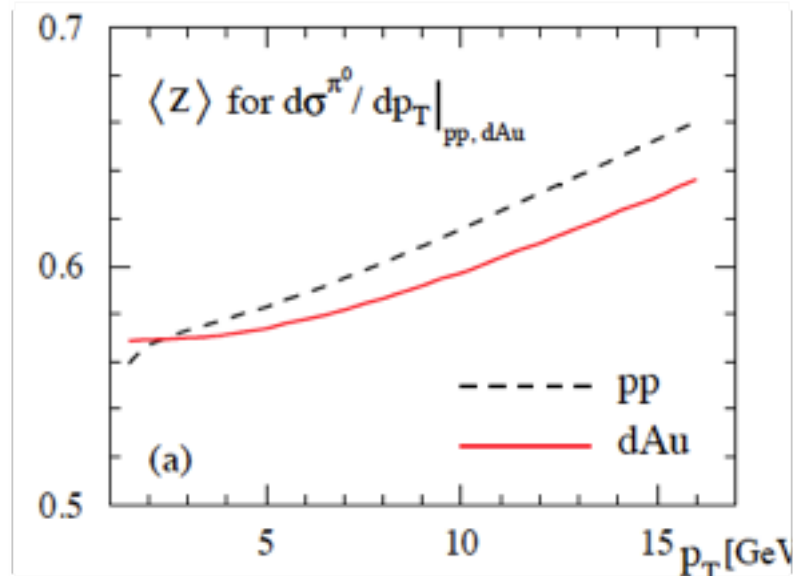
at RHIC (mid rapidity) we probe large z
and mostly pions from gluons



more on mid rapidity pions

at RHIC (mid rapidity) we probe large z
and mostly pions from gluons

result of our nPDF fit



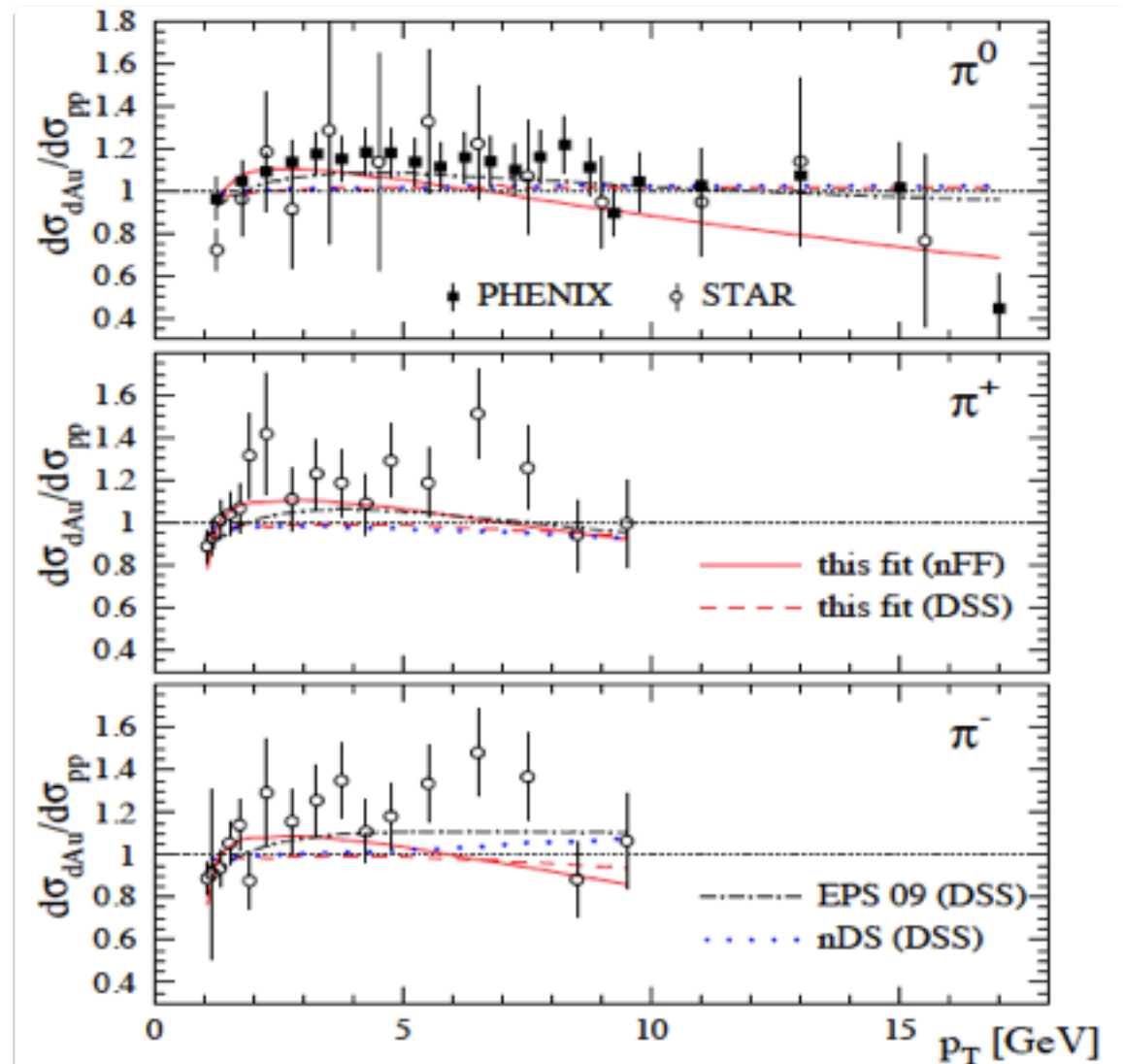
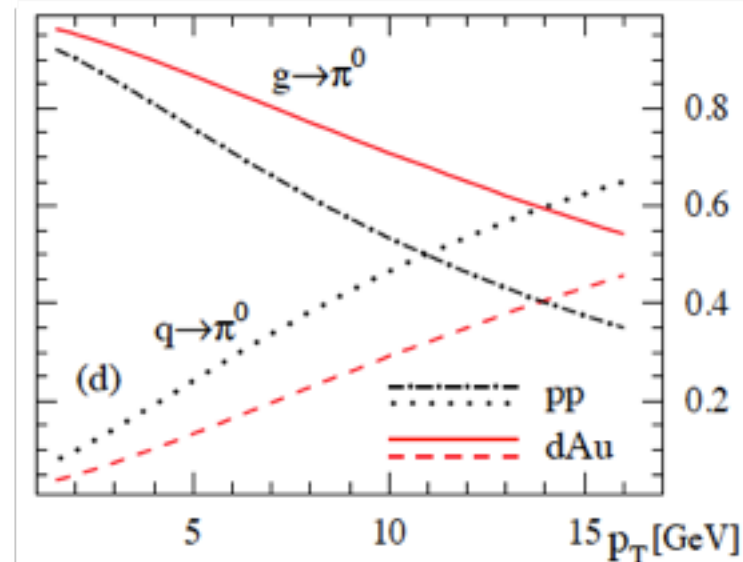
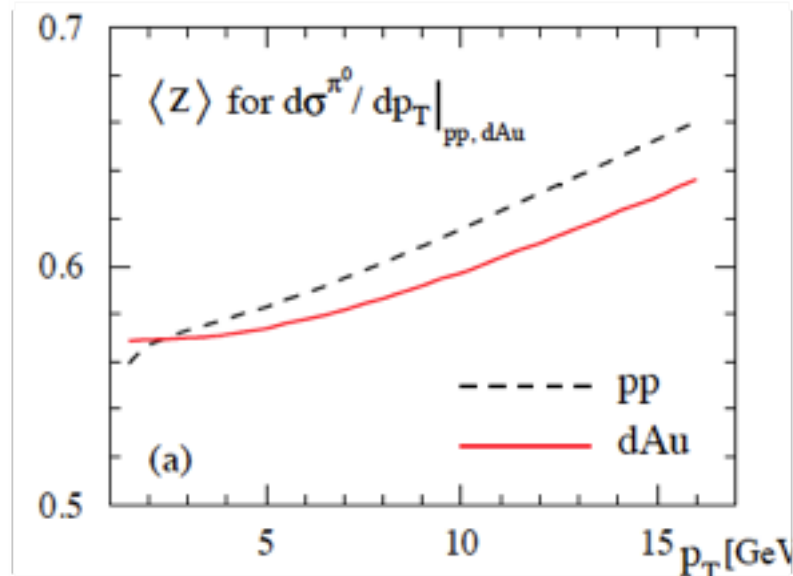
- ▶ good fit within large exp. uncertainties
- ▶ choice of FF has some impact (but not too much)

$$\chi^2 : 68.3 \text{ (nFF)} \rightarrow 83.6 \text{ (DSS)}$$

more on mid rapidity pions

at RHIC (mid rapidity) we probe large z
and mostly pions from gluons

result of our nPDF fit



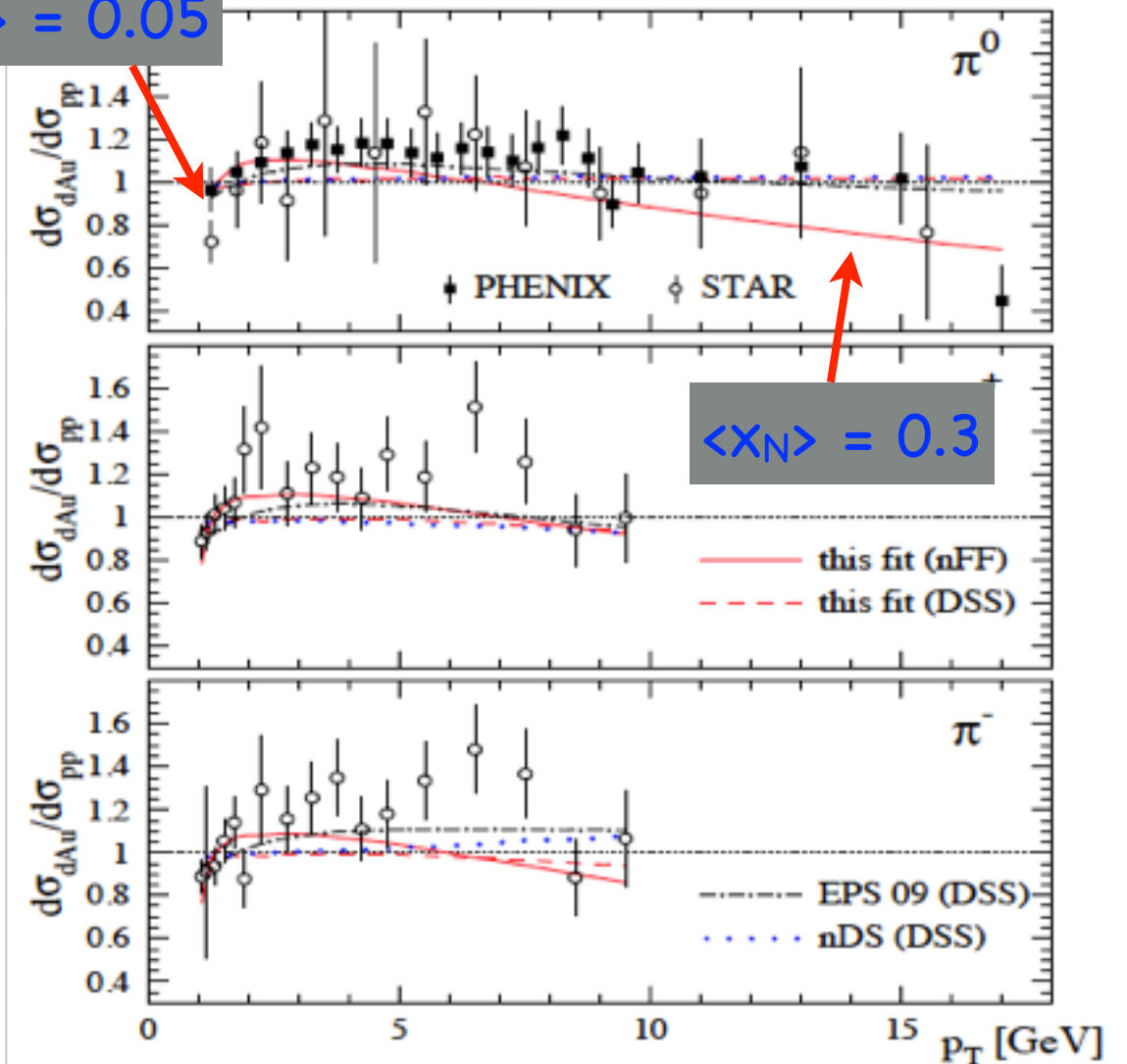
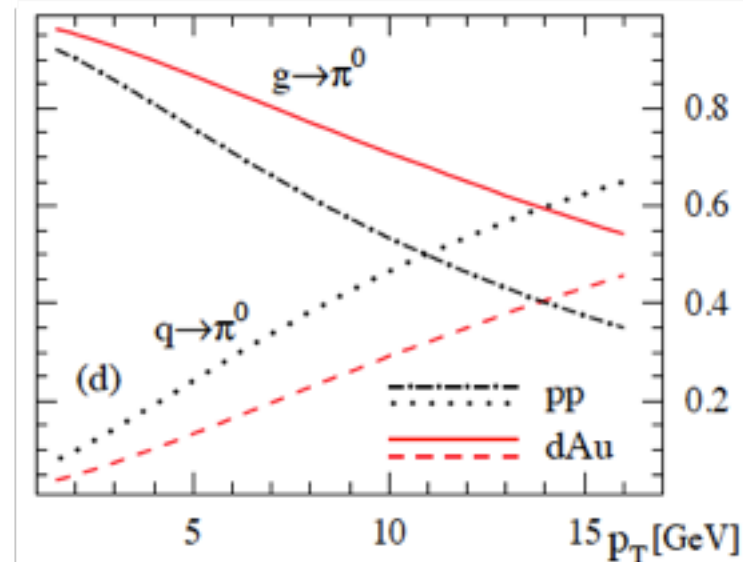
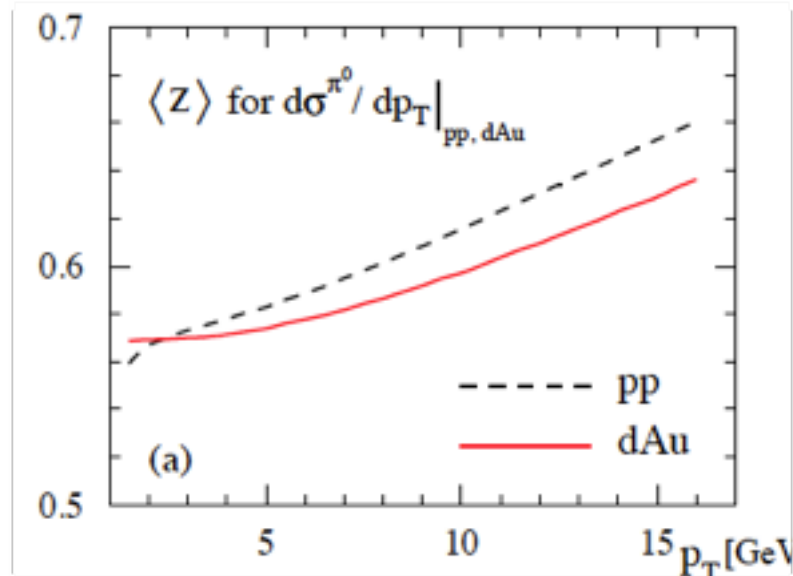
- ▶ good fit within large exp. uncertainties
- ▶ choice of FF has some impact (but not too much)
 $\chi^2 : 68.3 \text{ (nFF)} \rightarrow 83.6 \text{ (DSS)}$
- ▶ unlike EPS fit, limited impact on gluon (no weight factor)

more on mid rapidity pions

at RHIC (mid rapidity) we probe large z
and mostly pions from gluons

result of our nPDF fit

$$\langle x_N \rangle = 0.05$$



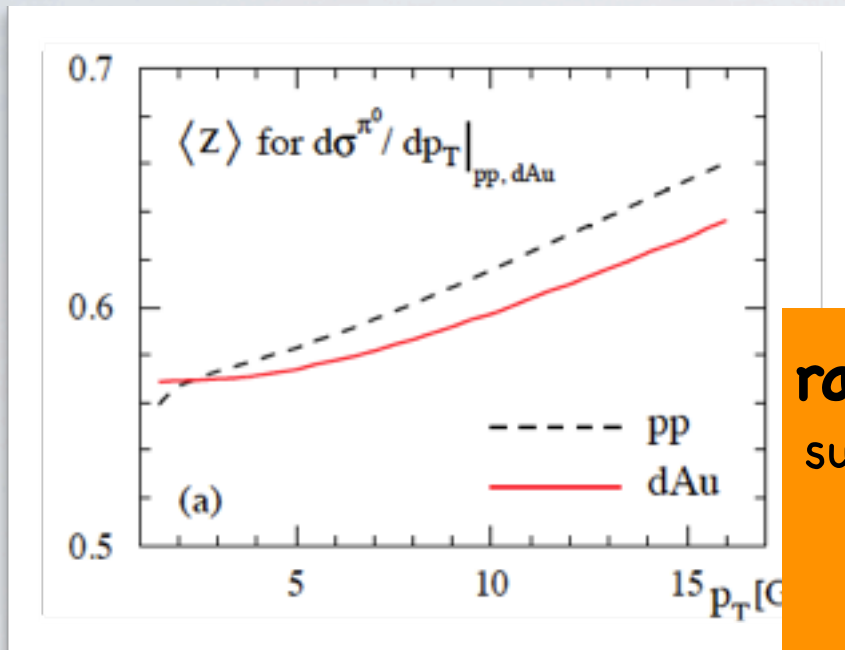
- ▶ good fit within large exp. uncertainties
- ▶ choice of FF has some impact (but not too much)
 $\chi^2 : 68.3 \text{ (nFF)} \rightarrow 83.6 \text{ (DSS)}$
- ▶ unlike EPS fit, limited impact on gluon (no weight factor)

more on mid rapidity pions

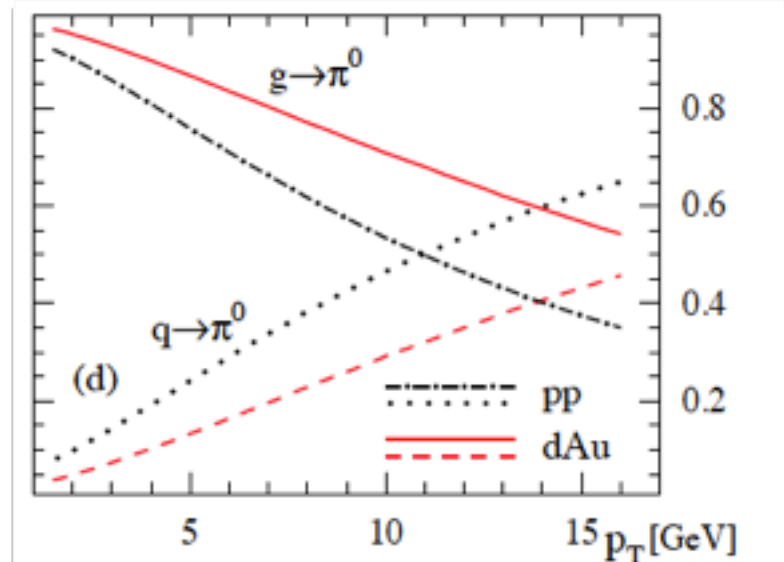
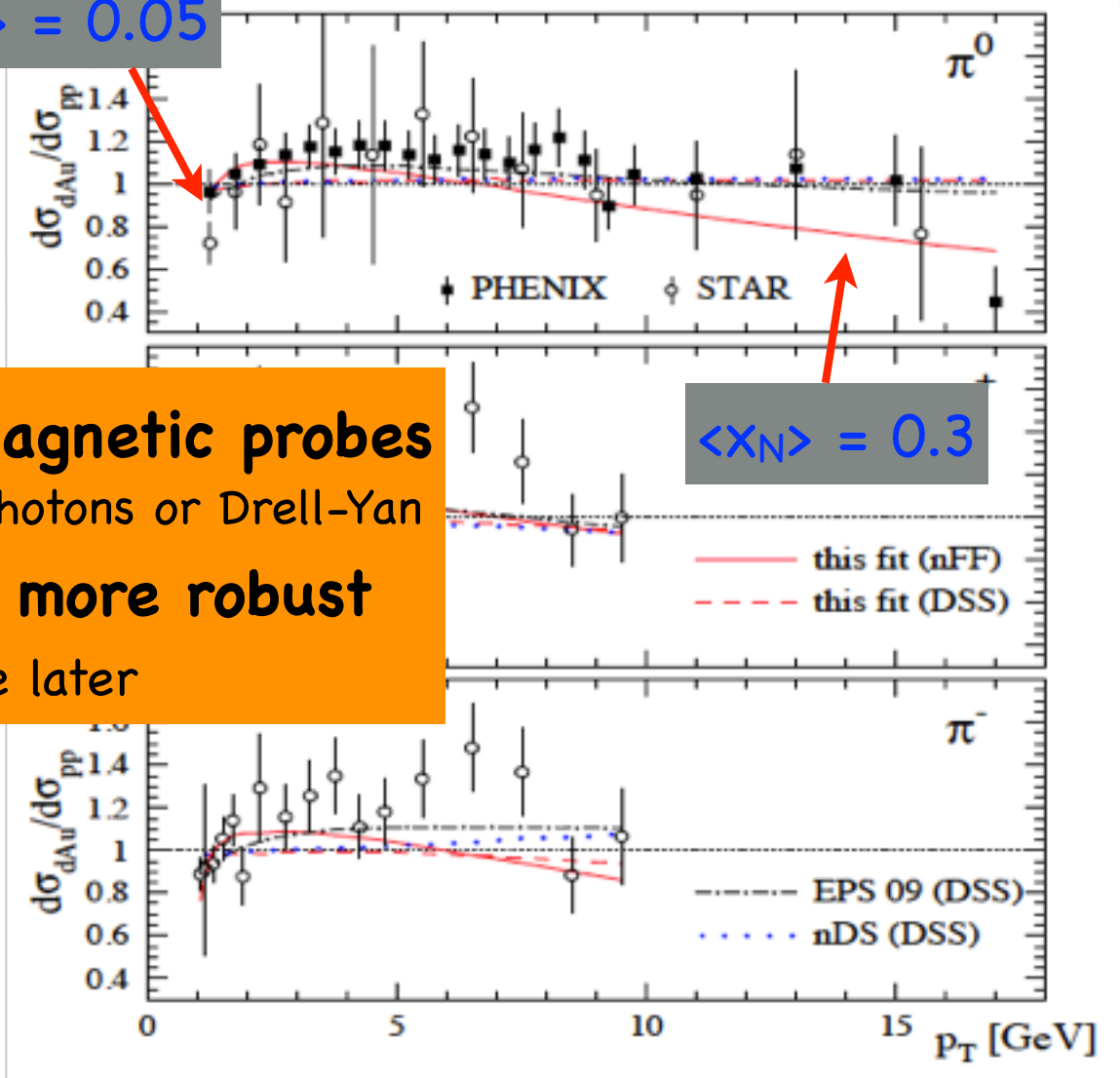
at RHIC (mid rapidity) we probe large z
and mostly pions from gluons

result of our nPDF fit

$$\langle x_N \rangle = 0.05$$



rare electromagnetic probes
such as prompt photons or Drell-Yan
are a much more robust
more later

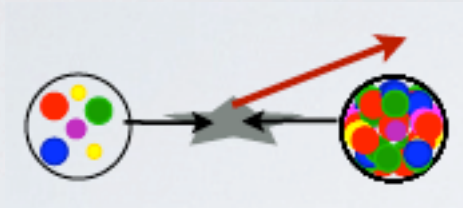


- ▶ good fit within large exp. uncertainties
- ▶ choice of FF has some impact (but not too much)
 $\chi^2 : 68.3 \text{ (nFF)} \rightarrow 83.6 \text{ (DSS)}$
- ▶ unlike EPS fit, limited impact on gluon (no weight factor)

pions in dAu at forward rapidity

why interesting

- ▶ allows to access smaller x in nucleus
- ▶ gets one closer to the region where one expects saturation effects



$$x_{1,2} \simeq \frac{p_T}{\sqrt{s}} e^{\pm y}$$

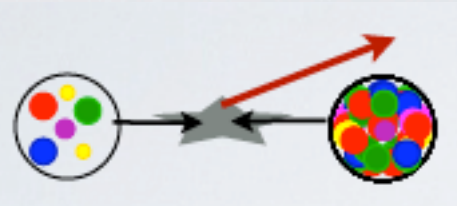
pions in dAu at forward rapidity

why interesting

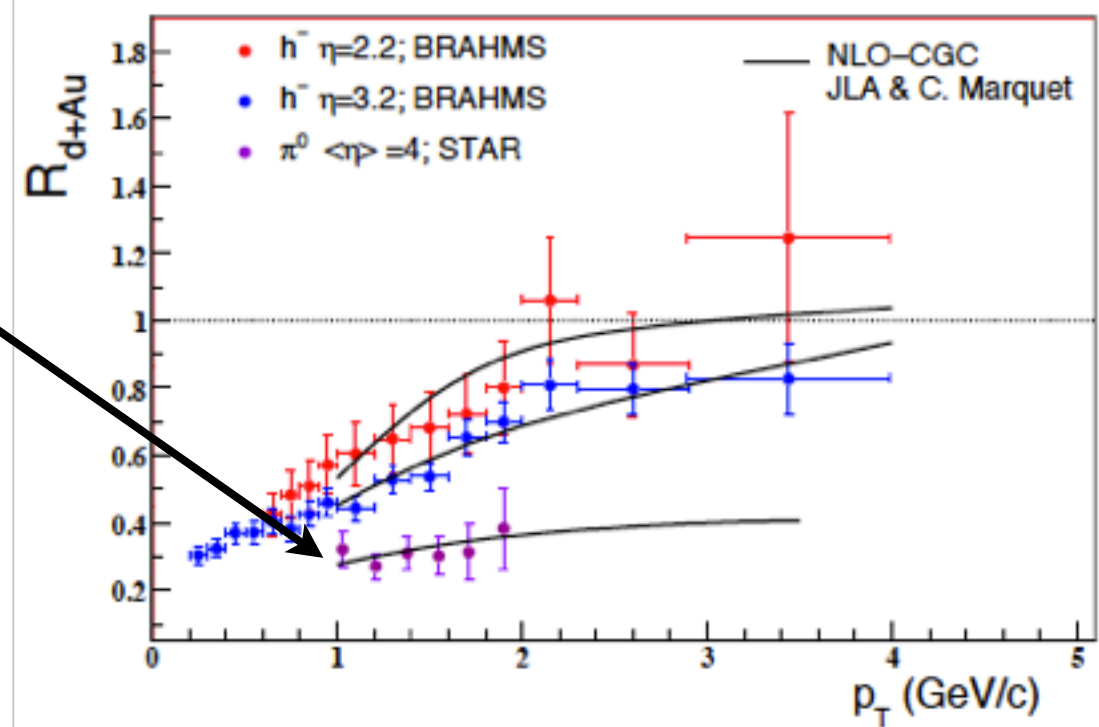
- ▶ allows to access smaller x in nucleus
- ▶ gets one closer to the region where one expects saturation effects

data indicate strong suppression of gluons at small x and low scales

forward suppression well described within **non-linear rcBK evolution (CGC)**



$$x_{1,2} \simeq \frac{p_T}{\sqrt{s}} e^{\pm y}$$



Albacete, Marquet

pions in dAu at forward rapidity

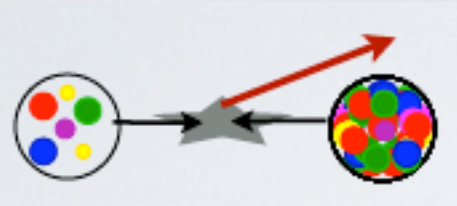
why interesting

- ▶ allows to access smaller x in nucleus
- ▶ gets one closer to the region where one expects saturation effects

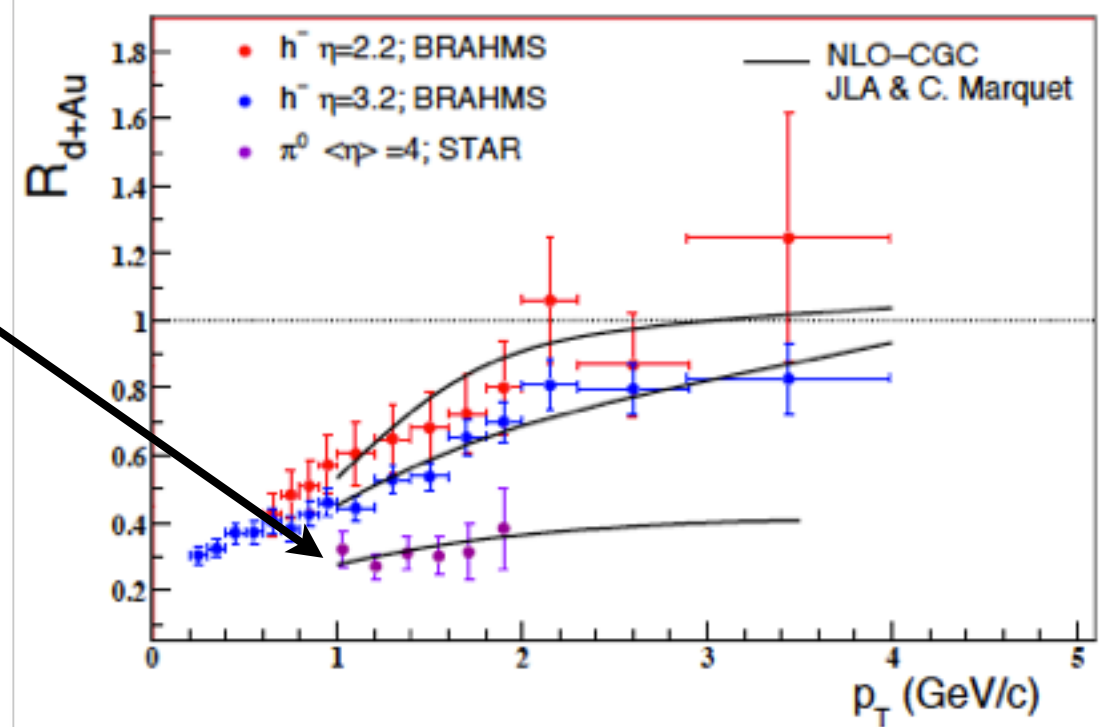
data indicate strong suppression of gluons at small x and low scales

forward suppression well described within **non-linear rcBK evolution (CGC)**

what does it take to describe it with nPDFs



$$x_{1,2} \simeq \frac{p_T}{\sqrt{s}} e^{\pm y}$$

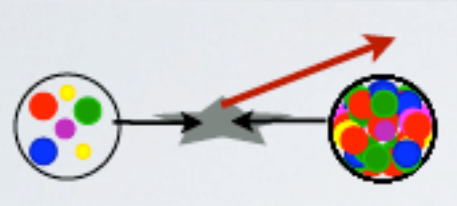


Albacete, Marquet

pions in dAu at forward rapidity

why interesting

- ▶ allows to access smaller x in nucleus
- ▶ gets one closer to the region where one expects saturation effects

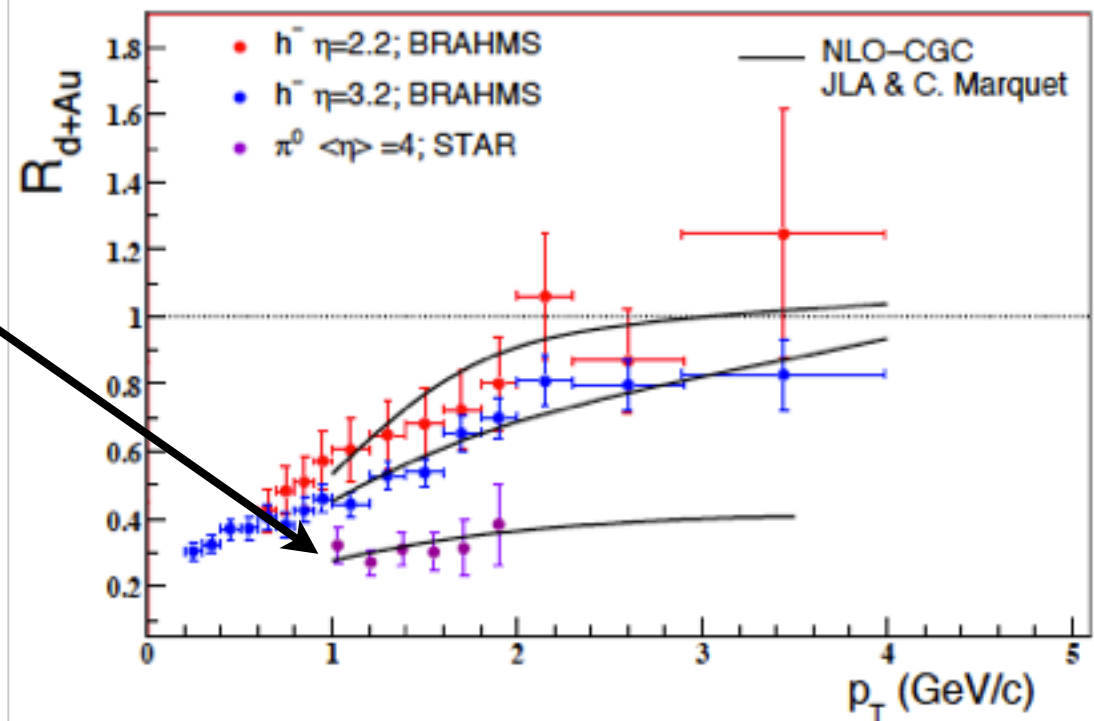


$$x_{1,2} \simeq \frac{p_T}{\sqrt{s}} e^{\pm y}$$

data indicate strong suppression of gluons at small x and low scales

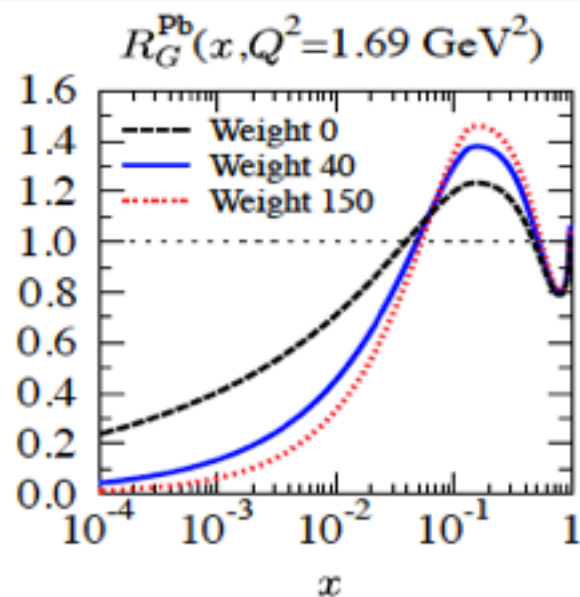
forward suppression well described within **non-linear rcBK evolution (CGC)**

what does it take to describe it with nPDFs



Albacete, Marquet

Eskola, Paukkunen, Salgado



- ▶ need humongous shadowing at a scale of about 1 GeV

pions in dAu at forward rapidity

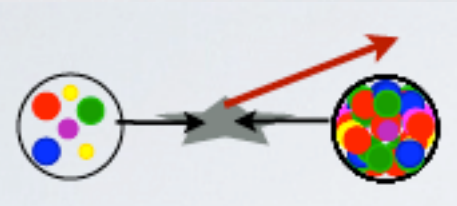
why interesting

- ▶ allows to access smaller x in nucleus
- ▶ gets one closer to the region where one expects saturation effects

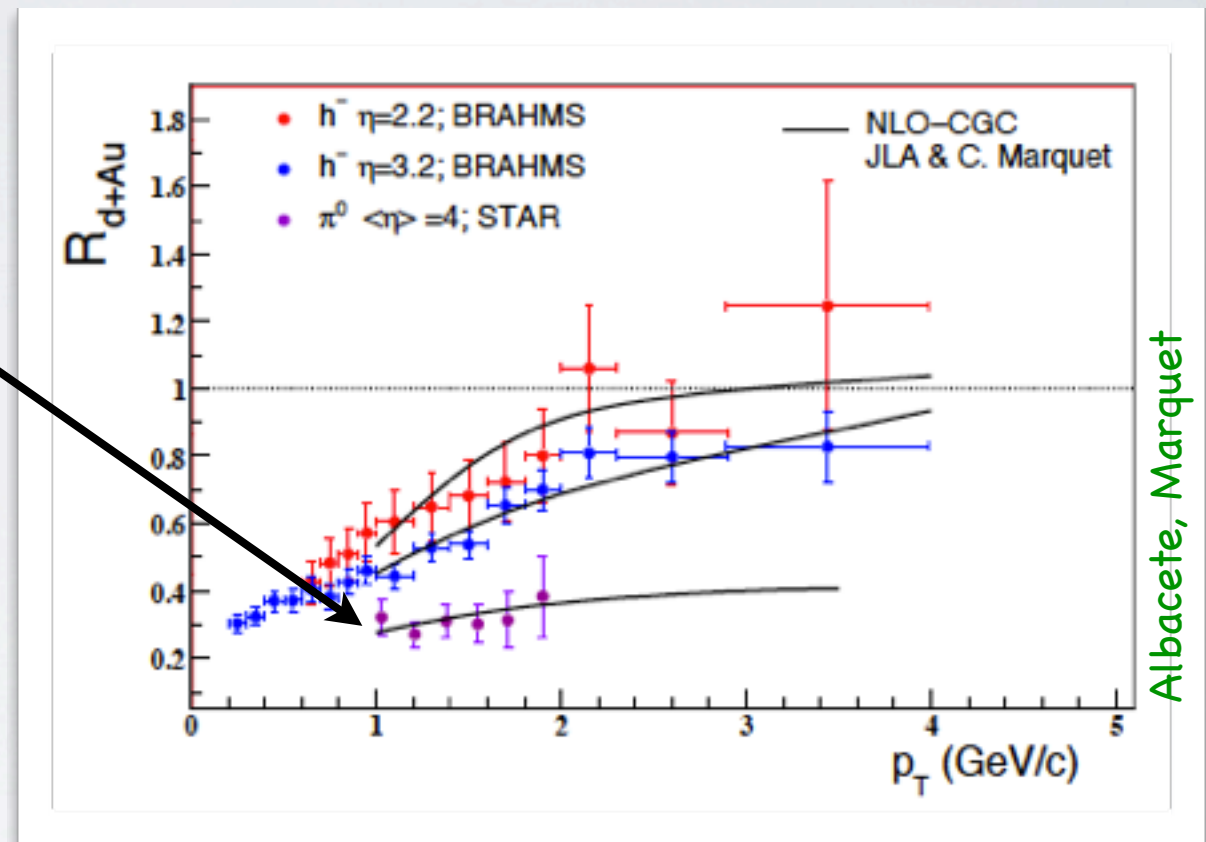
data indicate strong suppression of gluons at small x and low scales

forward suppression well described within **non-linear rcBK evolution (CGC)**

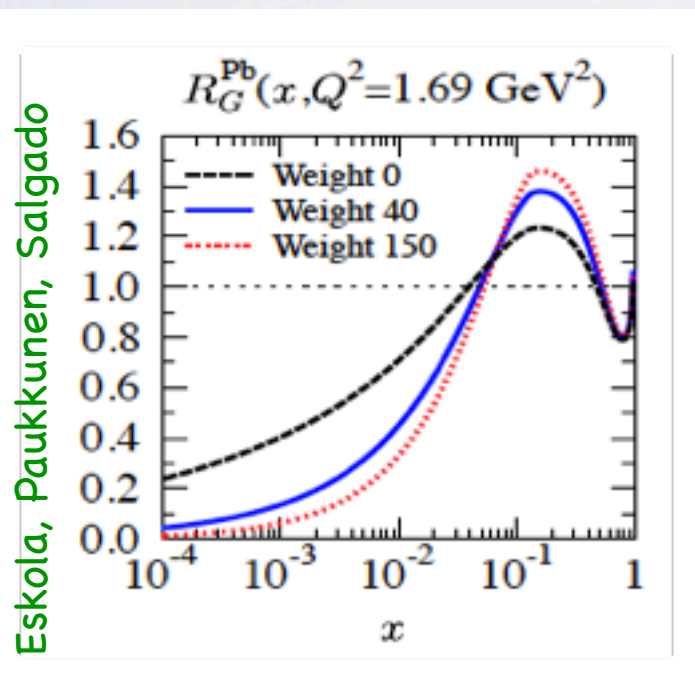
what does it take to describe it with nPDFs



$$x_{1,2} \simeq \frac{p_T}{\sqrt{s}} e^{\pm y}$$



Albacete, Marquet

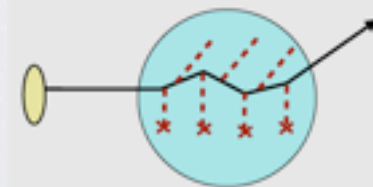


Eskola, Paukkunen, Salgado

- ▶ need humongous shadowing at a scale of about 1 GeV



could be much less if final-state effects are relevant
advocated by Frankfurt, Strikman; Kopeliovich; ...



pions in dAu at forward rapidity

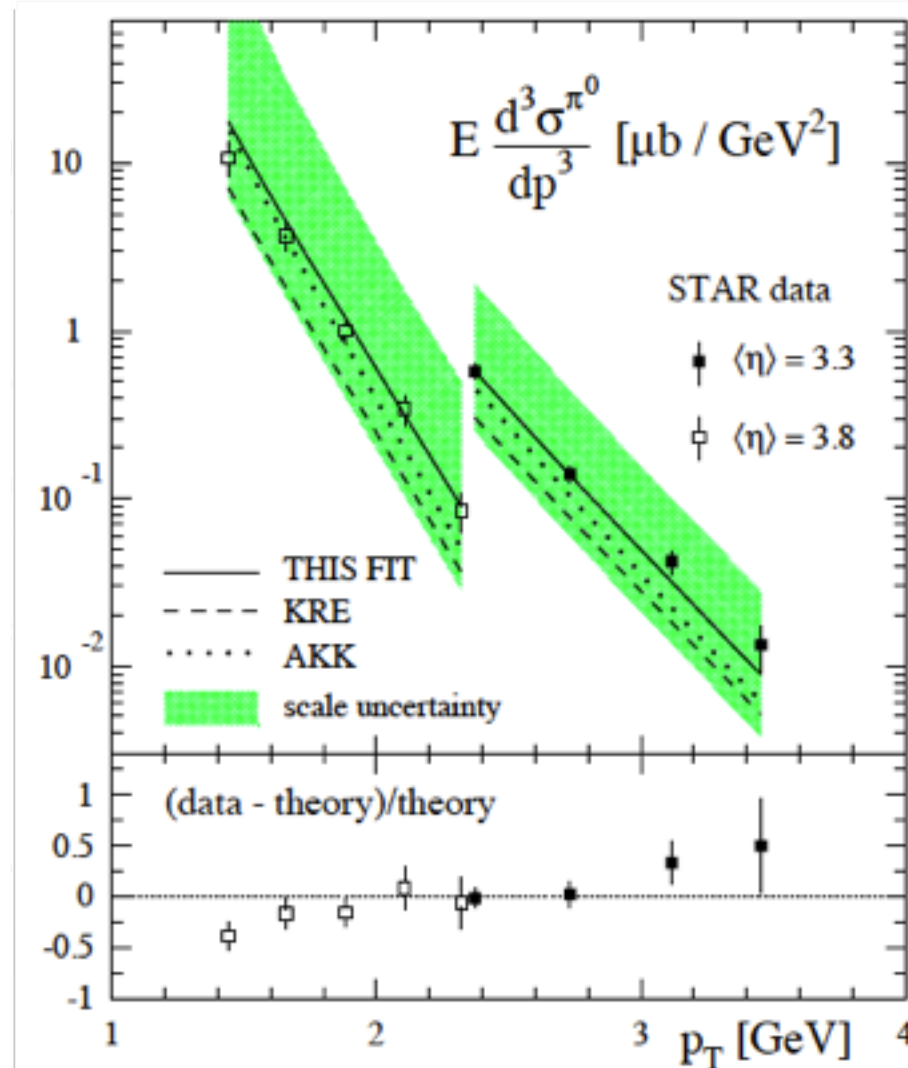
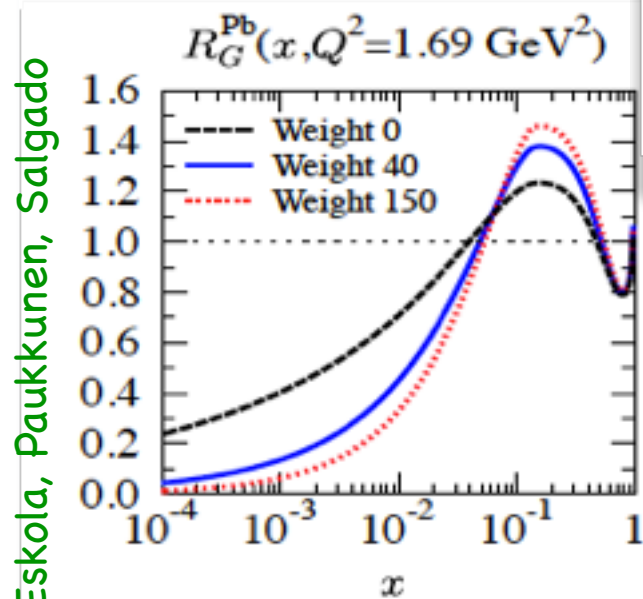
why interesting

- ▶ allows to access smaller x
- ▶ gets one closer to the region where one expects saturation effects

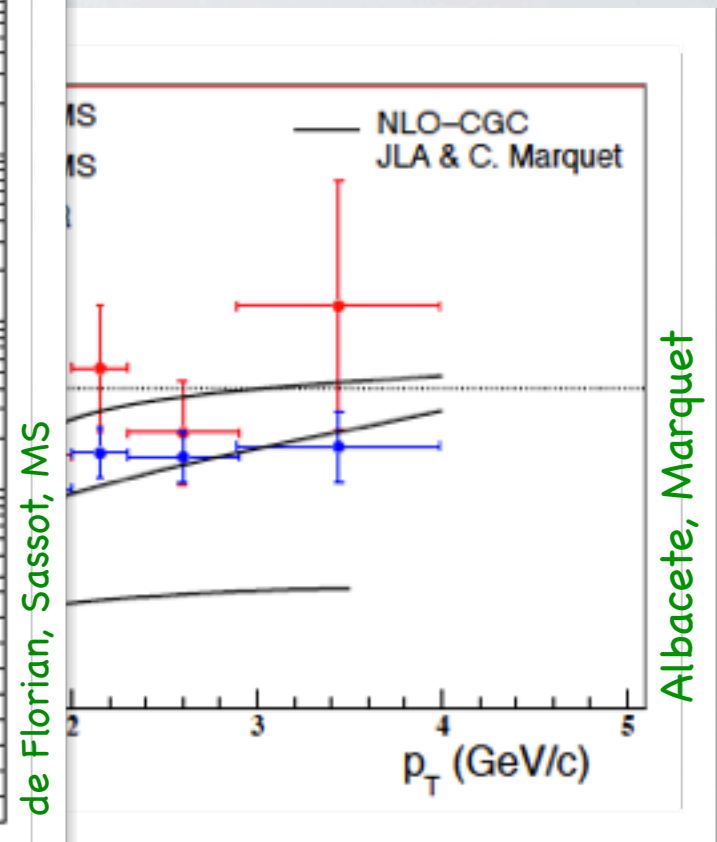
data indicate strong suppression of gluons at small x and low p_T

forward suppression well described within non-linear rcBK evolution

what does it take to describe



$$x_{1,2} \simeq \frac{p_T}{\sqrt{s}} e^{\pm y}$$



- ▶ need humongous shadowing at a scale of about 1 GeV



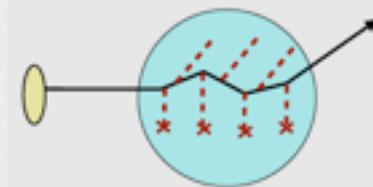
could be much less if final-state effects are relevant
advocated by Frankfurt, Strikman; Kopeliovich; ...



pQCD does not work well at small p_T and large y
corrections become excessive; pp data for $y=4$ not used in any fit

general issue with pQCD and forward physics at RHIC

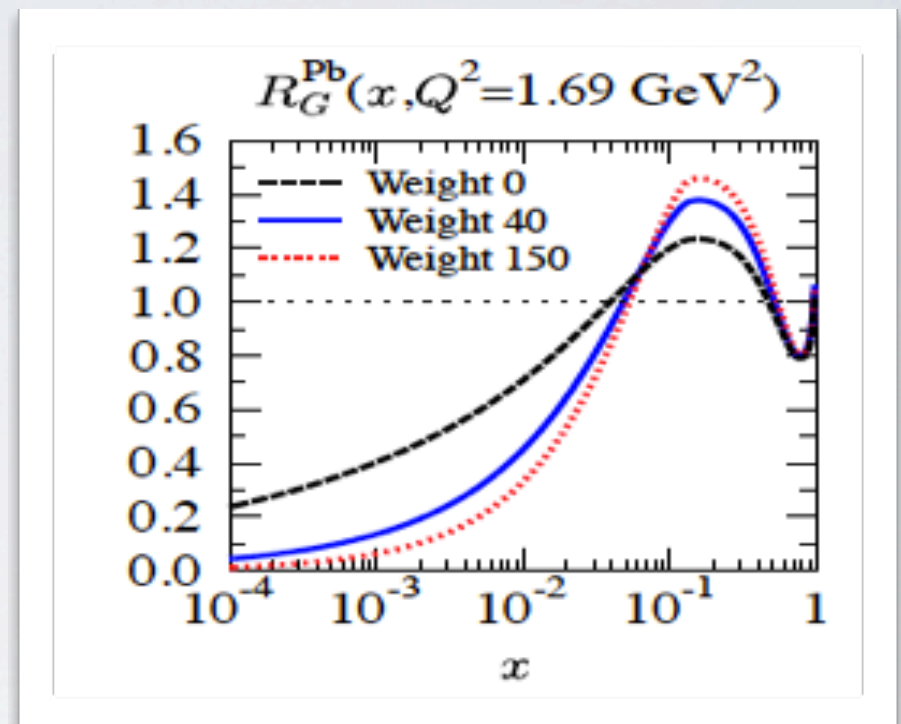
recall: CGC has Q_s as additional semi-hard scale



how “bad” are extreme initial conditions?

we refrain from using the forward dAu data in our analysis ...

... however, there is enough freedom at small x to enforce a good description at the expense of strong shadowing

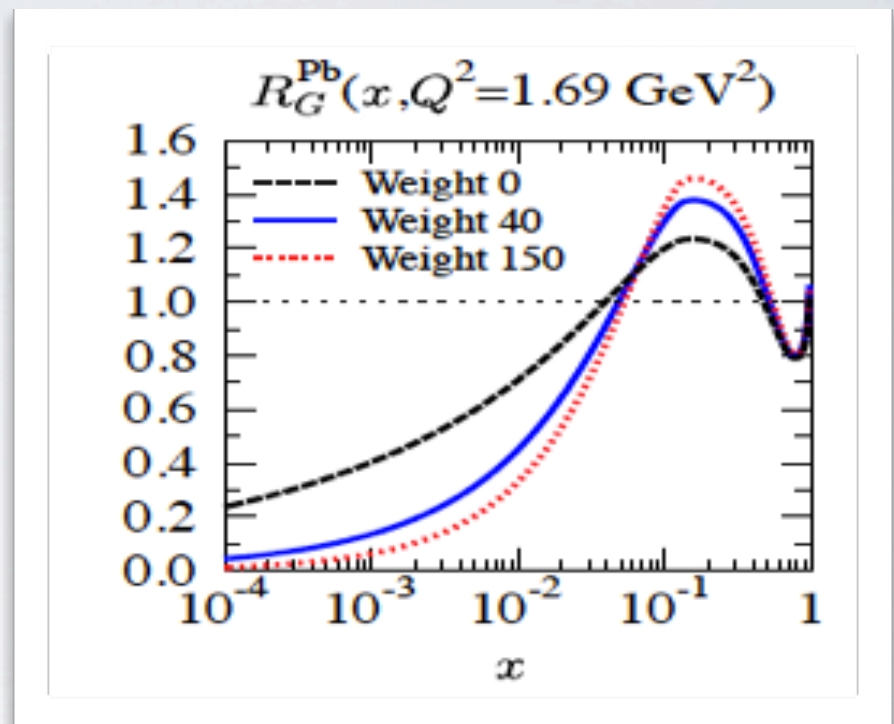


how “bad” are extreme initial conditions?

we refrain from using the forward dAu data in our analysis ...

... however, there is enough freedom at small x to enforce a good description at the expense of strong shadowing

an evil choice of initial conditions ?



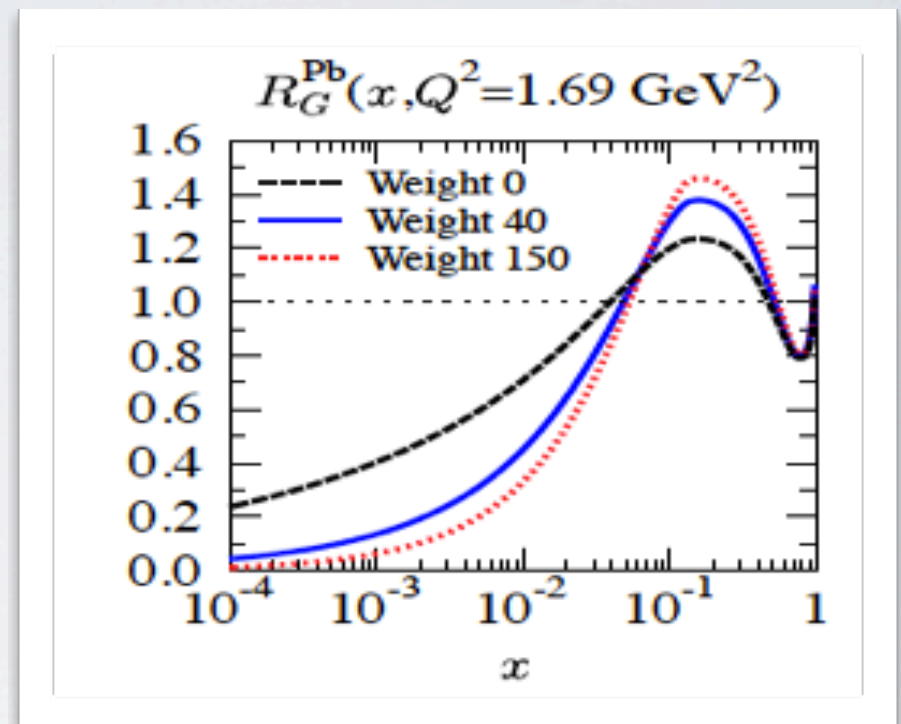
how “bad” are extreme initial conditions?

we refrain from using the forward dAu data in our analysis ...

... however, there is enough freedom at small x to enforce a good description at the expense of strong shadowing

an evil choice of initial conditions ?

well, ...



- ▶ DGLAP only predicts the scale evolution
- ▶ input usually quickly washed out

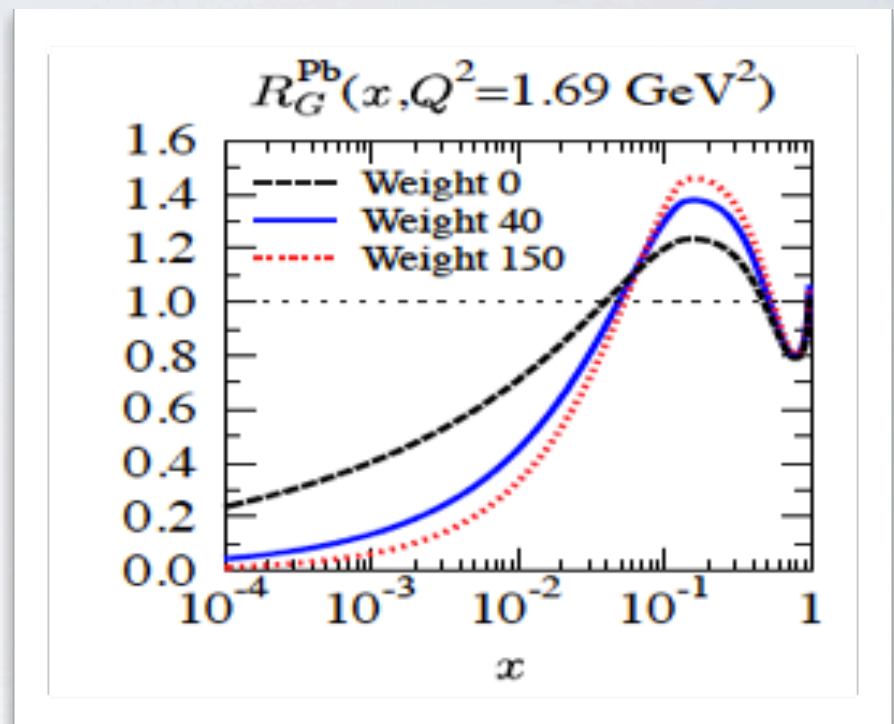
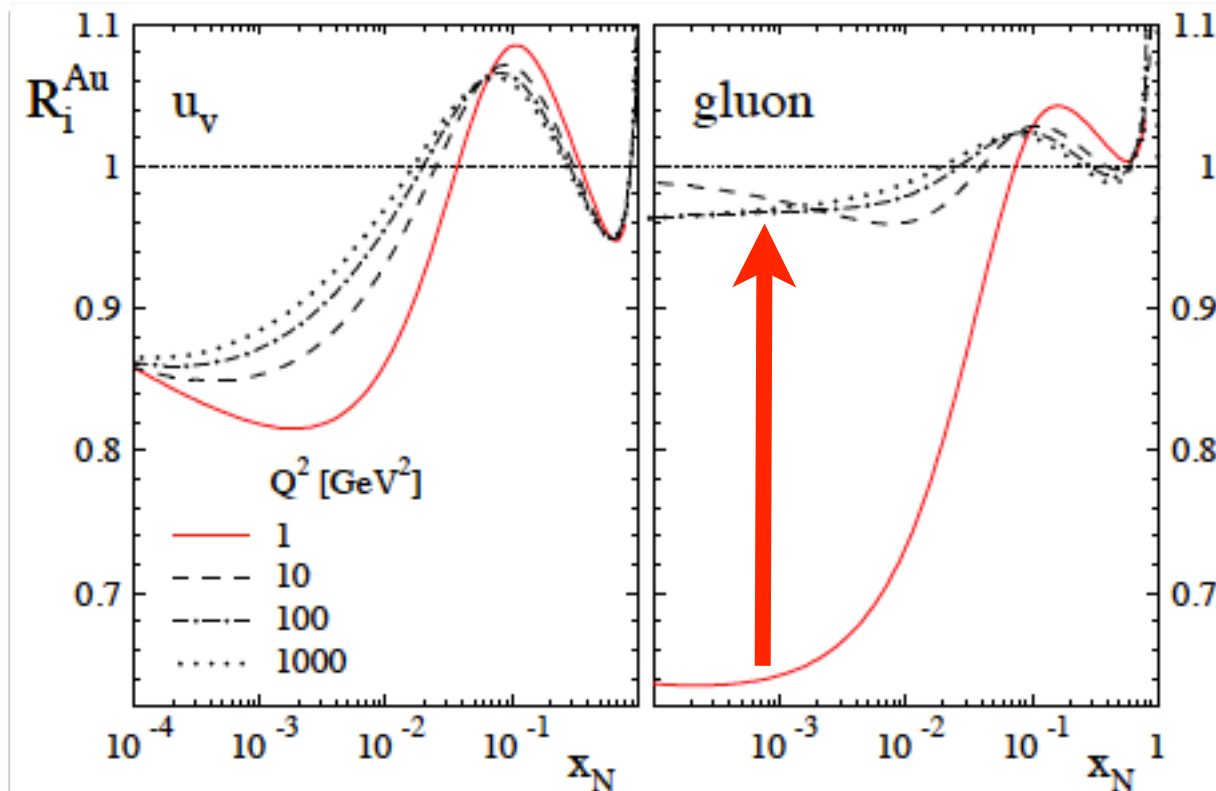
how "bad" are extreme initial conditions?

we refrain from using the forward dAu data in our analysis ...

... however, there is enough freedom at small x to enforce a good description at the expense of strong shadowing

an evil choice of initial conditions ?

well, ...



- ▶ DGLAP only predicts the scale evolution
- ▶ input usually quickly washed out

a strong shadowing of the gluon
would quickly evolve away

how about using nPDFs in AA collisions ?

many observables of interest involve

small p_T , global properties, centrality dependence,



how about using nPDFs in AA collisions ?

many observables of interest involve

small p_T , global properties, centrality dependence,



- **nPDFs are collinear objects**

there is no impact parameter or other geometrical dependence

recently: EPS nPDFs decorated with some b dependence
[Helenius, Eskola, Honkanen, Salgado arXiv:1205.5359](#)

- **many observables in AA have no “hard scale”**

not amenable to pQCD calculations in standard factorizations

- **assuming factorization in AA is a stretch**

there might be some hard probes where things work out though

how about using nPDFs in AA collisions ?

many observables of interest involve

small p_T , global properties, centrality dependence,



- **nPDFs are collinear objects**

there is no impact parameter or other geometrical dependence

recently: EPS nPDFs decorated with some b dependence
[Helenius, Eskola, Honkanen, Salgado arXiv:1205.5359](#)

- **many observables in AA have no “hard scale”**

not amenable to pQCD calculations in standard factorizations

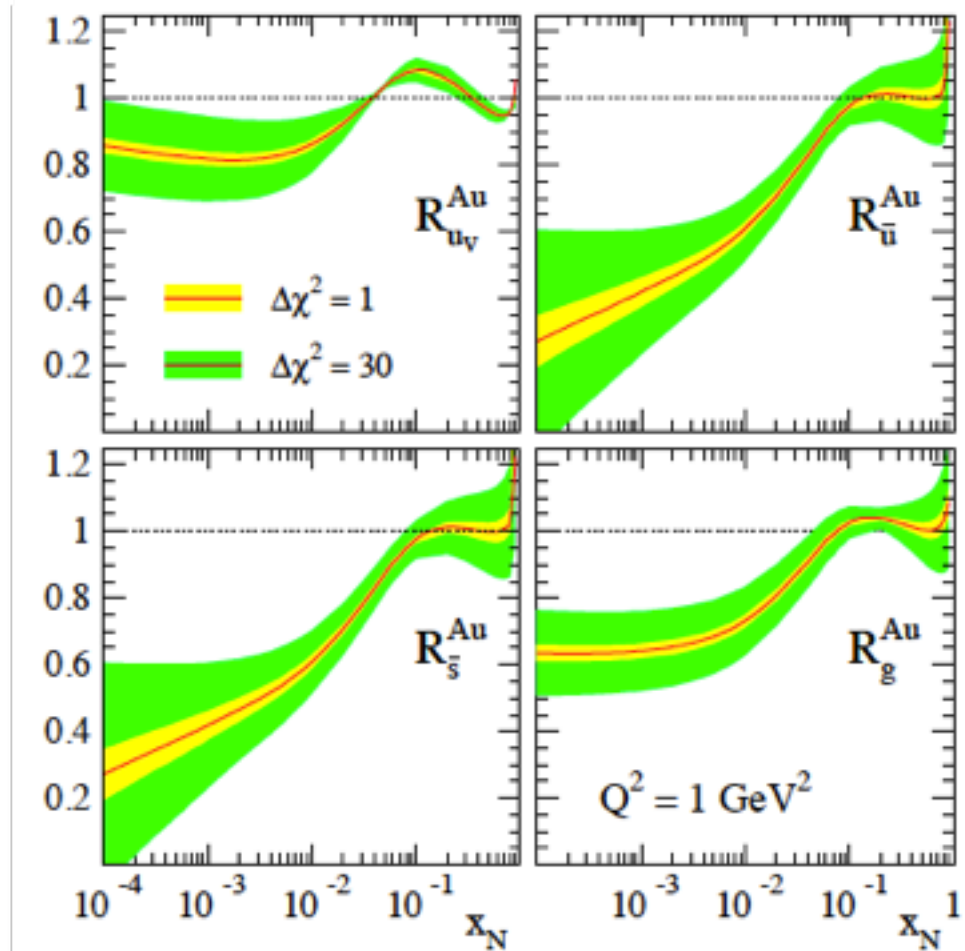
- **assuming factorization in AA is a stretch**

there might be some hard probes where things work out though

we do not touch AA data for the time being
nPDFs should be determined from probes in eA or pA
preferentially electromagnetic ones (free of hadronization issues)

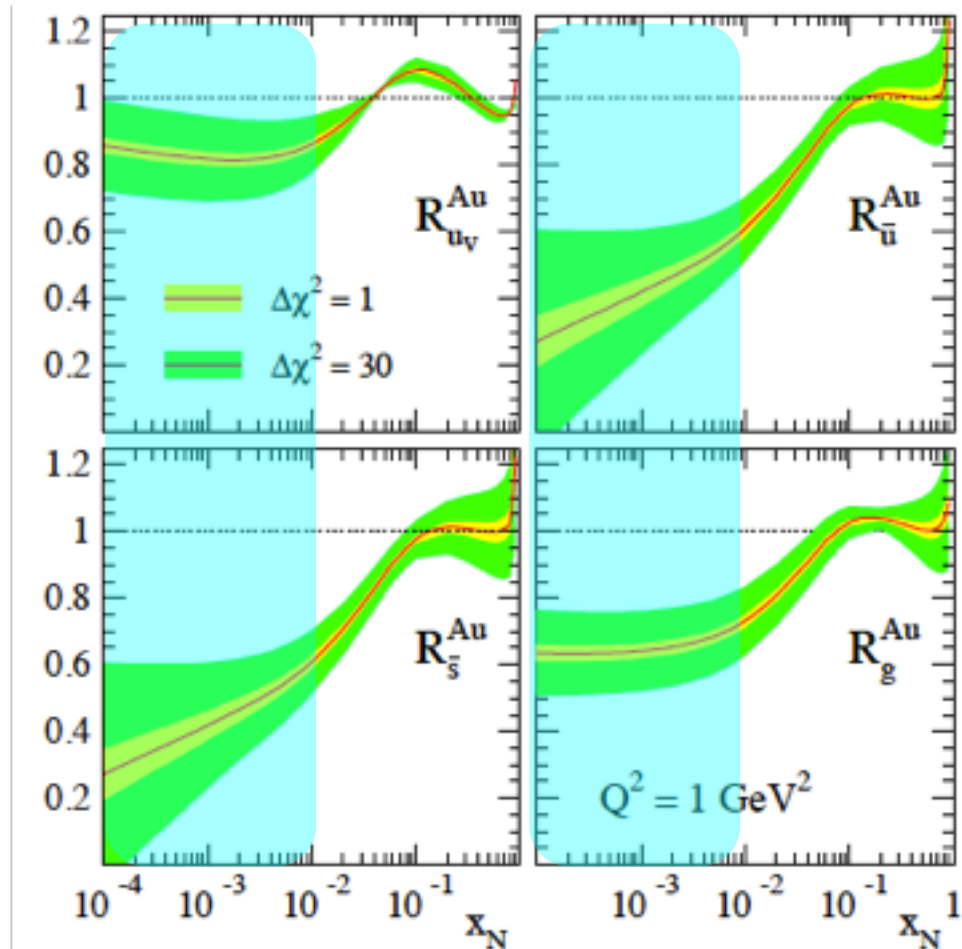
DSSZ nPDFs and their uncertainties

uncertainties at input scale of 1 GeV (for gold nucleus)



DSSZ nPDFs and their uncertainties

uncertainties at input scale of 1 GeV (for gold nucleus)

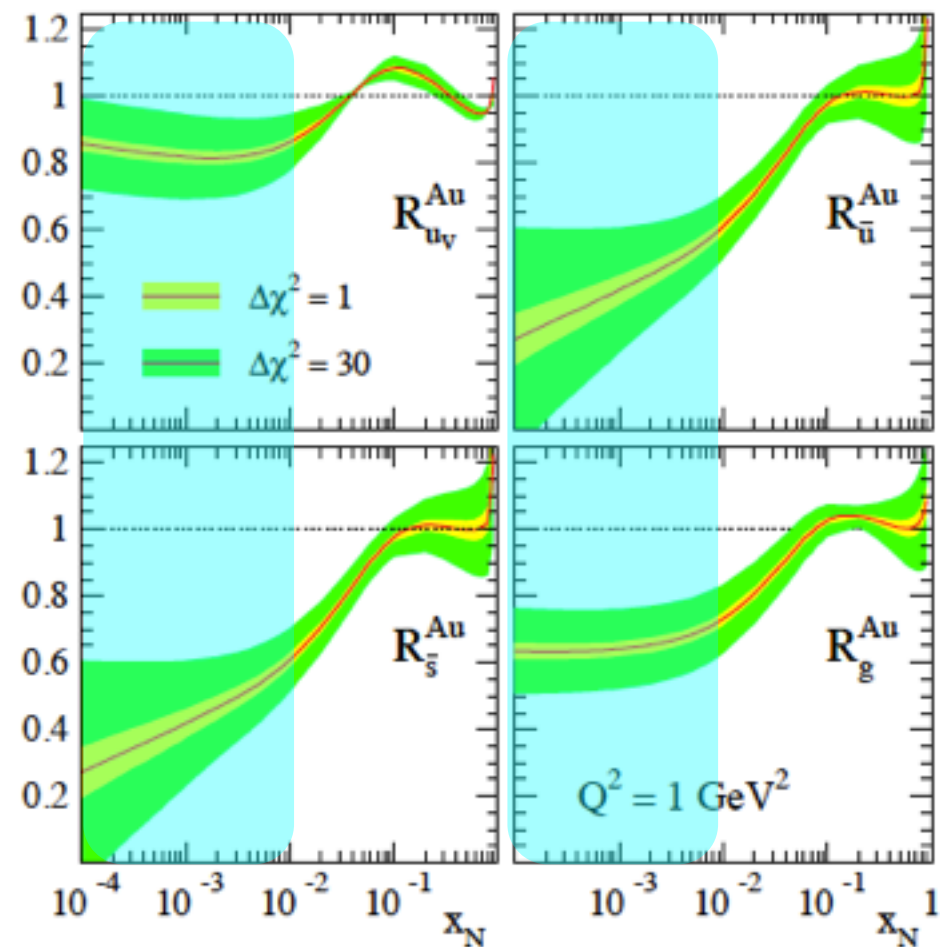


- **uncertainties below 0.01** merely reflect extrapolation of chosen functional form
not constrained by any data



DSSZ nPDFs and their uncertainties

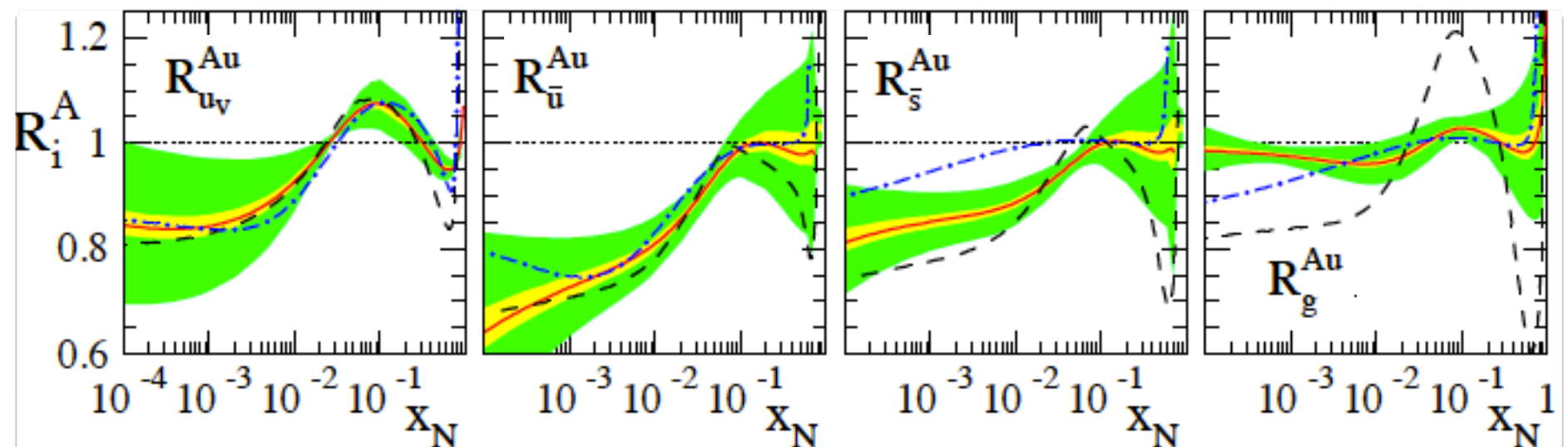
uncertainties at input scale of 1 GeV (for gold nucleus)



- **uncertainties below 0.01** merely reflect extrapolation of chosen functional form
not constrained by any data
- nuclear modifications quickly diminish under evolution

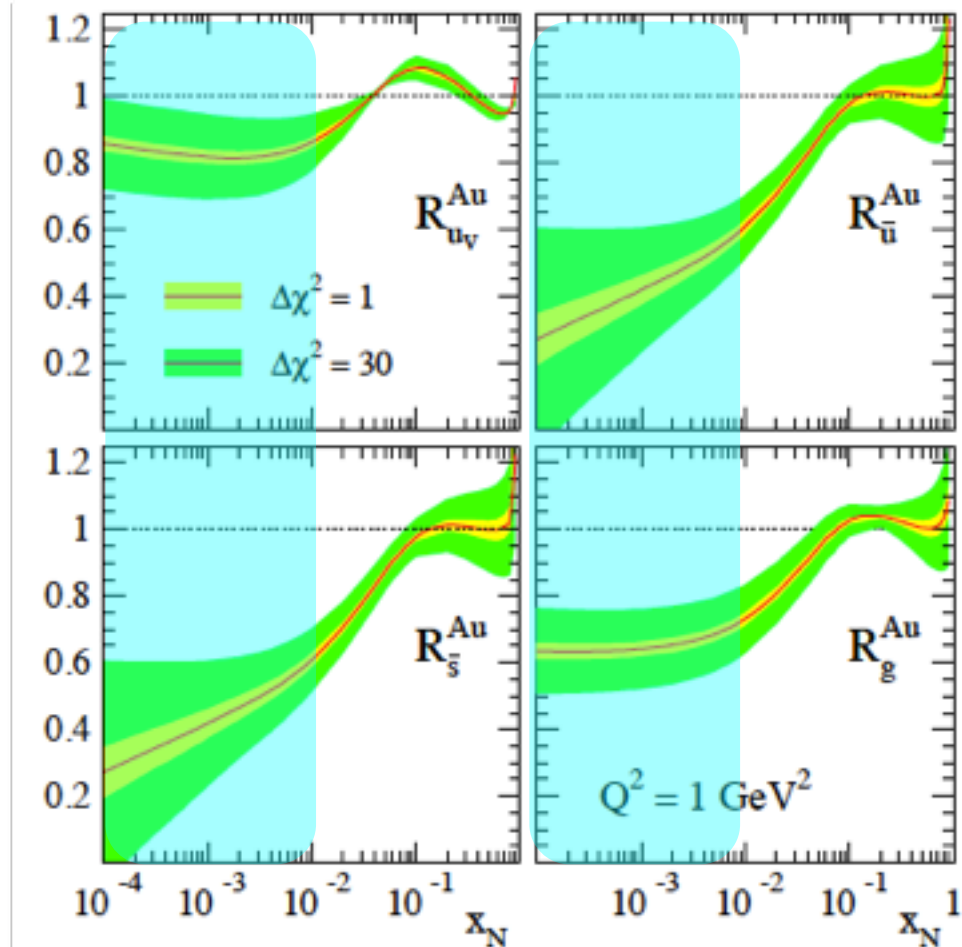


evolve to 10 GeV₂



DSSZ nPDFs and their uncertainties

uncertainties at input scale of 1 GeV (for gold nucleus)

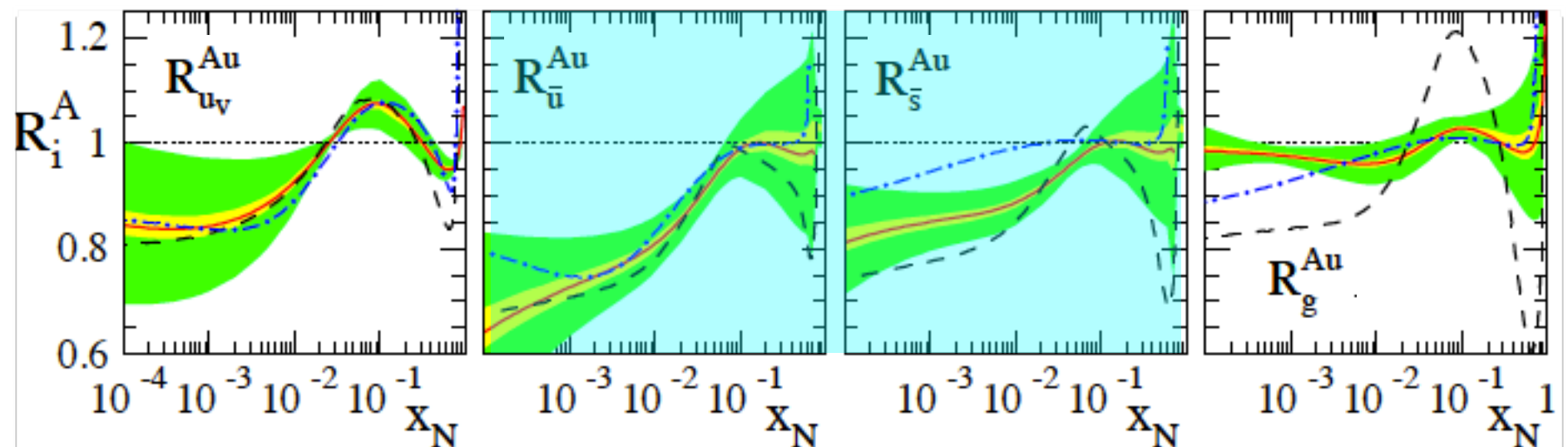


- uncertainties below 0.01 merely reflect extrapolation of chosen functional form
not constrained by any data



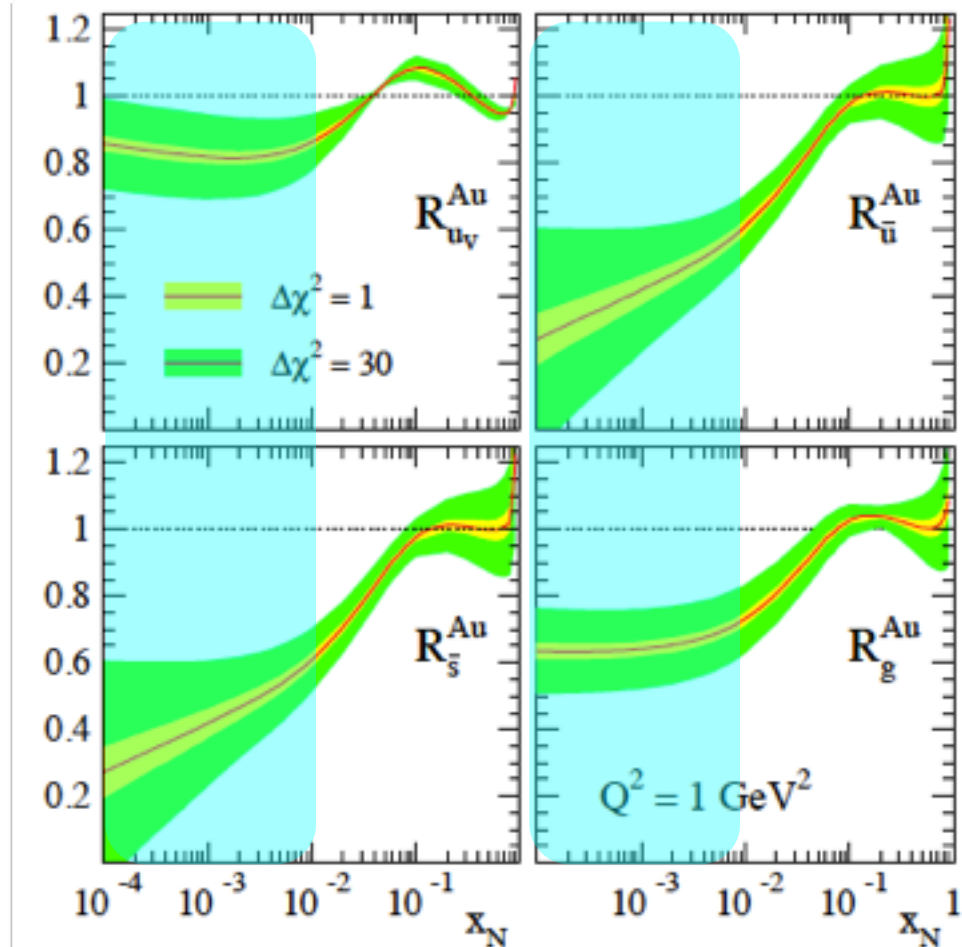
- nuclear modifications quickly diminish under evolution
- evolution imprints different nuclear effects on individual quark flavors
recall: we start with $R_u^A = R_d^A = R_s^A$

evolve to 10 GeV^2



DSSZ nPDFs and their uncertainties

uncertainties at input scale of 1 GeV (for gold nucleus)

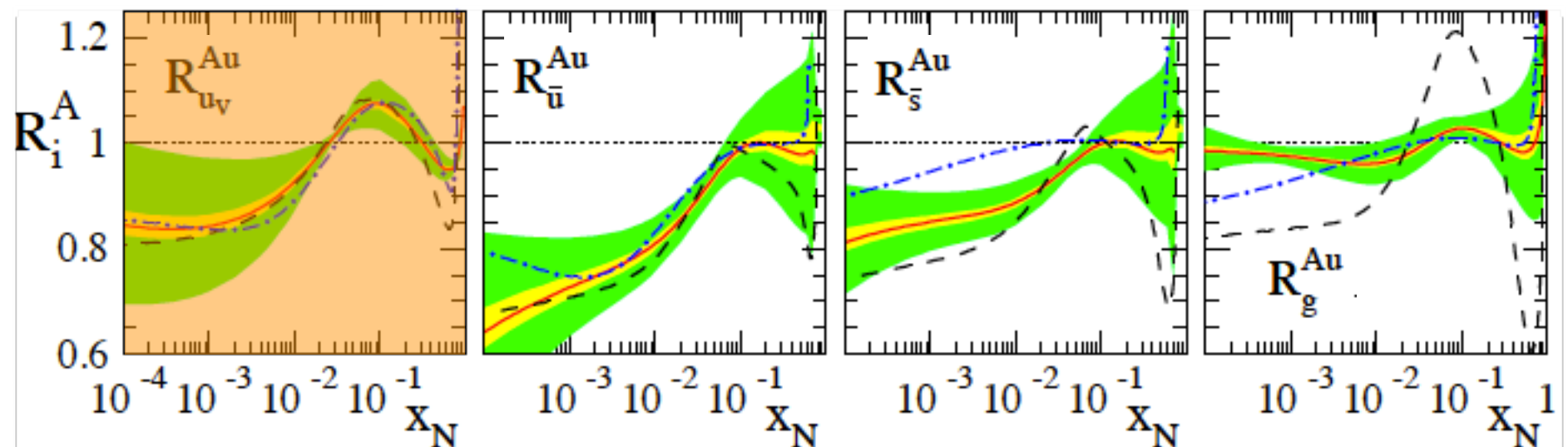


- uncertainties below 0.01 merely reflect extrapolation of chosen functional form
not constrained by any data



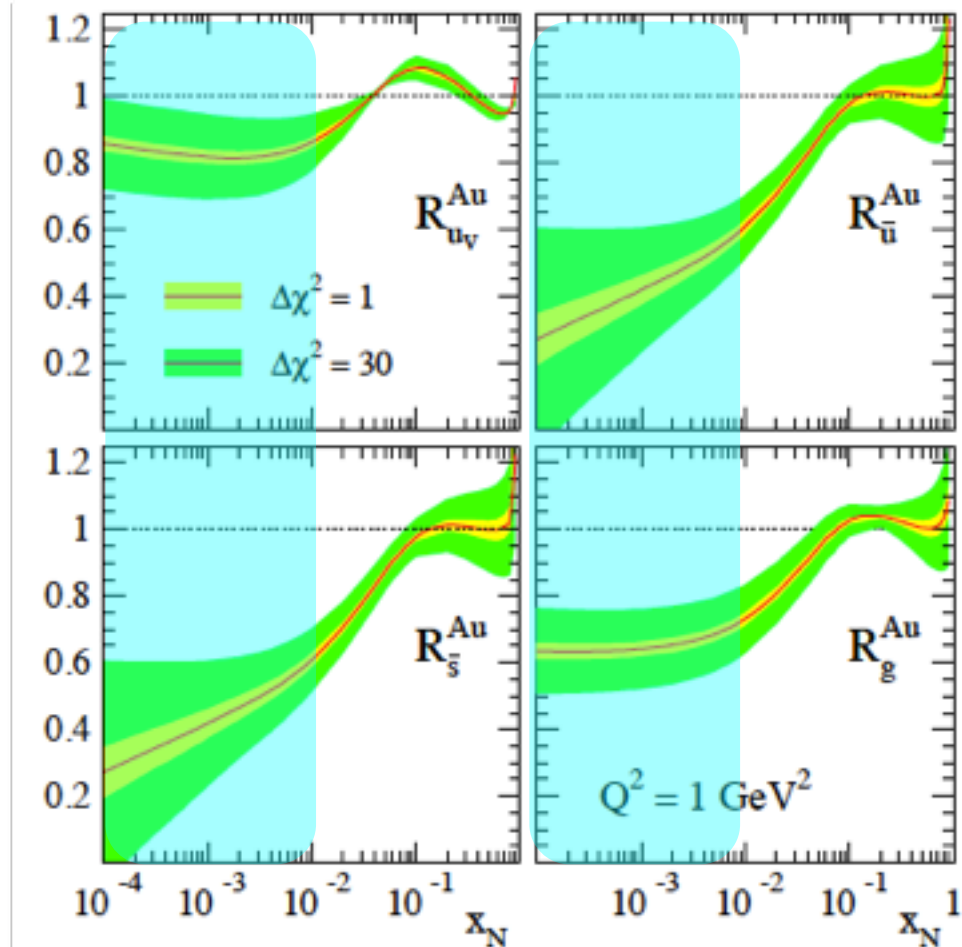
- nuclear modifications quickly diminish under evolution
- evolution imprints different nuclear effects on individual quark flavors
recall: we start with $R_u^A = R_d^A = R_s^A$
- $R_{u_v}^A$ exhibits textbook-like behavior

evolve to 10 GeV²



DSSZ nPDFs and their uncertainties

uncertainties at input scale of 1 GeV (for gold nucleus)

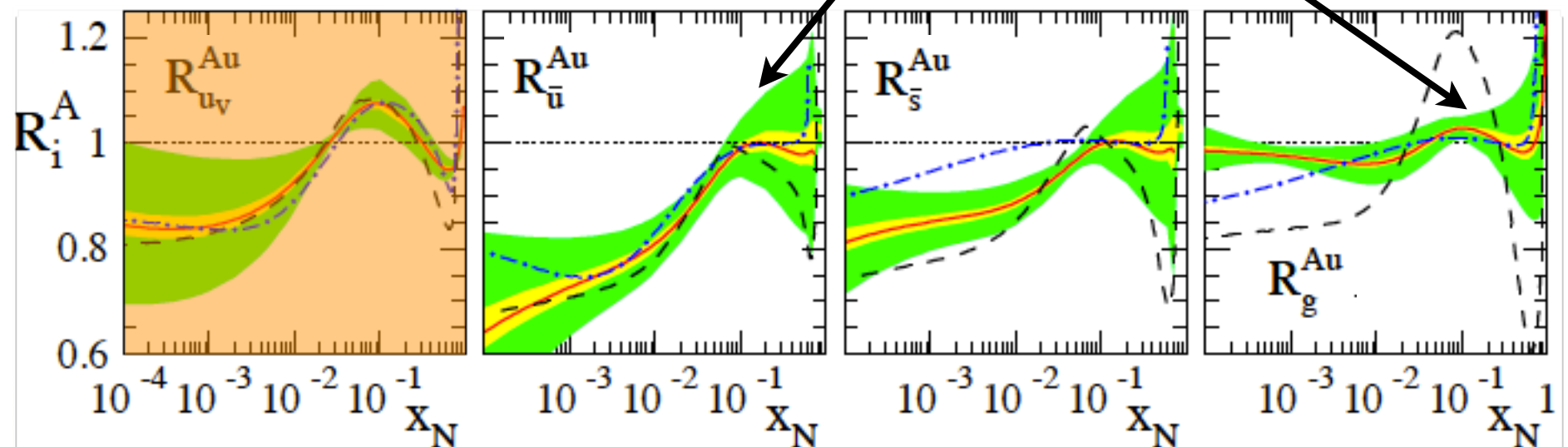


- uncertainties below 0.01 merely reflect extrapolation of chosen functional form
not constrained by any data



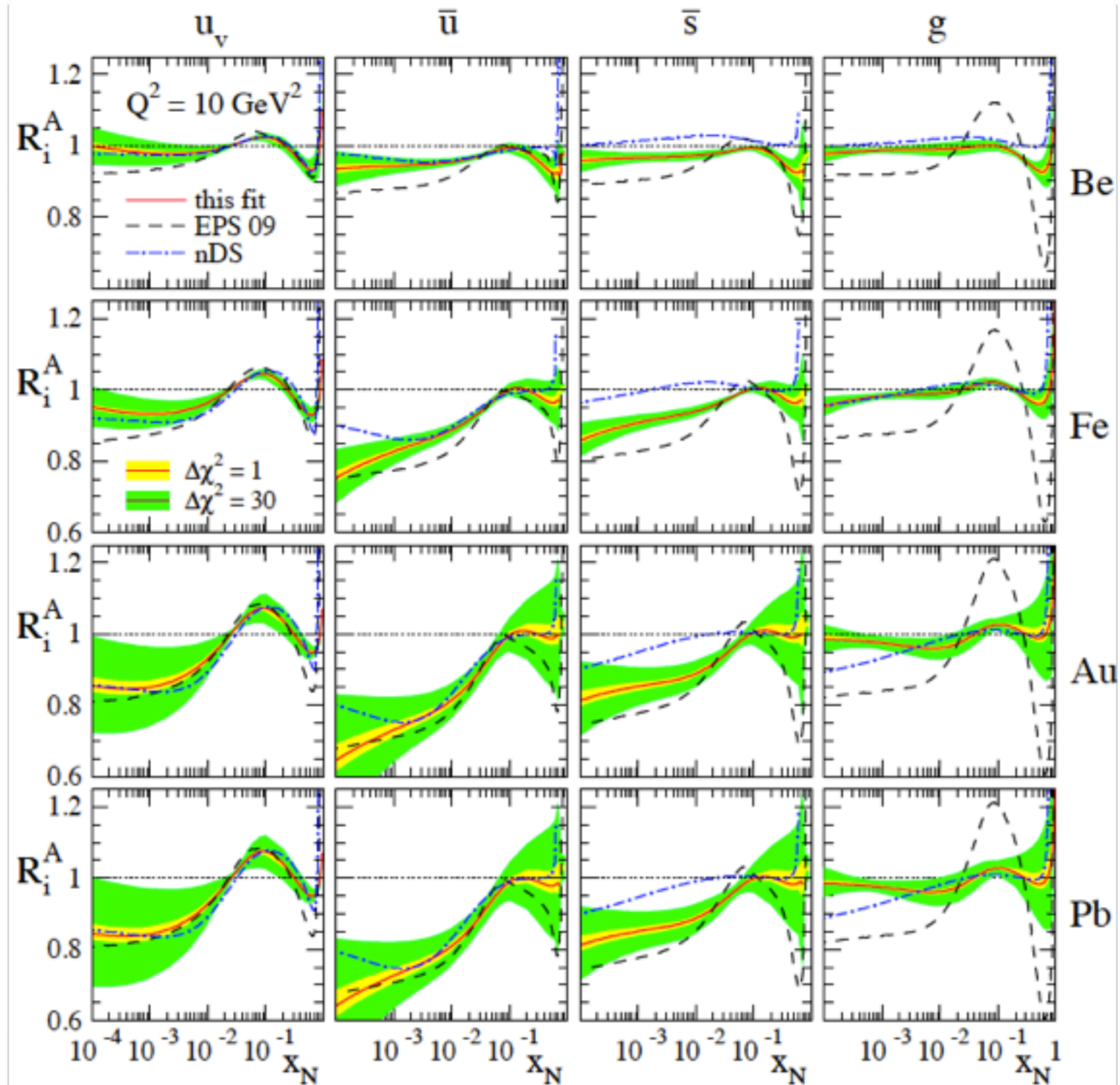
- nuclear modifications quickly diminish under evolution
- evolution imprints different nuclear effects on individual quark flavors
recall: we start with $R_u^A = R_d^A = R_s^A$
- $R_{u_v}^A$ exhibits textbook-like behavior
- little evidence for anti-shadowing in sea (and gluon)

evolve to 10 GeV^2



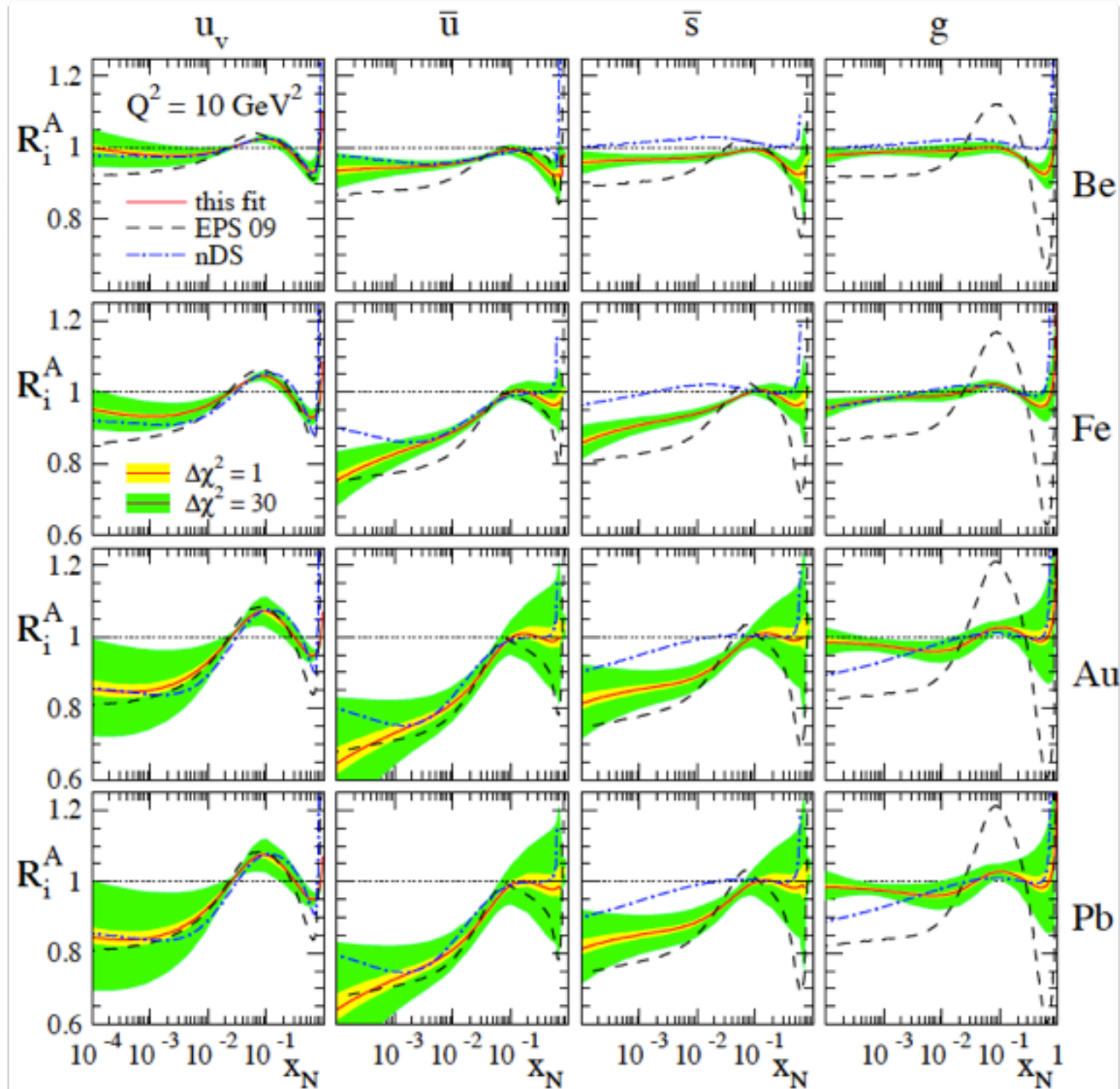
DSSZ nPDFs and their uncertainties

A dependence at $Q^2 = 10 \text{ GeV}^2$



DSSZ nPDFs and their uncertainties

A dependence at $Q^2 = 10 \text{ GeV}^2$

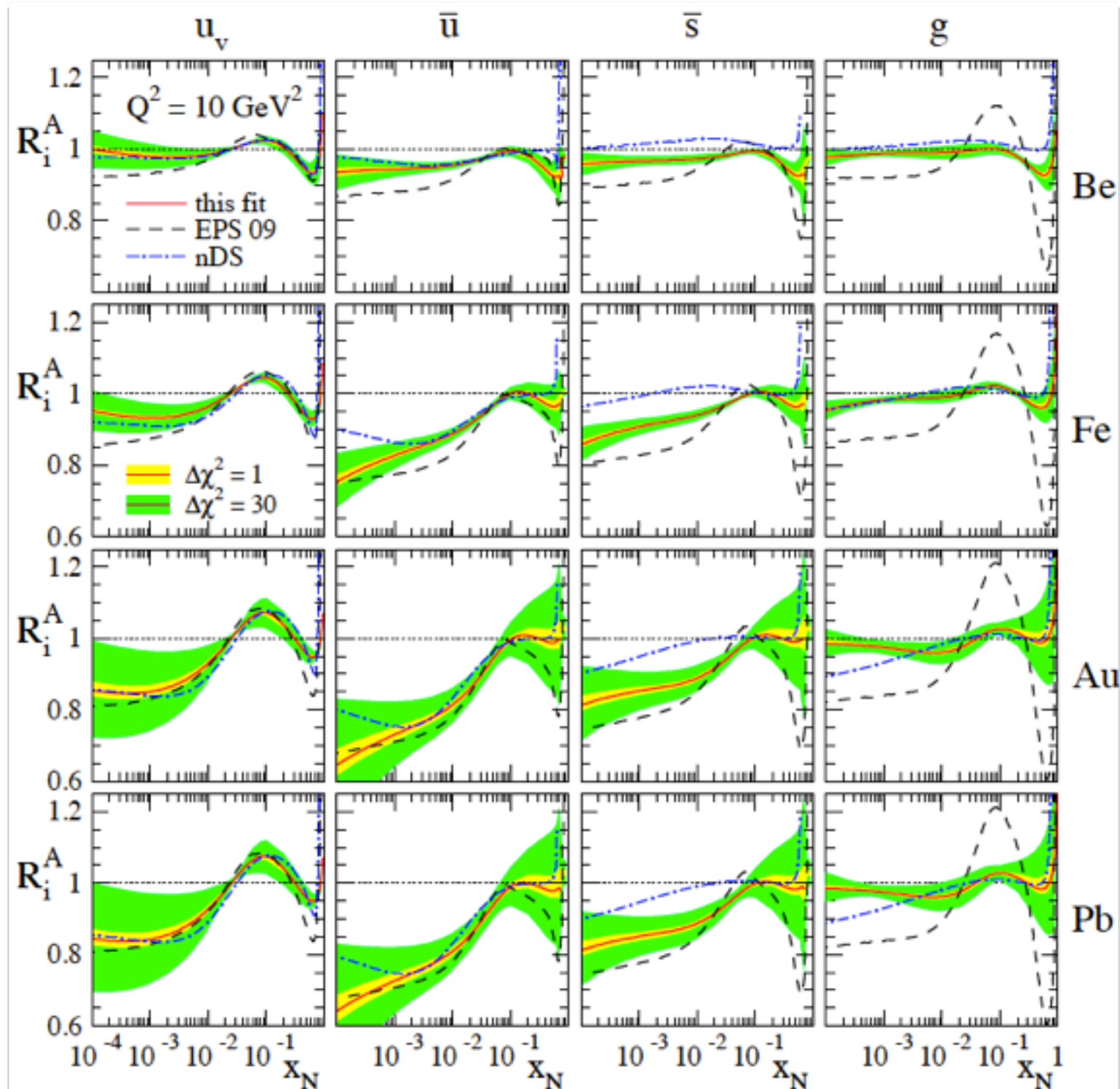


- nuclear modifications increase with A



DSSZ nPDFs and their uncertainties

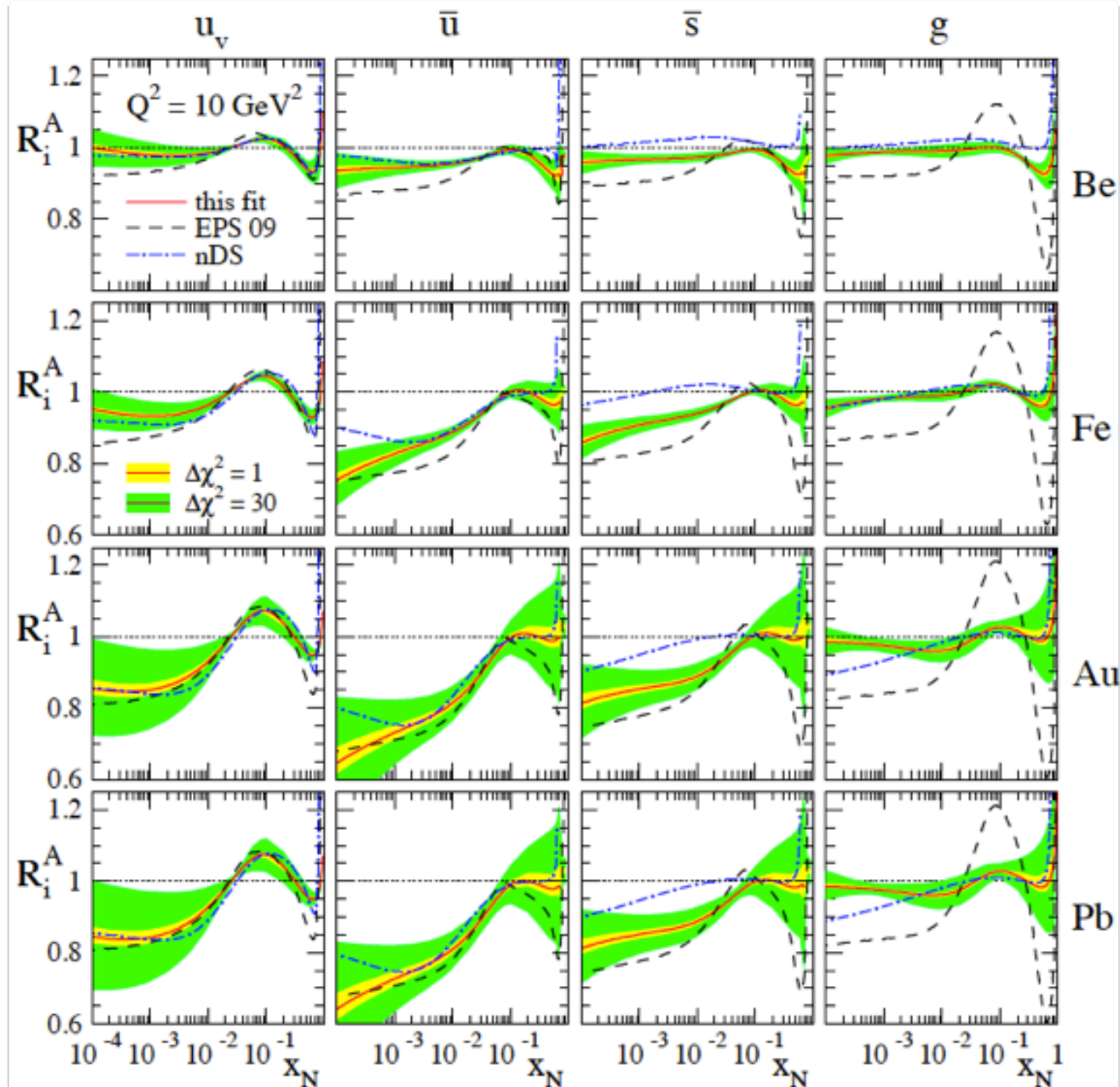
A dependence at $Q^2 = 10 \text{ GeV}^2$



- nuclear modifications increase with A
- good agreement with previous fits for $R_{u_v}^A$ and $R_{\bar{u}}^A$

DSSZ nPDFs and their uncertainties

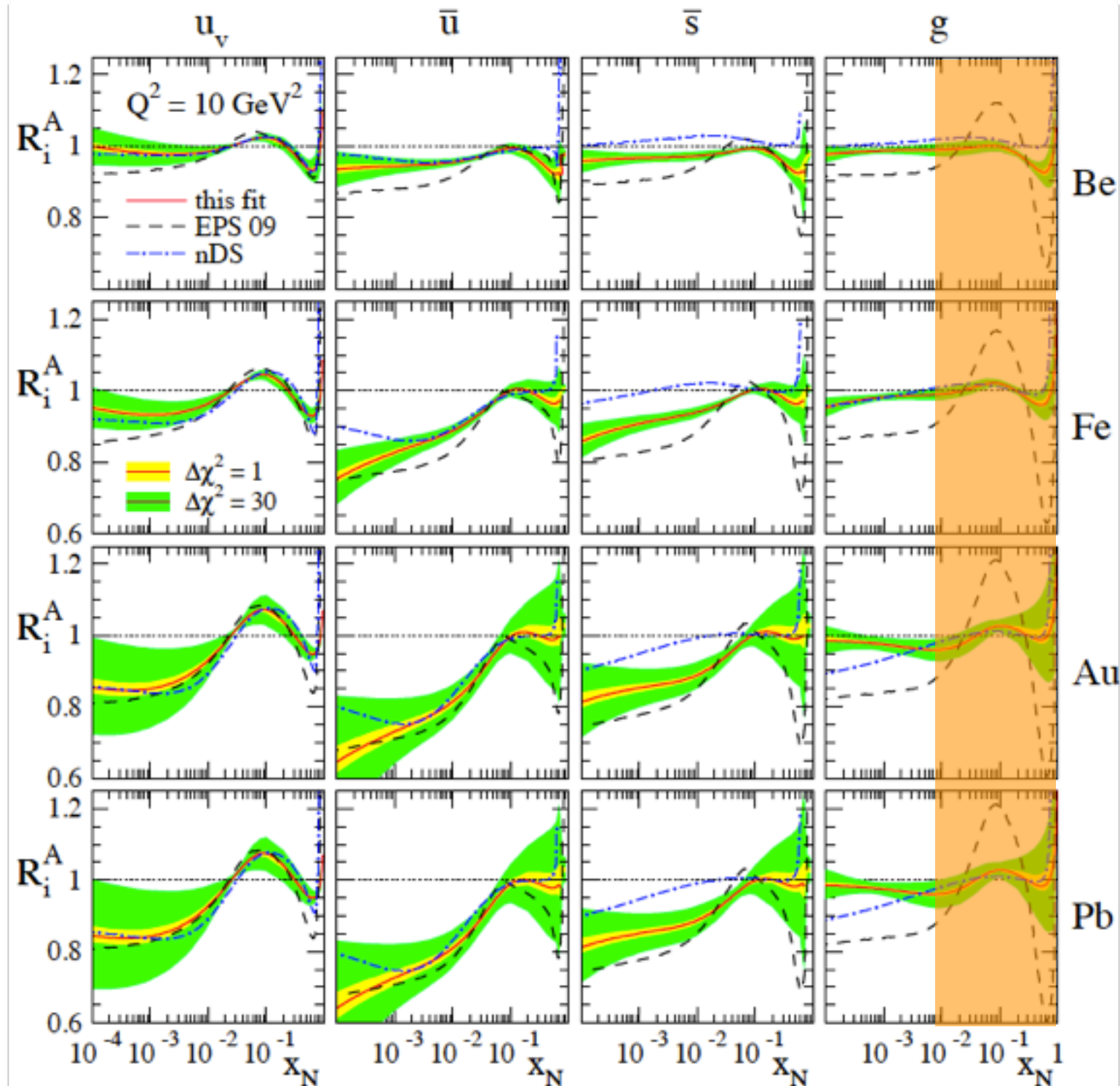
A dependence at $Q^2 = 10 \text{ GeV}^2$



- nuclear modifications increase with A
- good agreement with previous fits for $R_{u_v}^A$ and $R_{\bar{u}}^A$
- less so for $R_{\bar{s}}^A$ due to recent changes in free proton PDFs

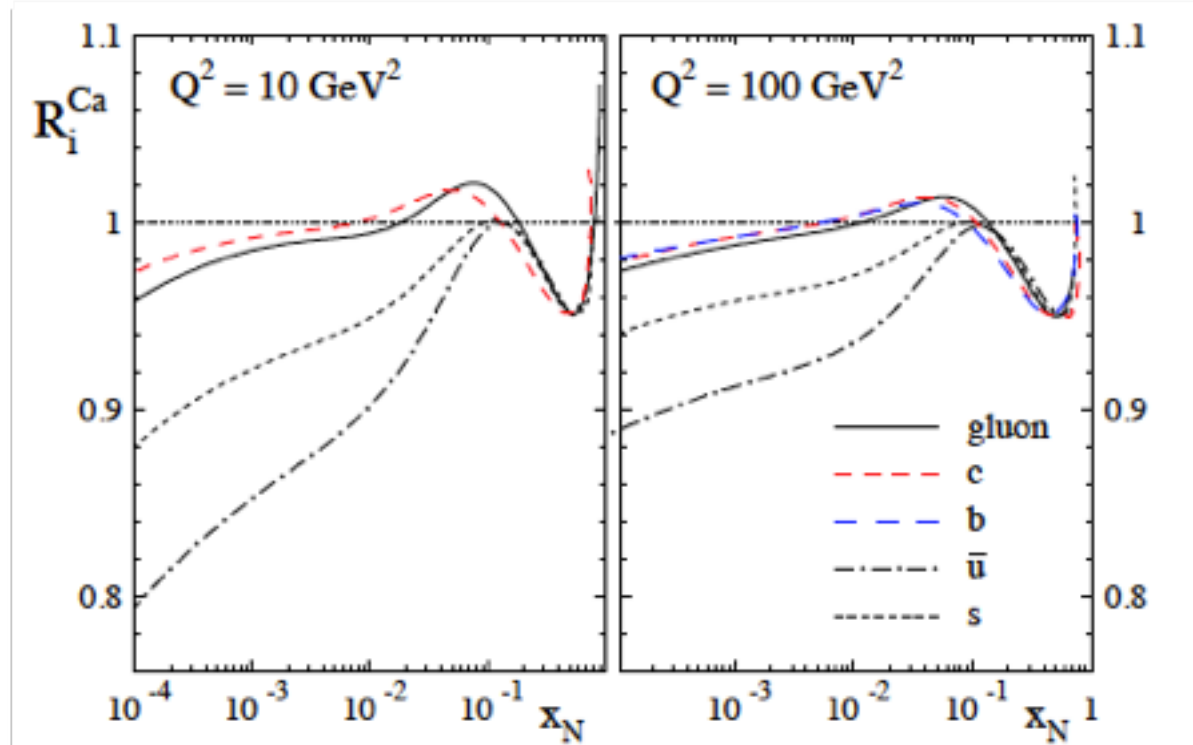
DSSZ nPDFs and their uncertainties

A dependence at $Q^2 = 10 \text{ GeV}^2$



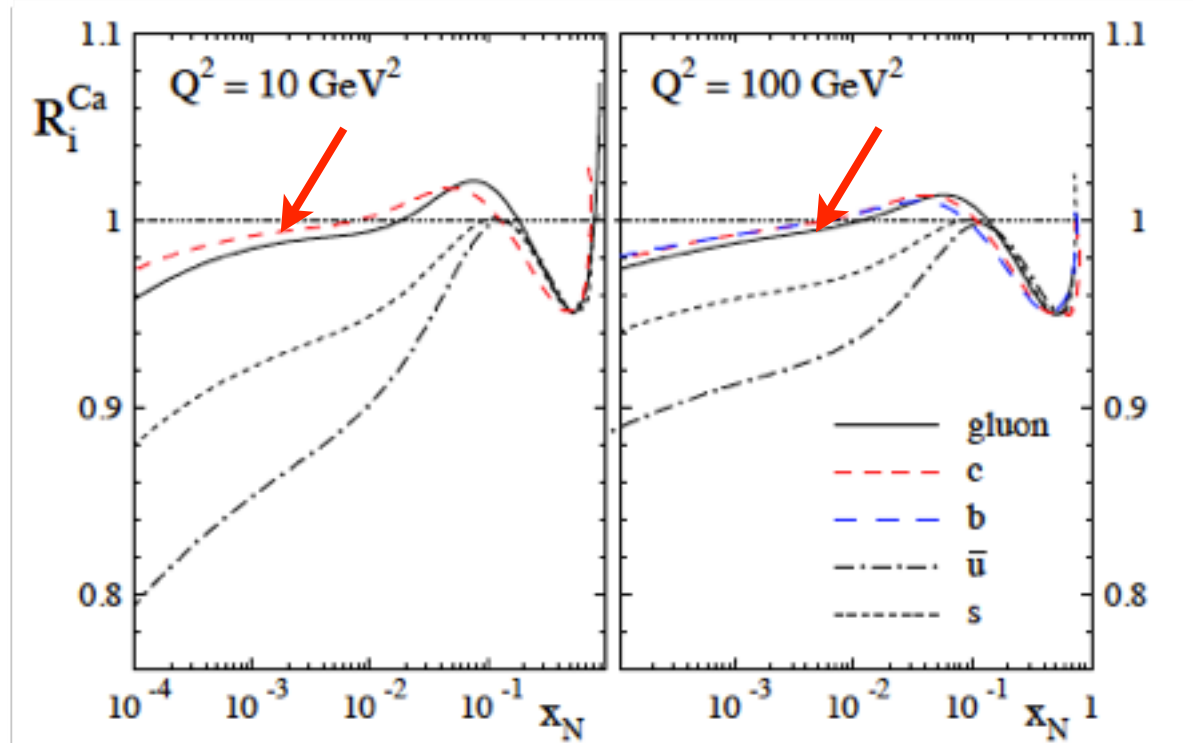
- nuclear modifications increase with A
- good agreement with previous fits for $R_{u_v}^A$ and $R_{\bar{u}}^A$
- less so for $R_{\bar{s}}^A$ due to recent changes in free proton PDFs
- **MUCH less anti-shadowing and EMC effect than for EPS gluon** driven by the way dAu data are analyzed

DSSZ nPDFs: peculiarities



perturbatively generated charm and bottom nPDFs

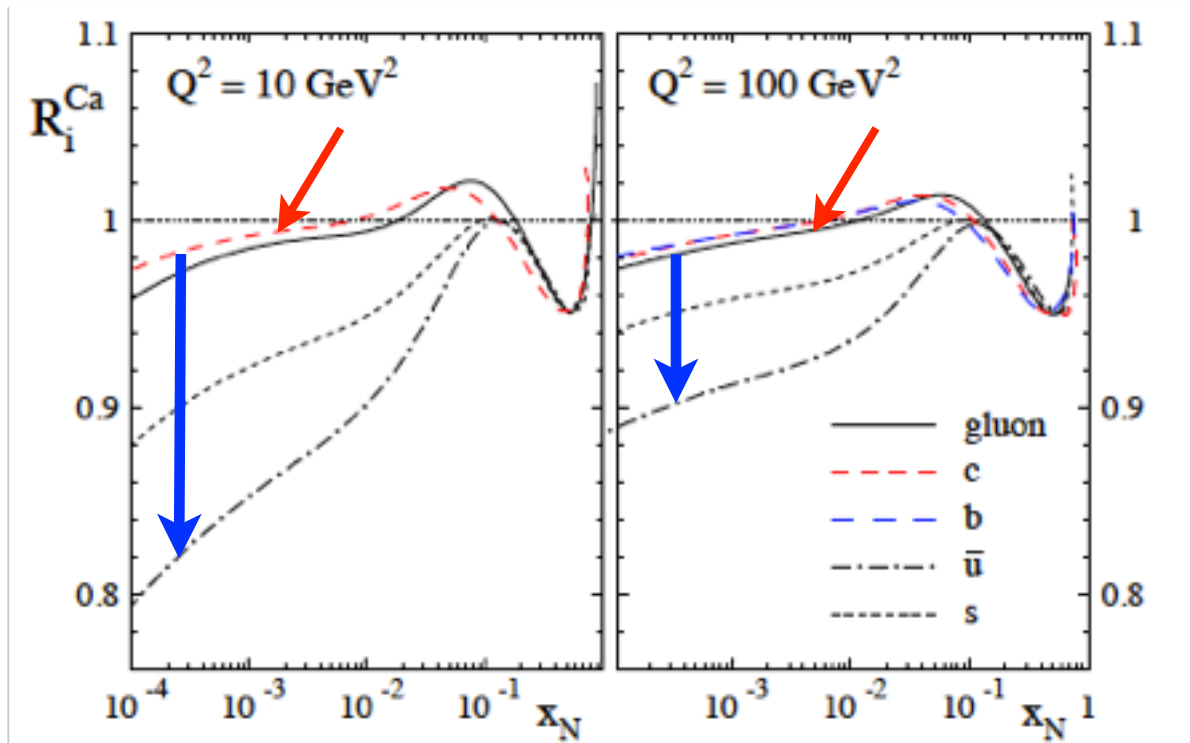
DSSZ nPDFs: peculiarities



perturbatively generated charm and bottom nPDFs

- modifications for c,b follow closely the gluon
no surprise, as they are generated from gluon splitting

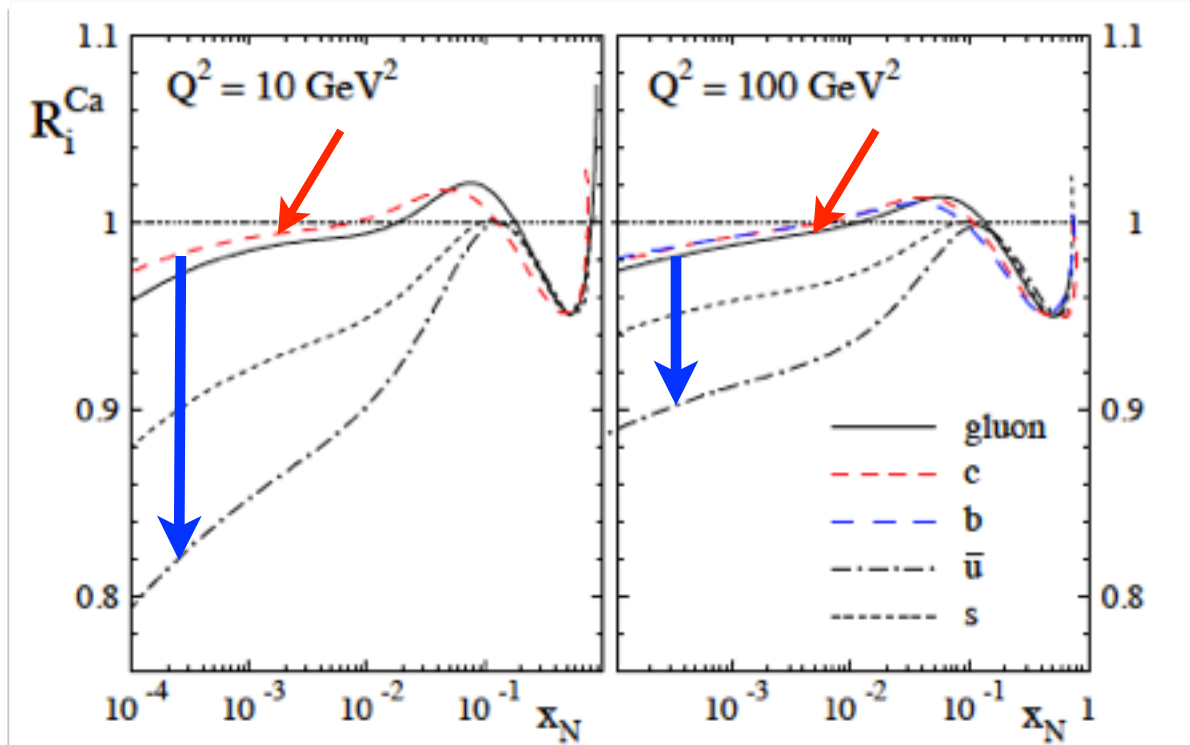
DSSZ nPDFs: peculiarities



perturbatively generated charm and bottom nPDFs

- modifications for c,b follow closely the gluon
no surprise, as they are generated from gluon splitting
- hierarchy in amount of low- x suppression:
the stronger, the lighter the quark

DSSZ nPDFs: peculiarities

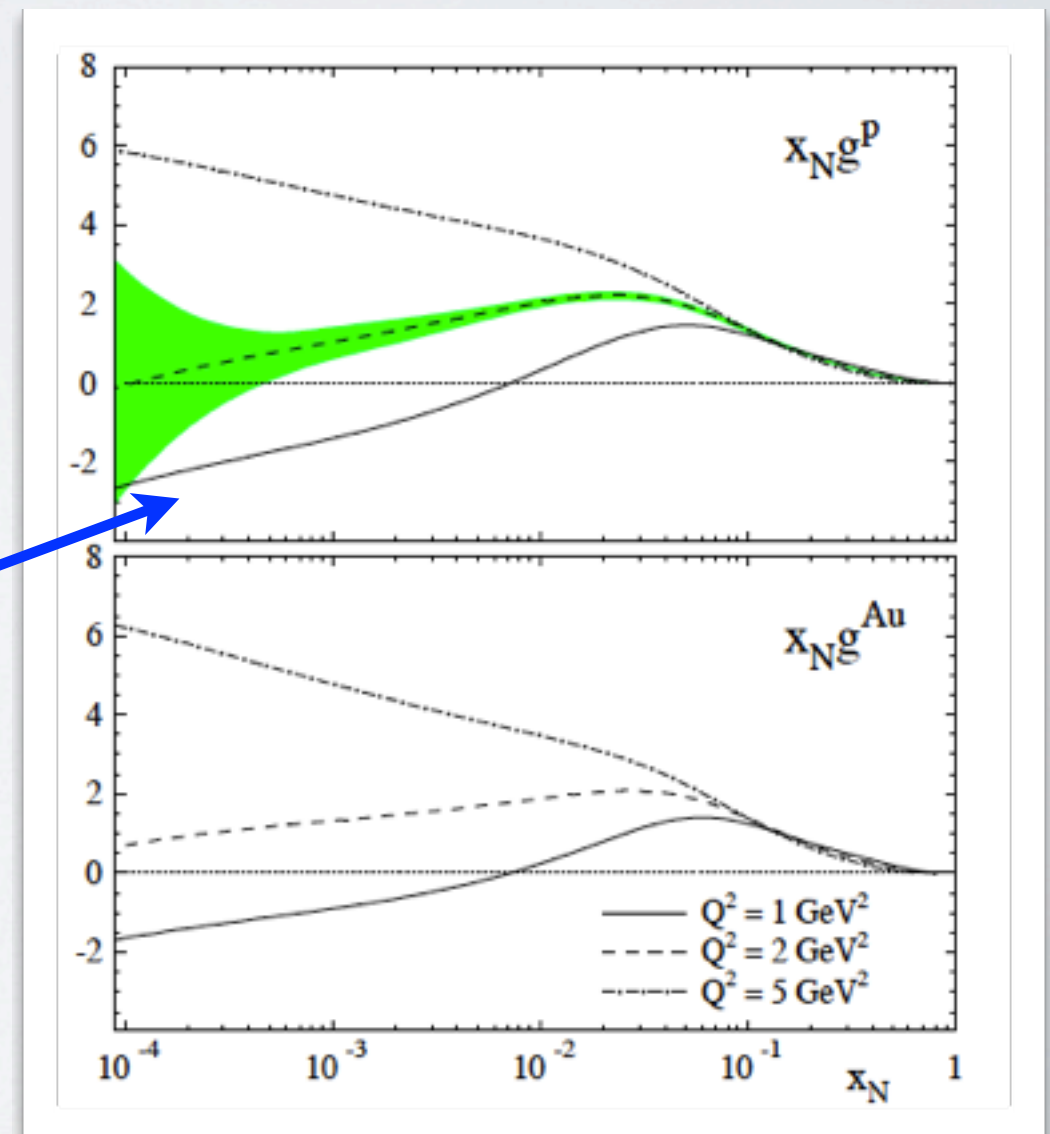


perturbatively generated charm and bottom nPDFs

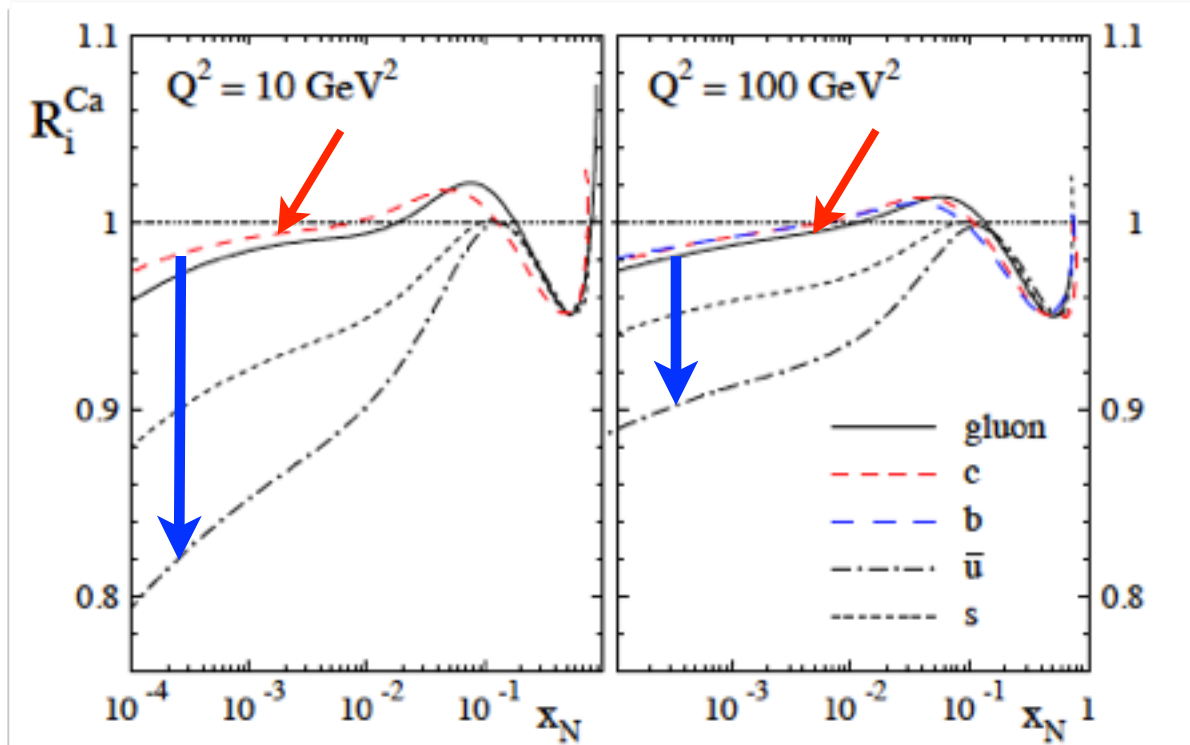
- modifications for c,b follow closely the gluon no surprise, as they are generated from gluon splitting
- hierarchy in amount of low- x suppression: the stronger, the lighter the quark

the issue of “negative gluons”

- MSTW exercises the possibility of **negative gluons** at small x and low scales [improves their fit of HERA data]
not a problem since PDFs are not observables but F_L should stay positive



DSSZ nPDFs: peculiarities

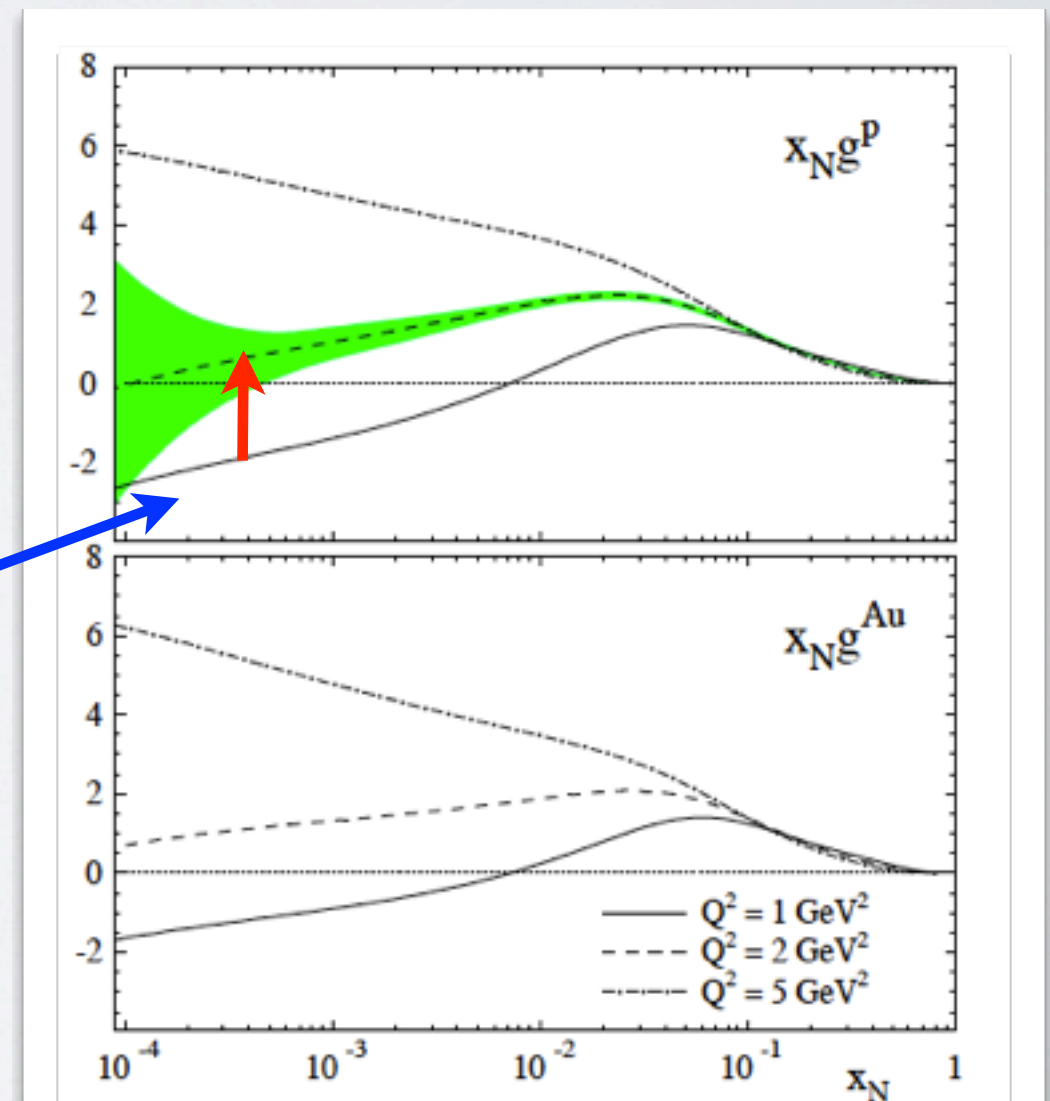


perturbatively generated charm and bottom nPDFs

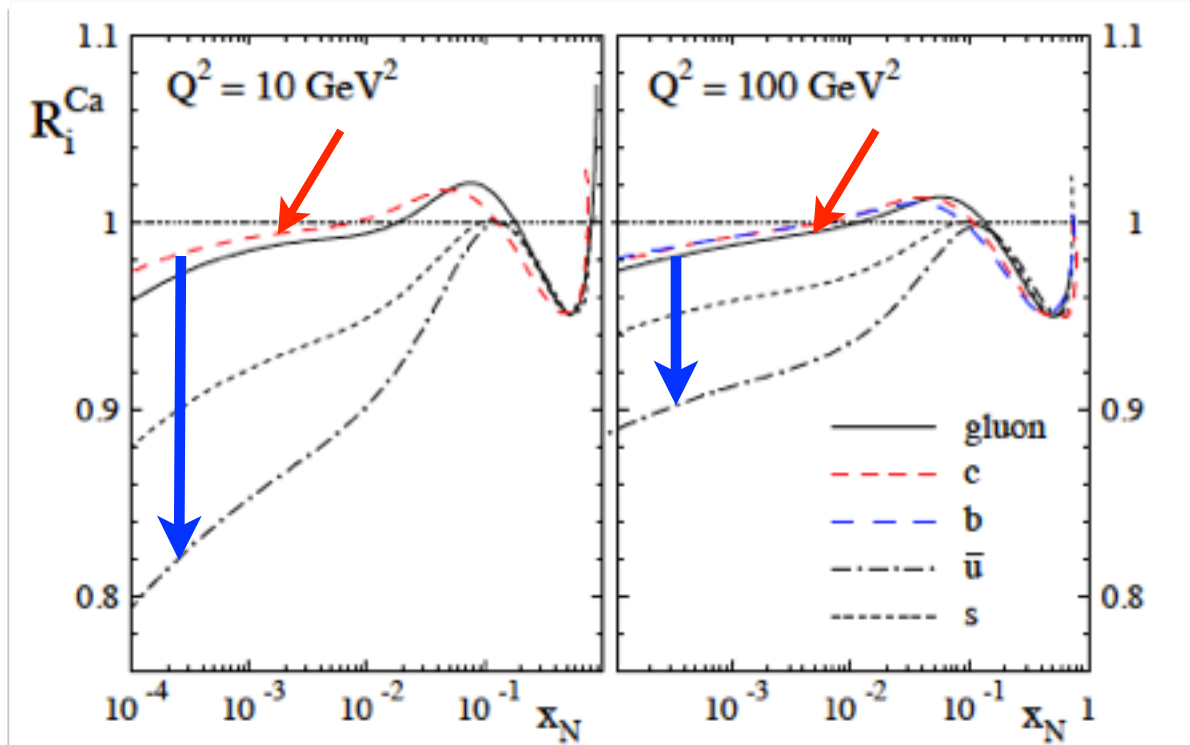
- modifications for c,b follow closely the gluon no surprise, as they are generated from gluon splitting
- hierarchy in amount of low-x suppression: the stronger, the lighter the quark

the issue of “negative gluons”

- MSTW exercises the possibility of **negative gluons** at small x and low scales [improves their fit of HERA data]
 not a problem since PDFs are not observables but F_L should stay positive
- evolution quickly pushes the gluon up



DSSZ nPDFs: peculiarities

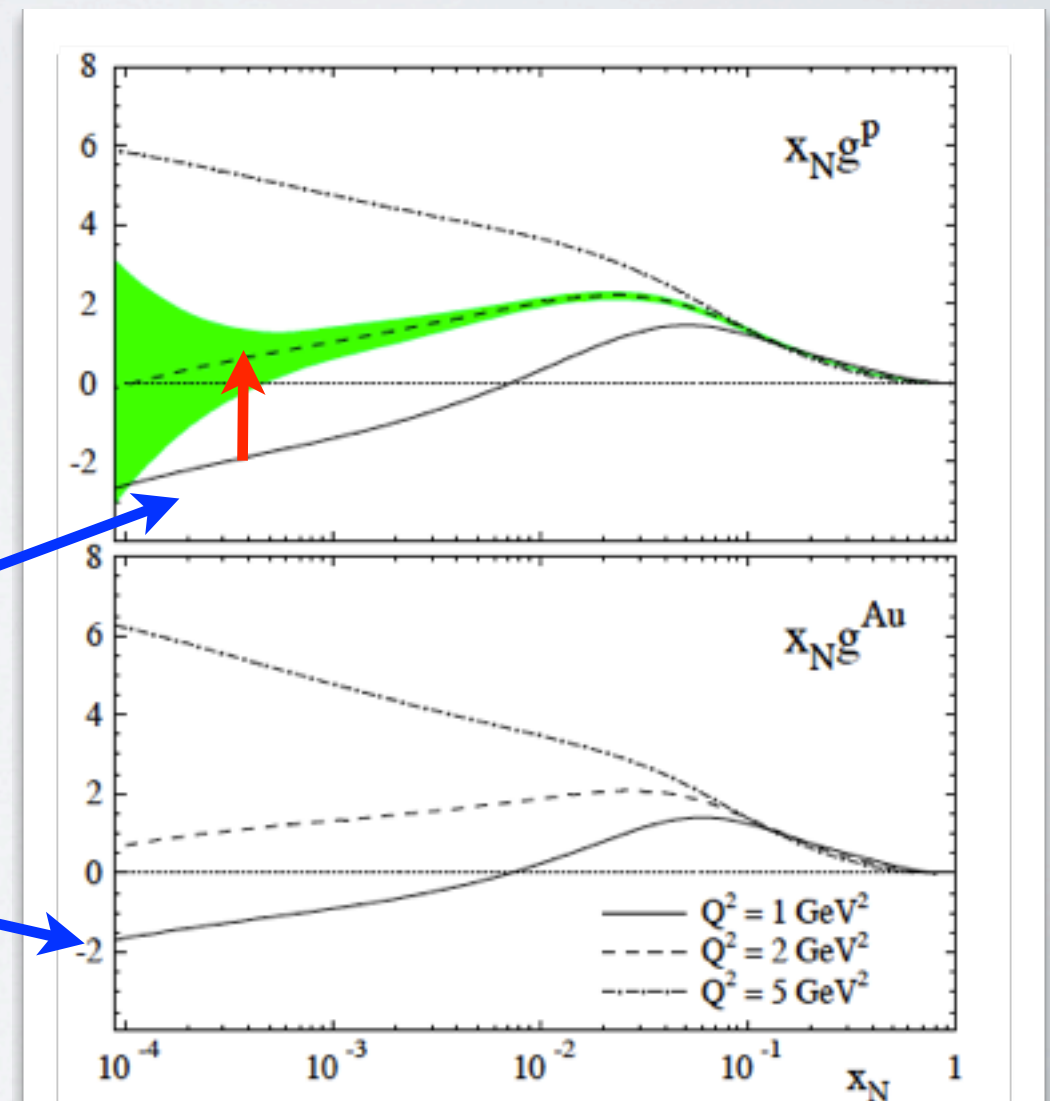


perturbatively generated charm and bottom nPDFs

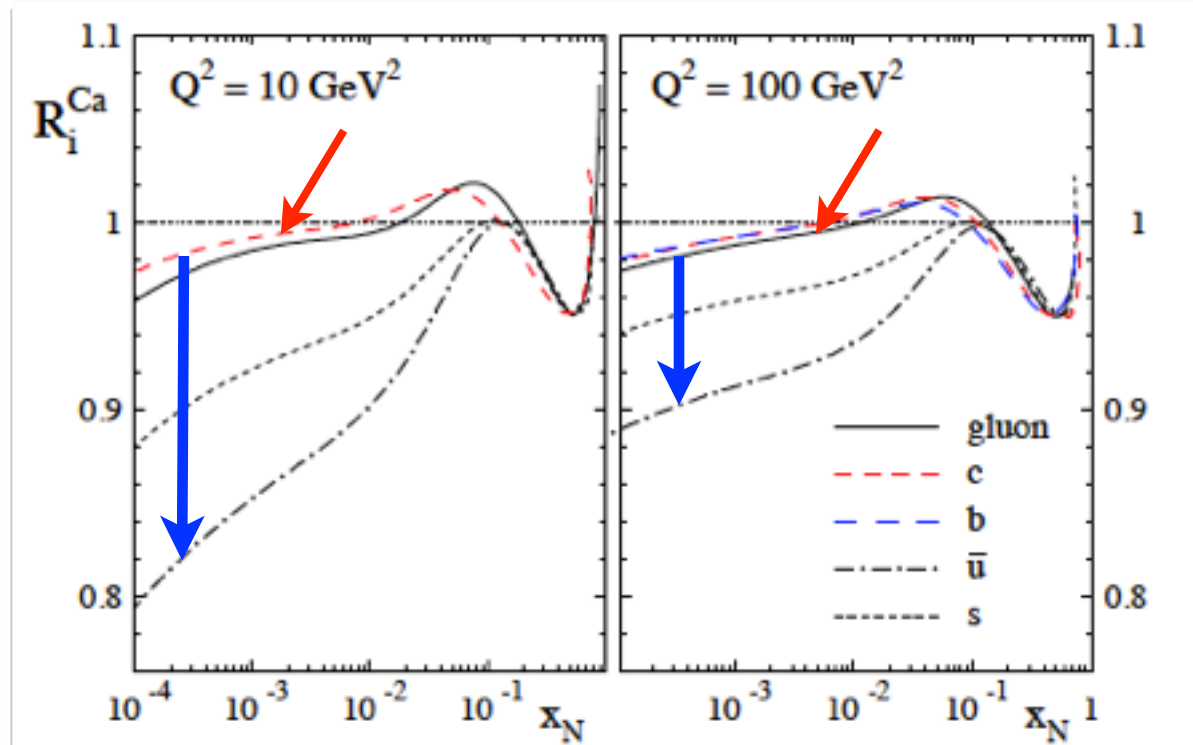
- modifications for c,b follow closely the gluon
no surprise, as they are generated from gluon splitting
- hierarchy in amount of low-x suppression:
the stronger, the lighter the quark

the issue of “negative gluons”

- MSTW exercises the possibility of **negative gluons**
at small x and low scales [improves their fit of HERA data]
not a problem since PDFs are not observables but F_L should stay positive
- evolution quickly pushes the gluon up
- our nPDF gluon is tied to the MSTW through R_g^A
and gets negative too $\rightarrow R_g^A$ ill defined at low scales (nodes)



DSSZ nPDFs: peculiarities



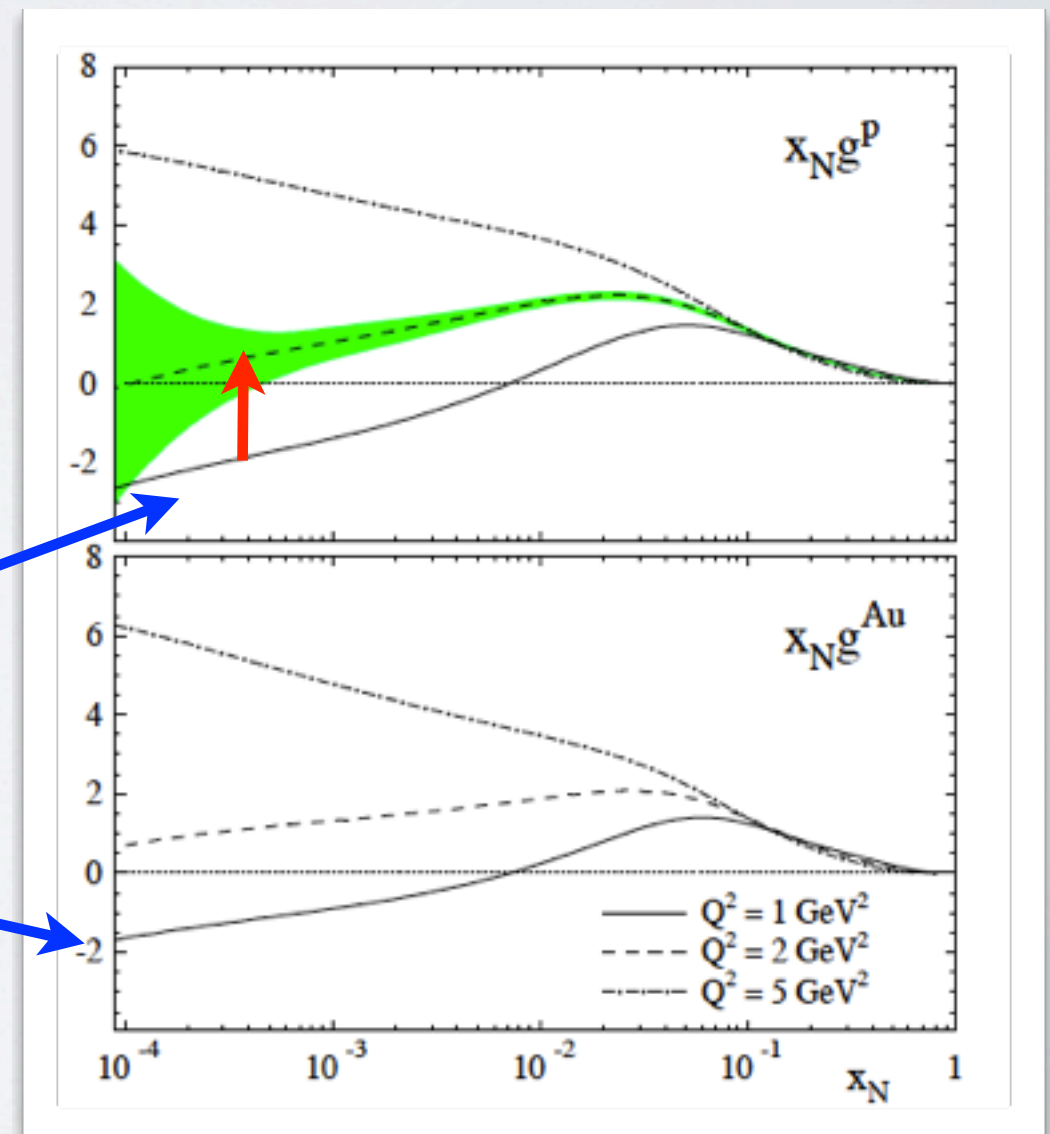
perturbatively generated charm and bottom nPDFs

- modifications for c,b follow closely the gluon no surprise, as they are generated from gluon splitting
- hierarchy in amount of low-x suppression: the stronger, the lighter the quark

the issue of “negative gluons”

- MSTW exercises the possibility of **negative gluons** at small x and low scales [improves their fit of HERA data]
not a problem since PDFs are not observables but F_L should stay positive
- evolution quickly pushes the gluon up
- our nPDF gluon is tied to the MSTW through R_g^A and gets negative too $\rightarrow R_g^A$ ill defined at low scales (nodes)

one must take trad. ratios R_i^A with a pinch of salt in NLO





**some future avenues for nPDF fits
RHIC & LHC**

prompt photons in dAu / pPb

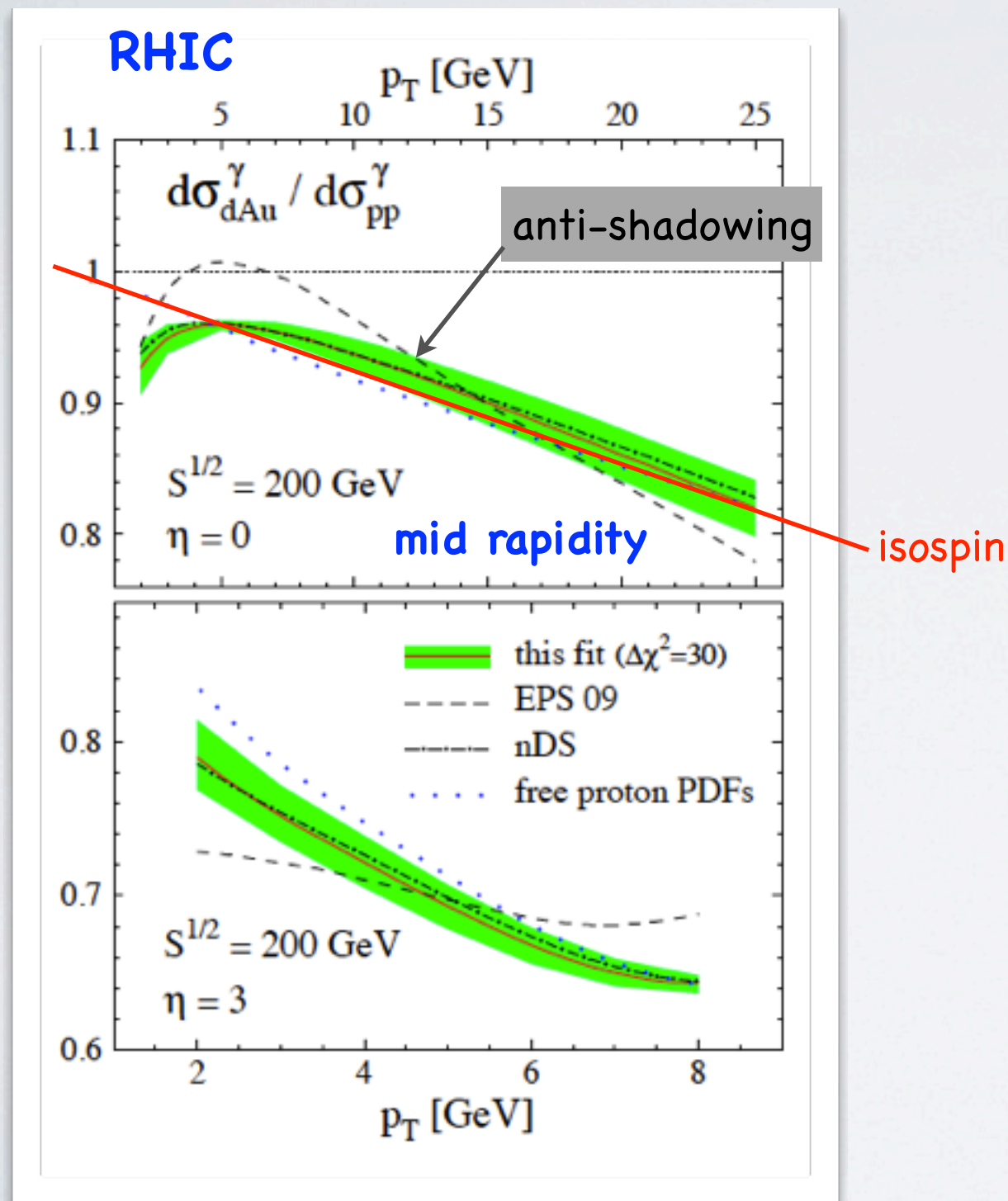
complication: “isospin effects” = dilution of u-quark density from neutrons $u^A(x) < u^P(x)$

→ ratio dAu/pp not unity even w/o nuclear modifications

prompt photons in dAu / pPb

complication: "isospin effects" = dilution of u-quark density from neutrons $u^A(x) < u^P(x)$

→ ratio dAu/pp not unity even w/o nuclear modifications

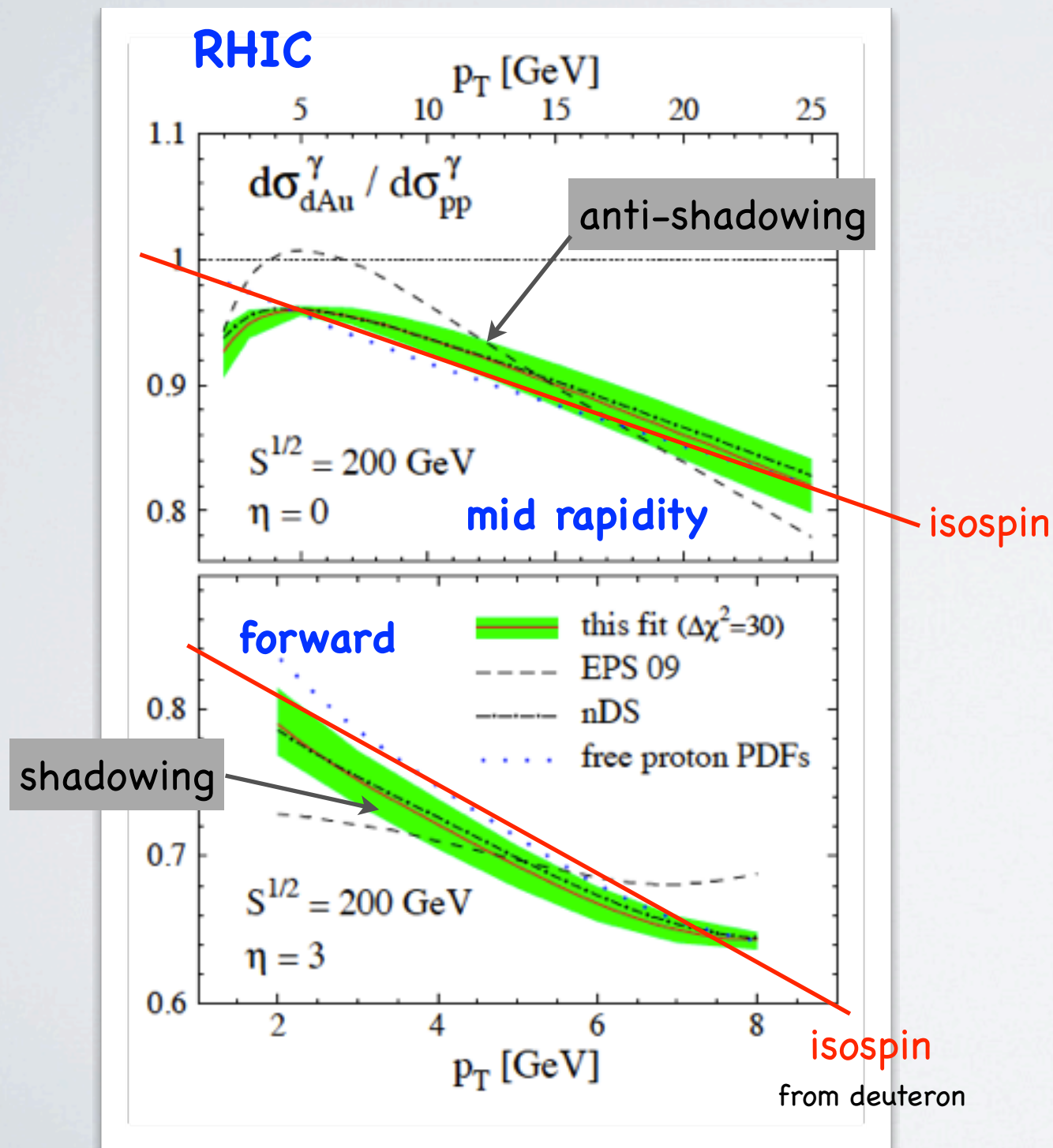


prompt photons in dAu / pPb

complication: "isospin effects" = dilution of u-quark density from neutrons $u^A(x) < u^P(x)$

→ ratio dAu/pp not unity even w/o nuclear modifications

RHIC

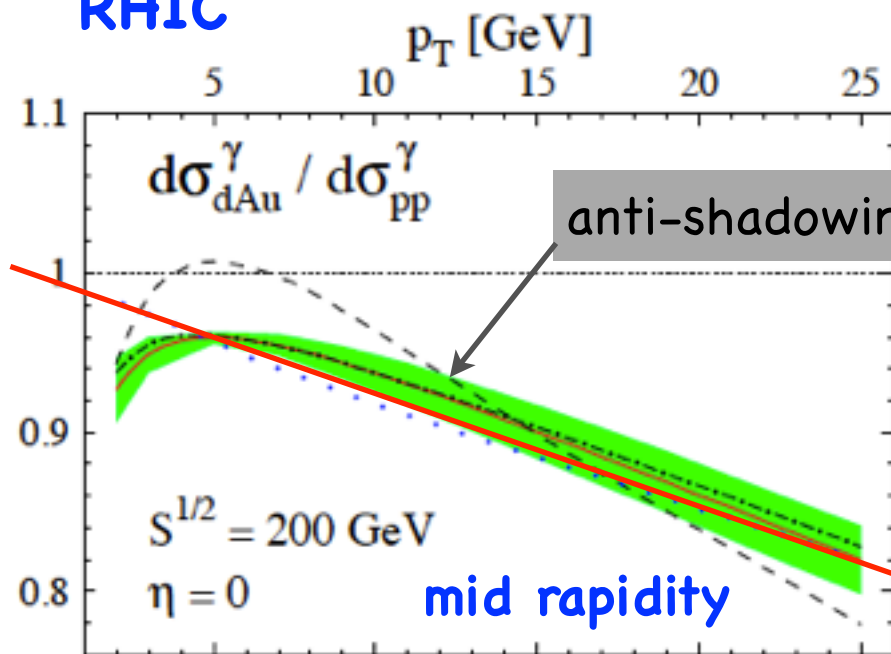


prompt photons in dAu / pPb

complication: "isospin effects" = dilution of u-quark density from neutrons $u^A(x) < u^P(x)$

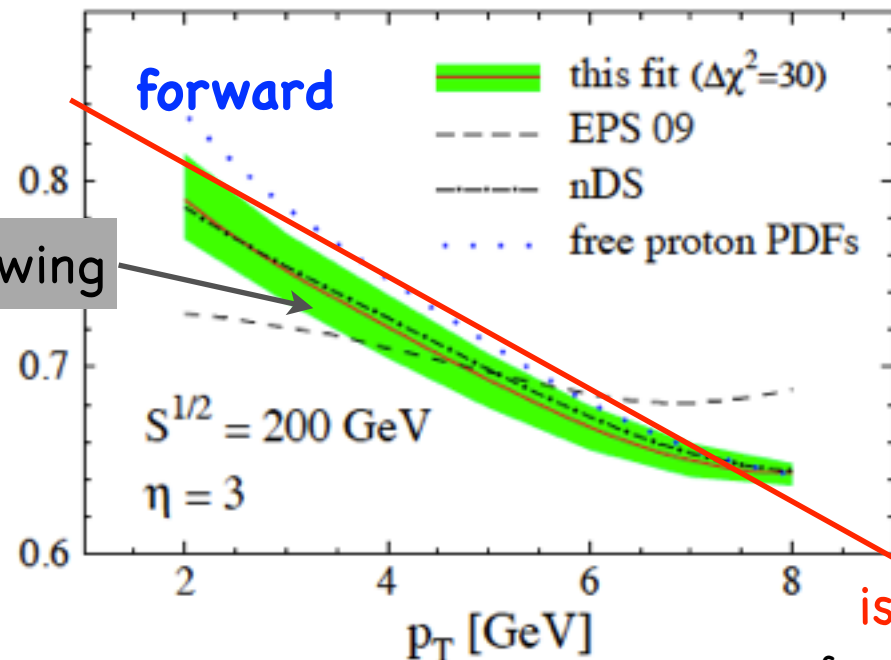
→ ratio dAu/pp not unity even w/o nuclear modifications

RHIC



forward

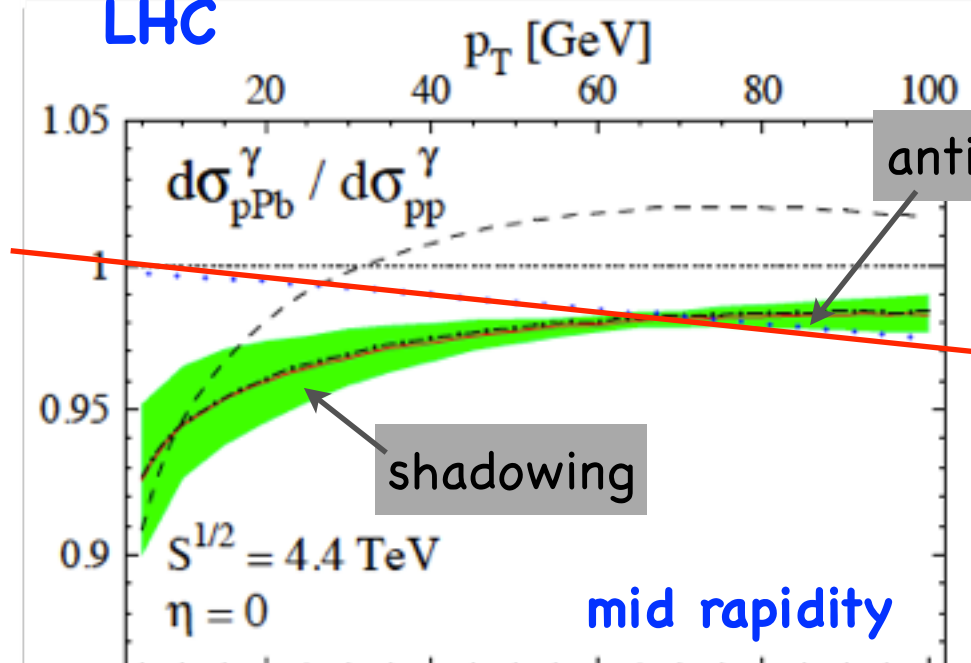
shadowing



isospin

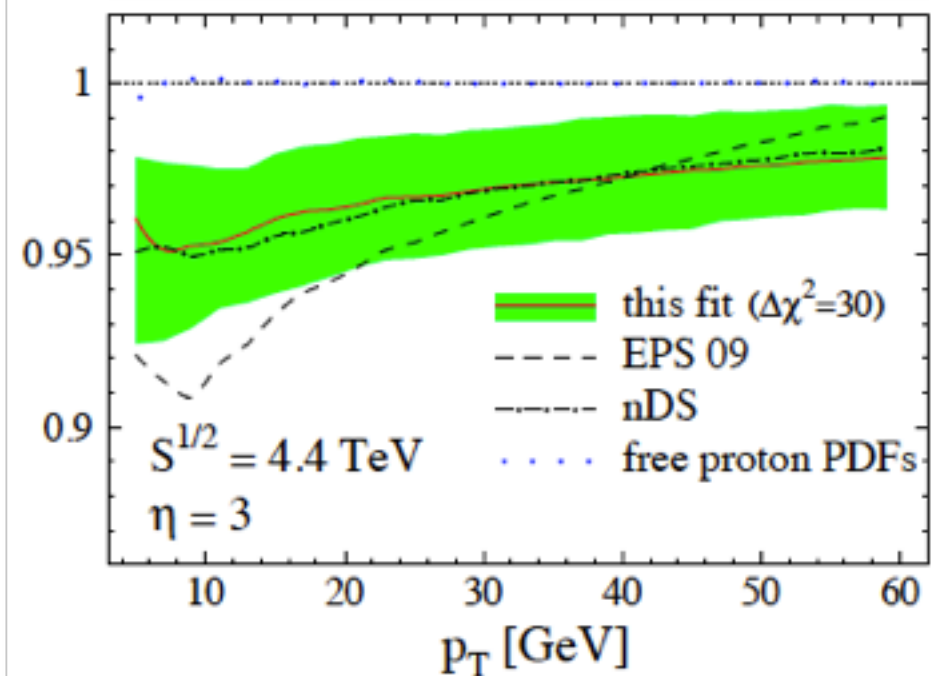
from deuteron

LHC



shadowing

isospin

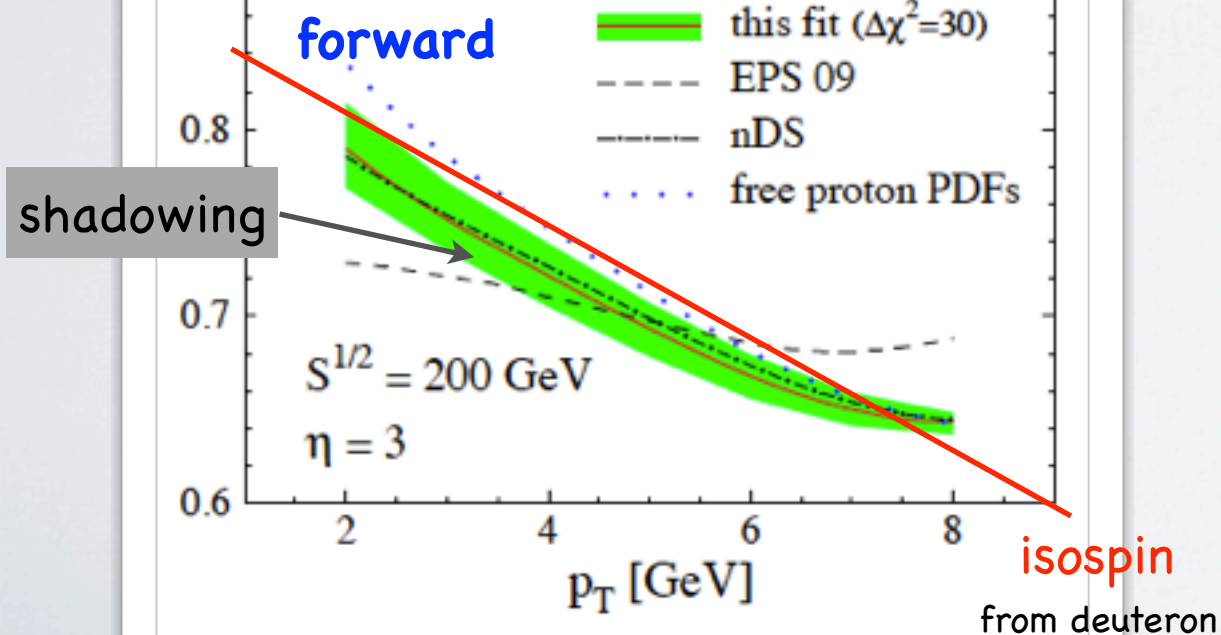
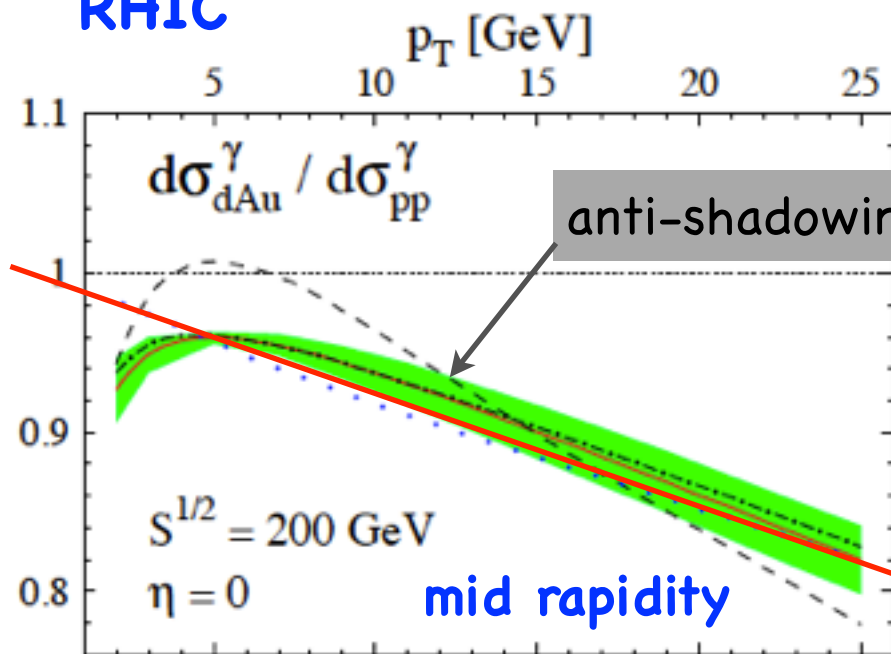


prompt photons in dAu / pPb

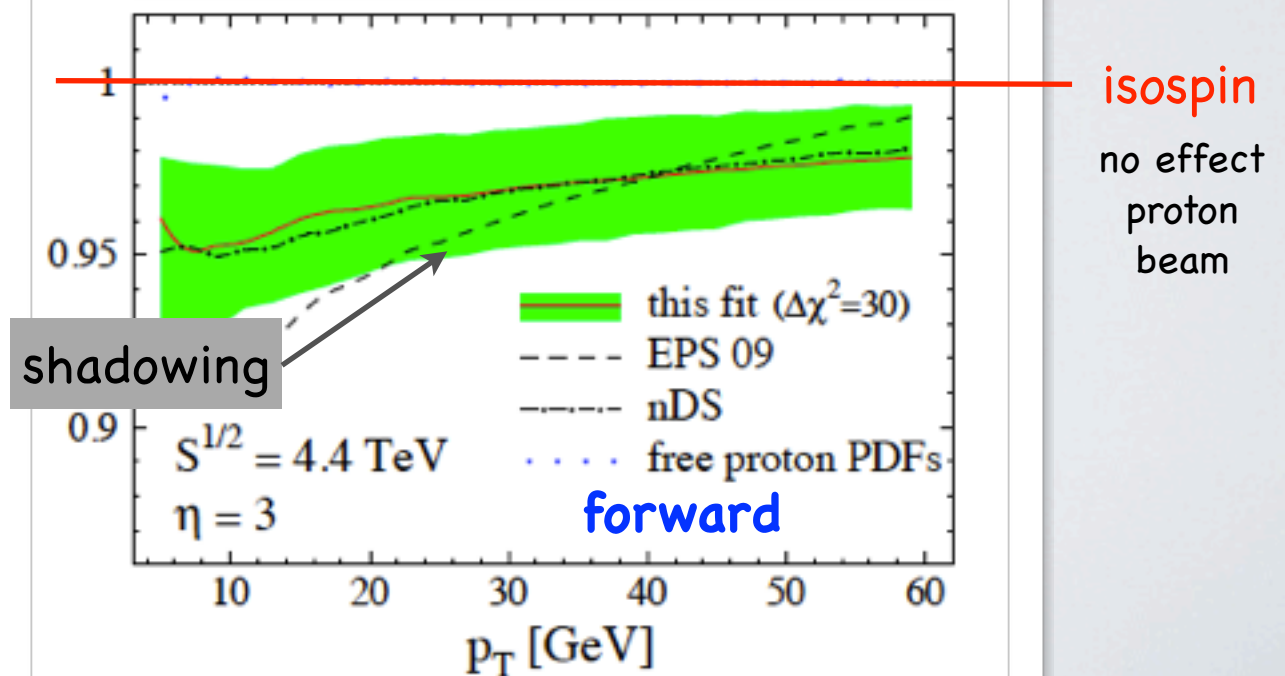
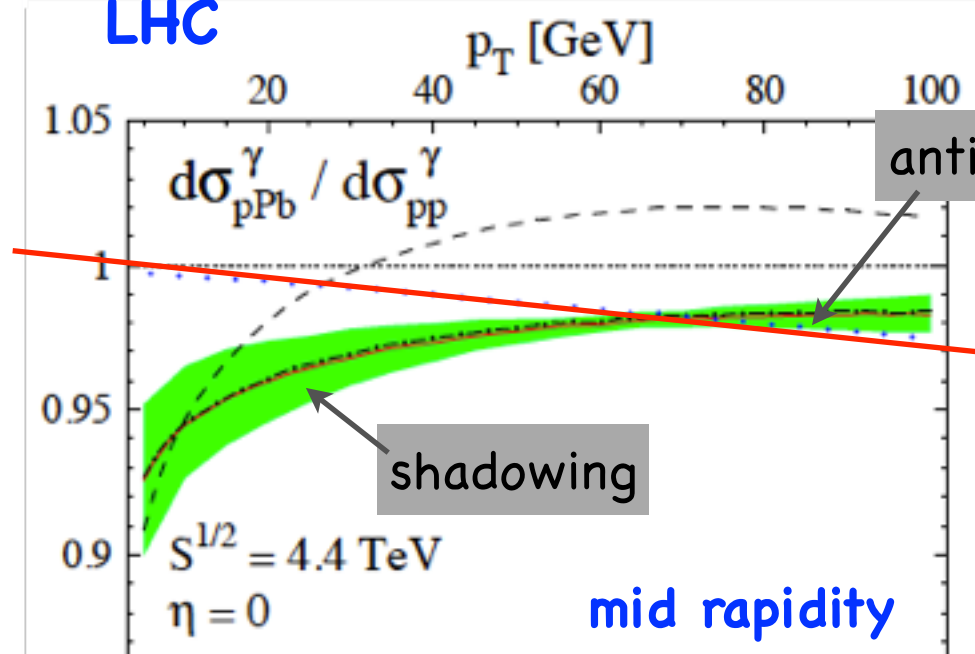
complication: "isospin effects" = dilution of u-quark density from neutrons $u^A(x) < u^P(x)$

→ ratio dAu/pp not unity even w/o nuclear modifications

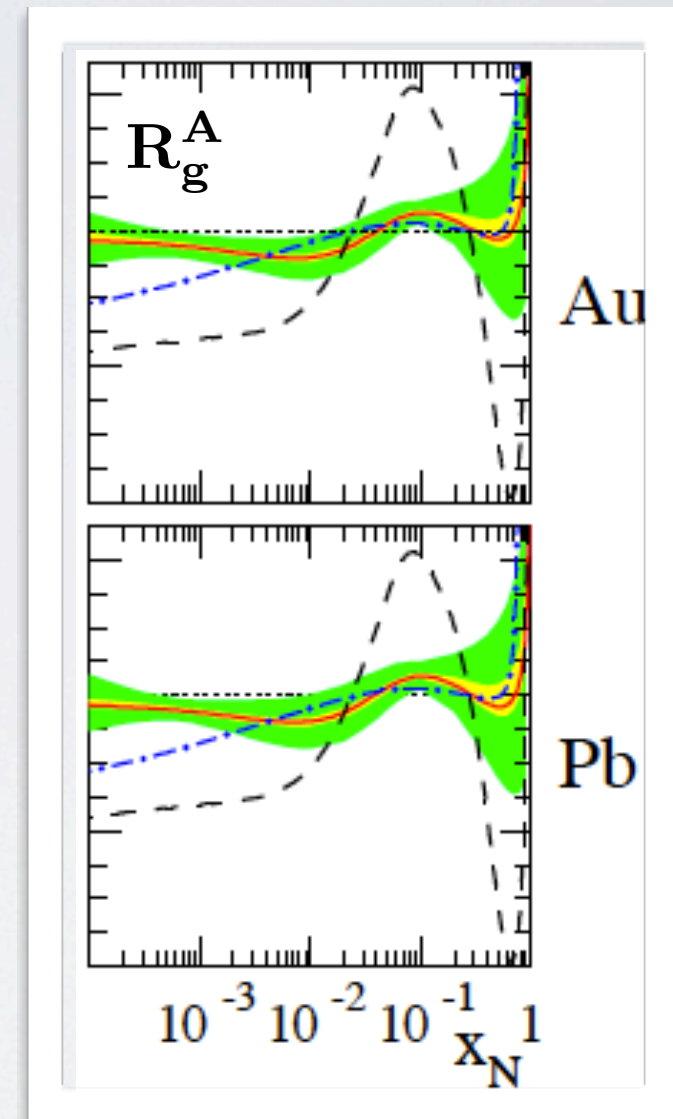
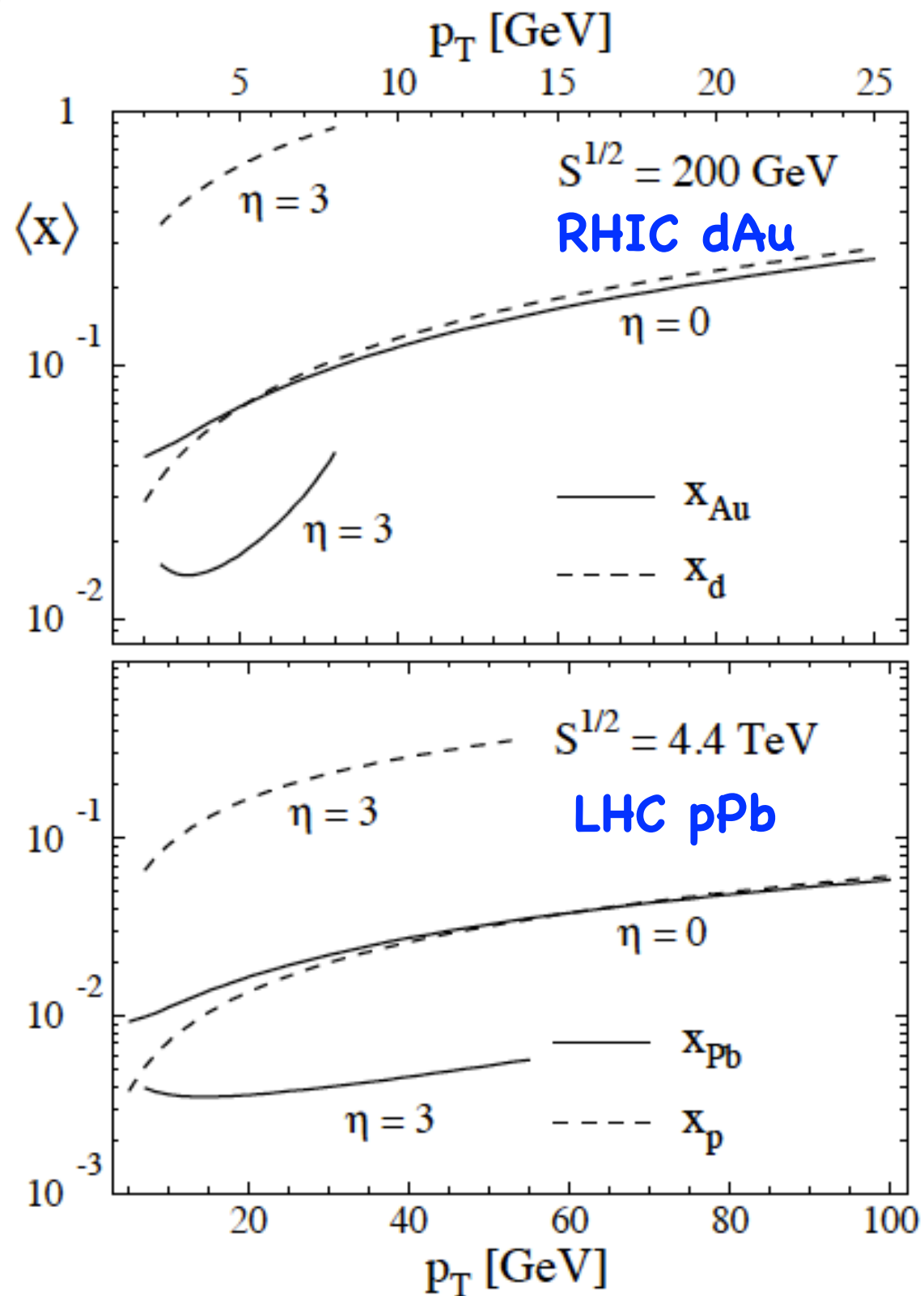
RHIC



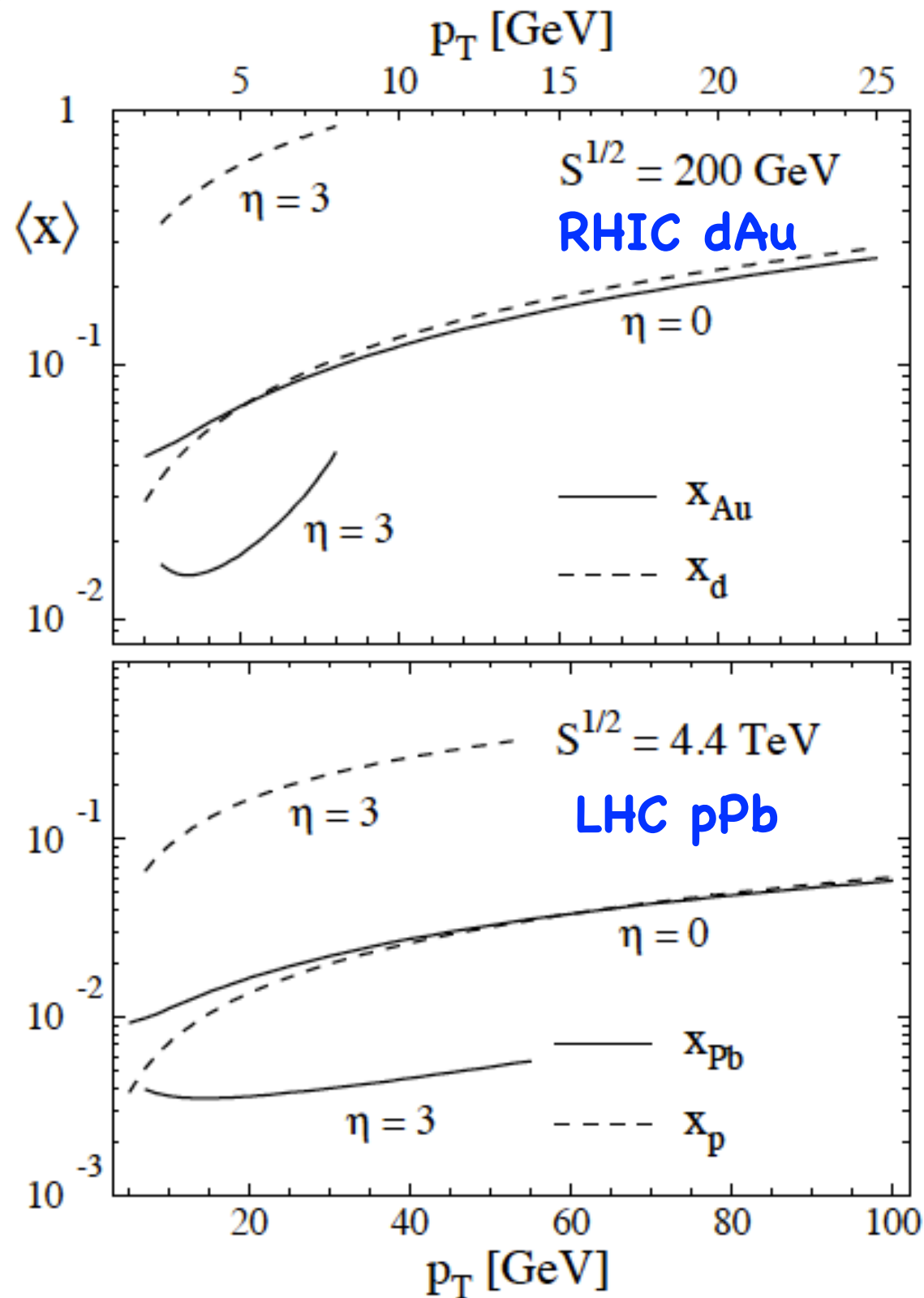
LHC



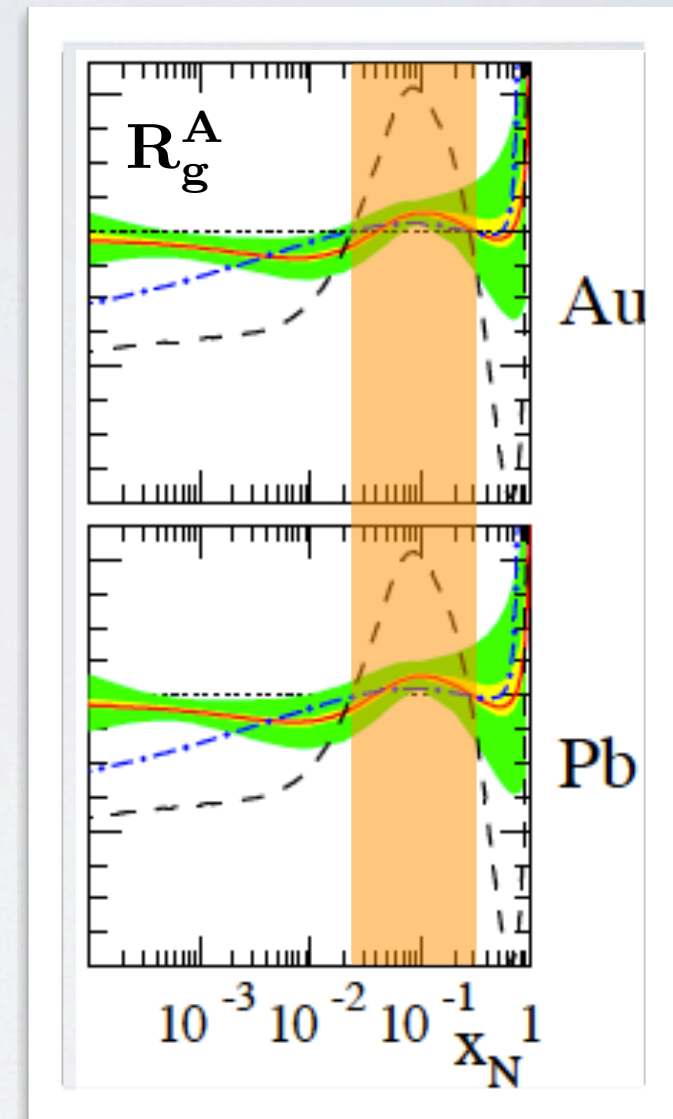
prompt photons – impact



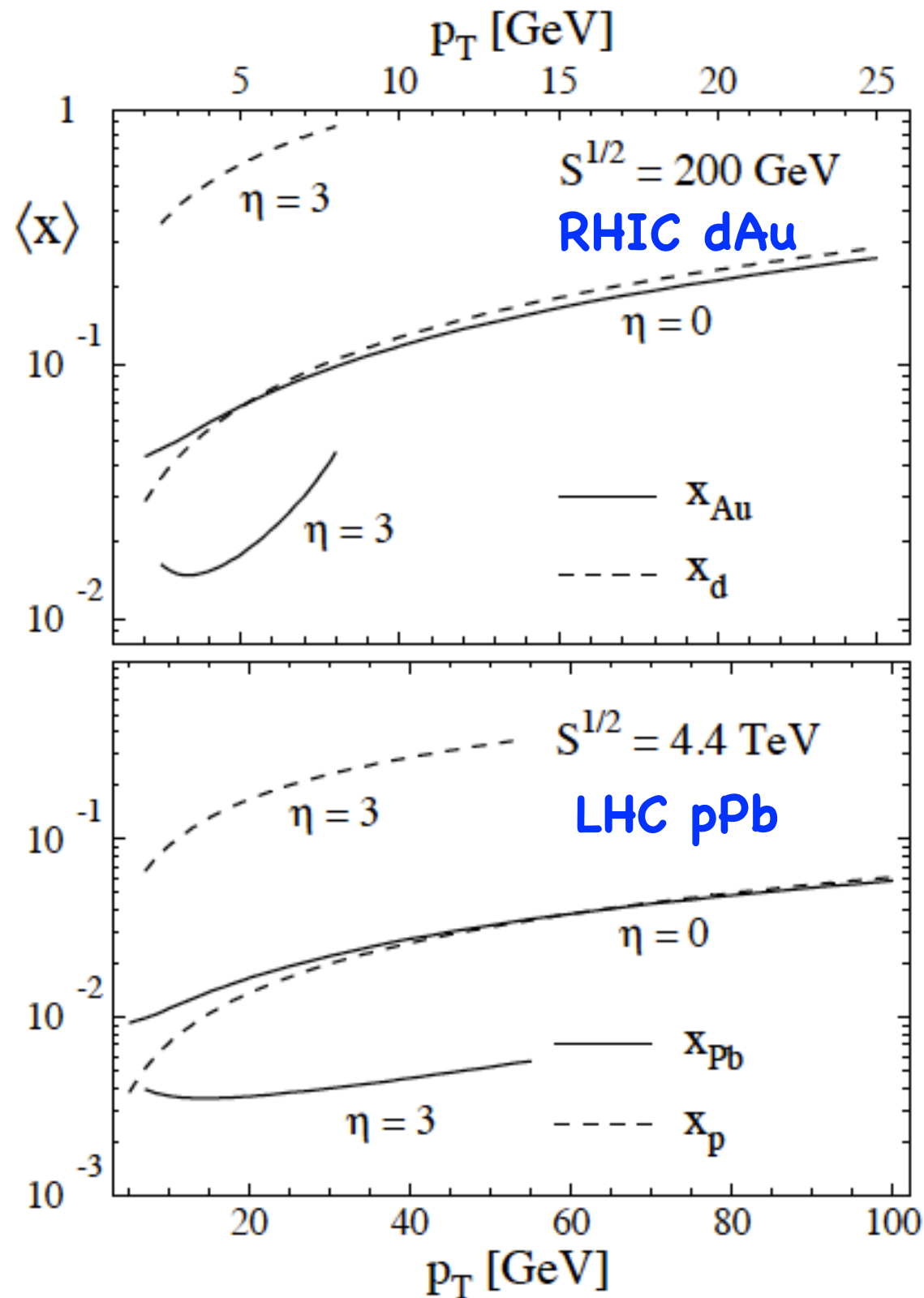
prompt photons – impact



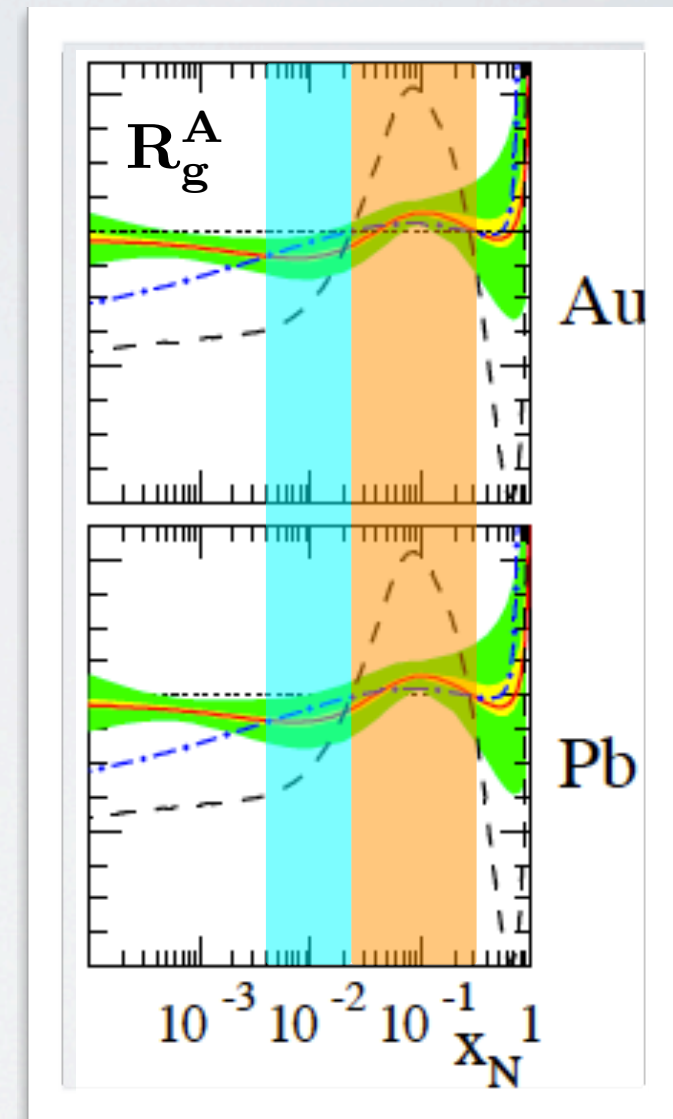
- can resolve characteristic differences between EPS and DSSZ gluons in anti-shadowing [and EMC] region



prompt photons – impact

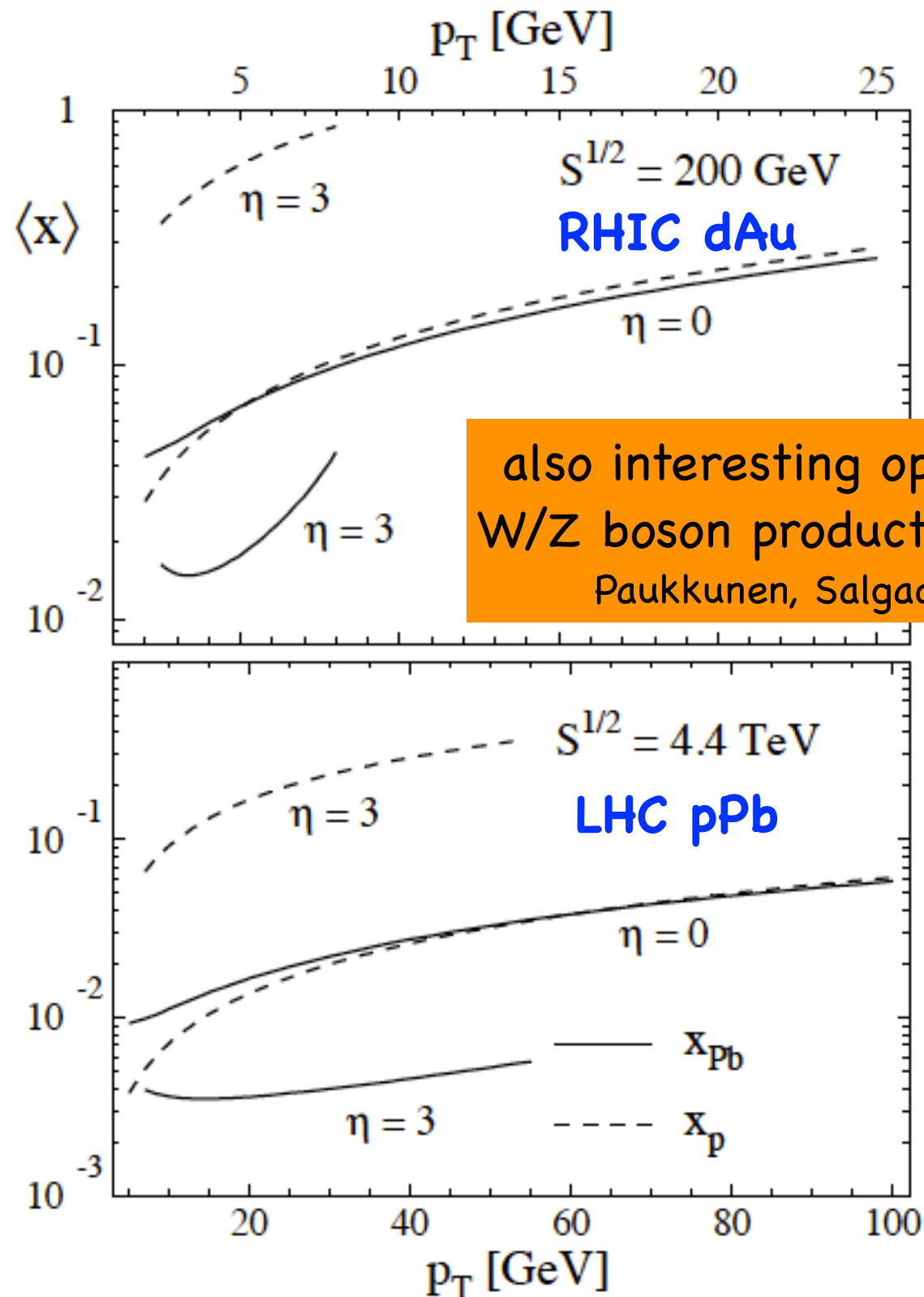


- can resolve characteristic differences between EPS and DSSZ gluons in anti-shadowing [and EMC] region



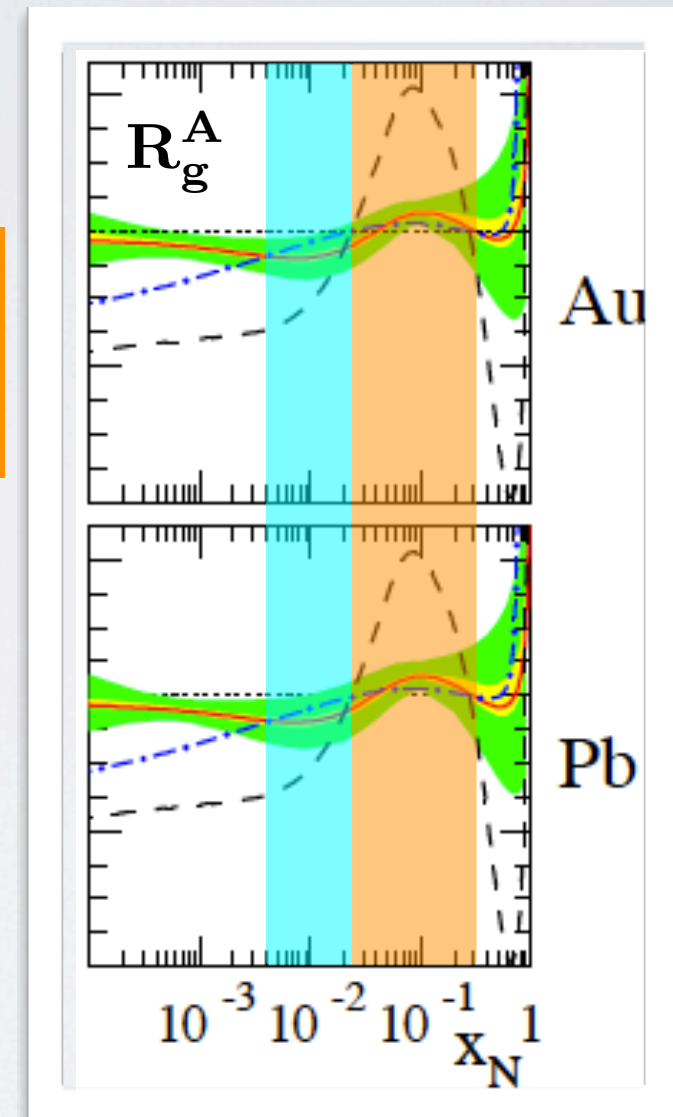
- can probe into shadowing region

prompt photons – impact



also interesting opportunities in
W/Z boson production at the LHC
Paukkunen, Salgado 1010.5392

- can resolve characteristic differences between EPS and DSSZ gluons in anti-shadowing [and EMC] region



- can probe into shadowing region

Drell Yan lepton pairs in dAu/pPb

LO $d\sigma_{DY}^{pA} \propto e_u^2 [u(x_1)\bar{u}^A(x_2) + \bar{u}(x_1)u^A(x_2)]$
 $+e_d^2 [d(x_1)\bar{d}^A(x_2) + \bar{d}(x_1)d^A(x_2)]$

$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$

Drell Yan lepton pairs in dAu/pPb

LO $d\sigma_{DY}^{pA} \propto e_u^2 [u(x_1)\bar{u}^A(x_2) + \bar{u}(x_1)u^A(x_2)]$
 $+ e_d^2 [d(x_1)\bar{d}^A(x_2) + \bar{d}(x_1)d^A(x_2)]$

large positive y

$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$

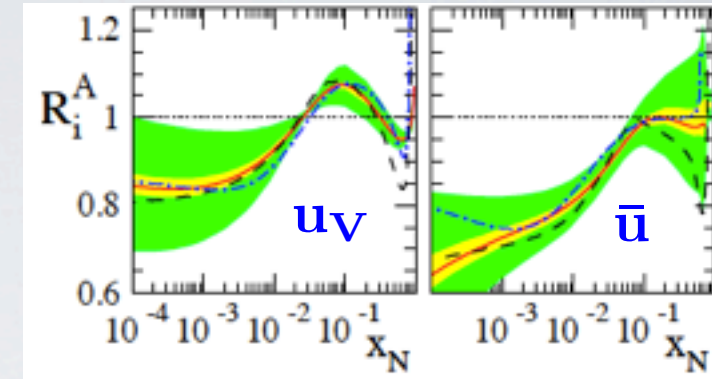
Drell Yan lepton pairs in dAu/pPb

LO $d\sigma_{DY}^{pA} \propto e_u^2 [u(x_1)\bar{u}^A(x_2) + \bar{u}(x_1)u^A(x_2)]$
 $+ e_d^2 [d(x_1)\bar{d}^A(x_2) + \bar{d}(x_1)d^A(x_2)]$

large positive y

large negative y

$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$



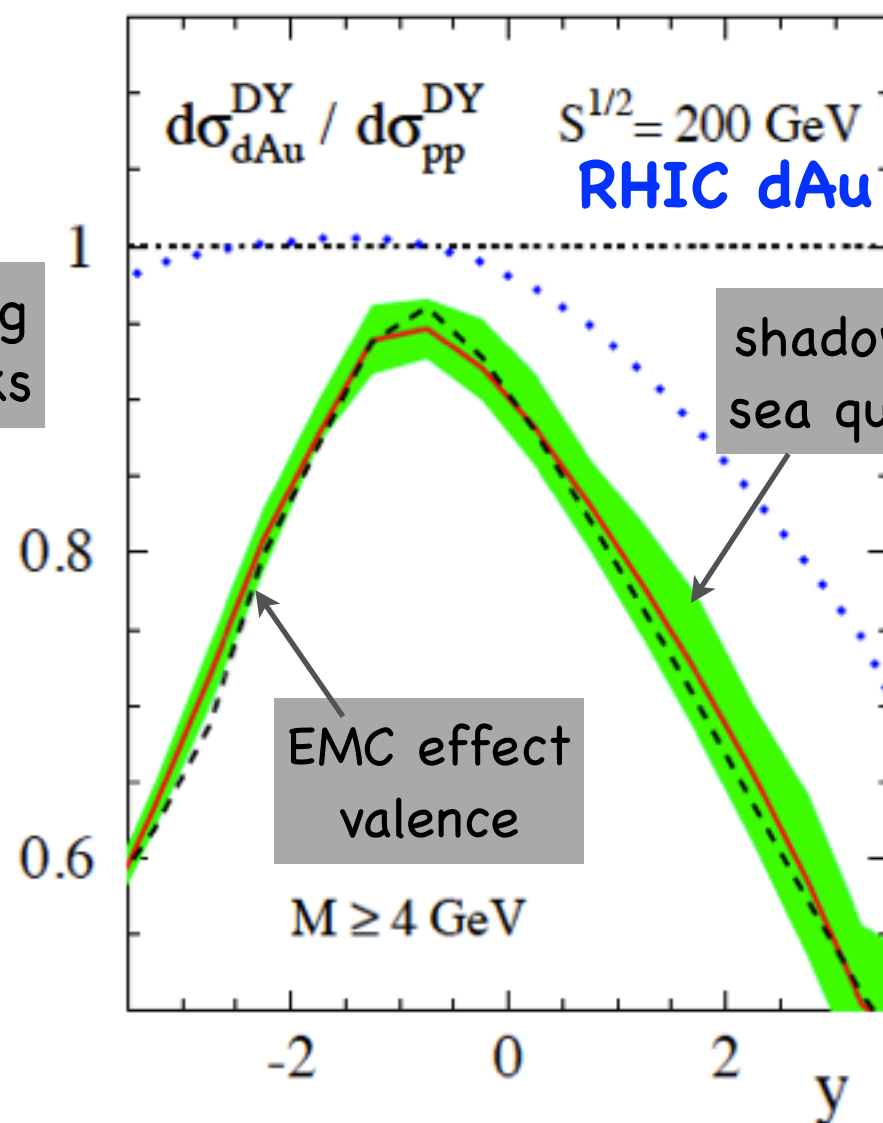
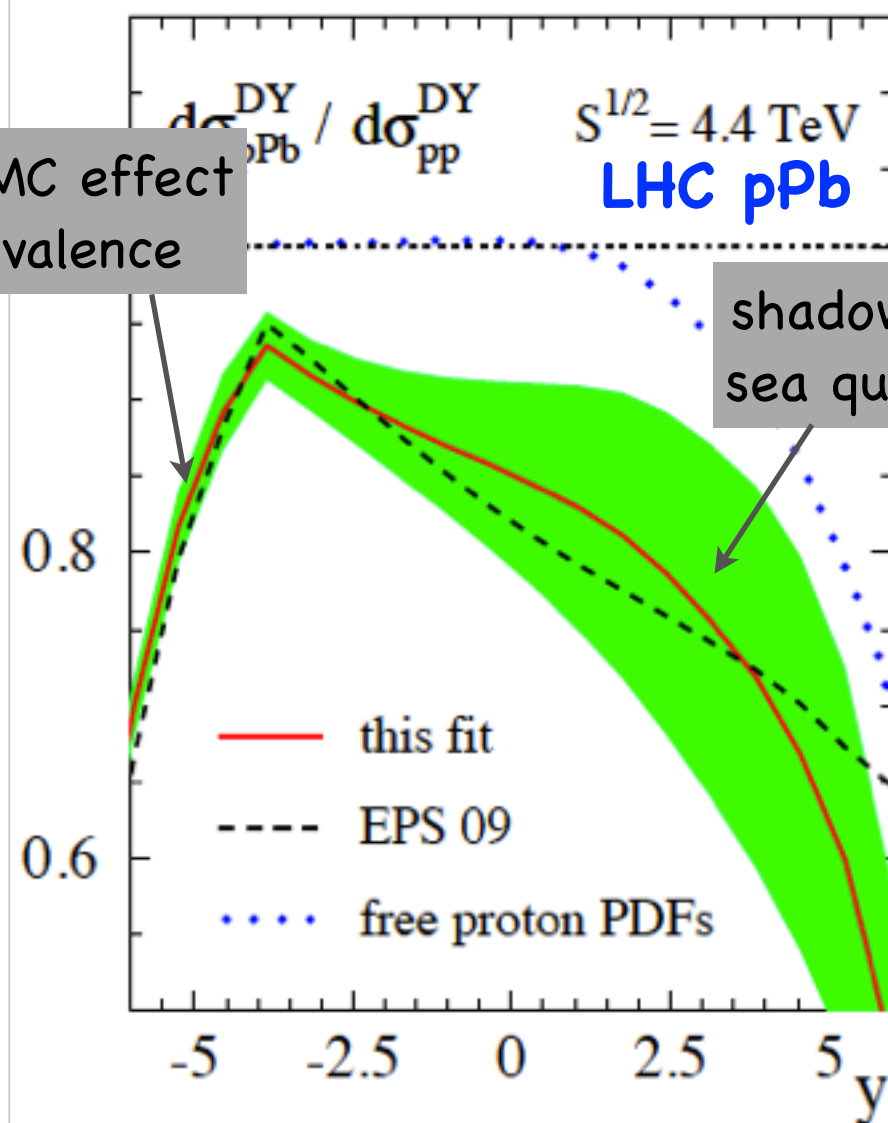
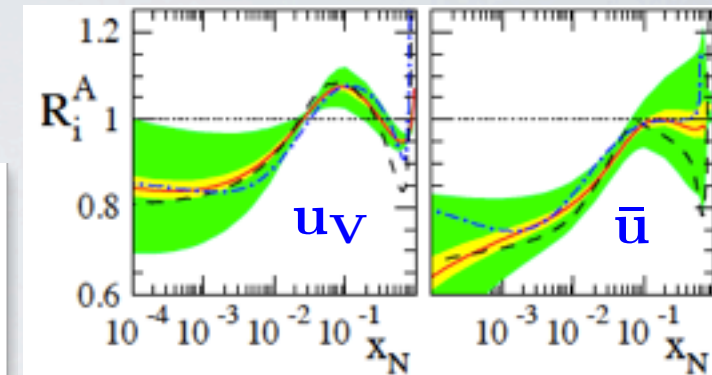
Drell Yan lepton pairs in dAu/pPb

LO $d\sigma_{DY}^{pA} \propto e_u^2 [u(x_1)\bar{u}^A(x_2) + \bar{u}(x_1)u^A(x_2)]$
 $+ e_d^2 [d(x_1)\bar{d}^A(x_2) + \bar{d}(x_1)d^A(x_2)]$

large positive y

large negative y

$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$



EMC effect
valence

shadowing
sea quarks

shadowing
sea quarks

EMC effect
valence

$M \geq 4 \text{ GeV}$

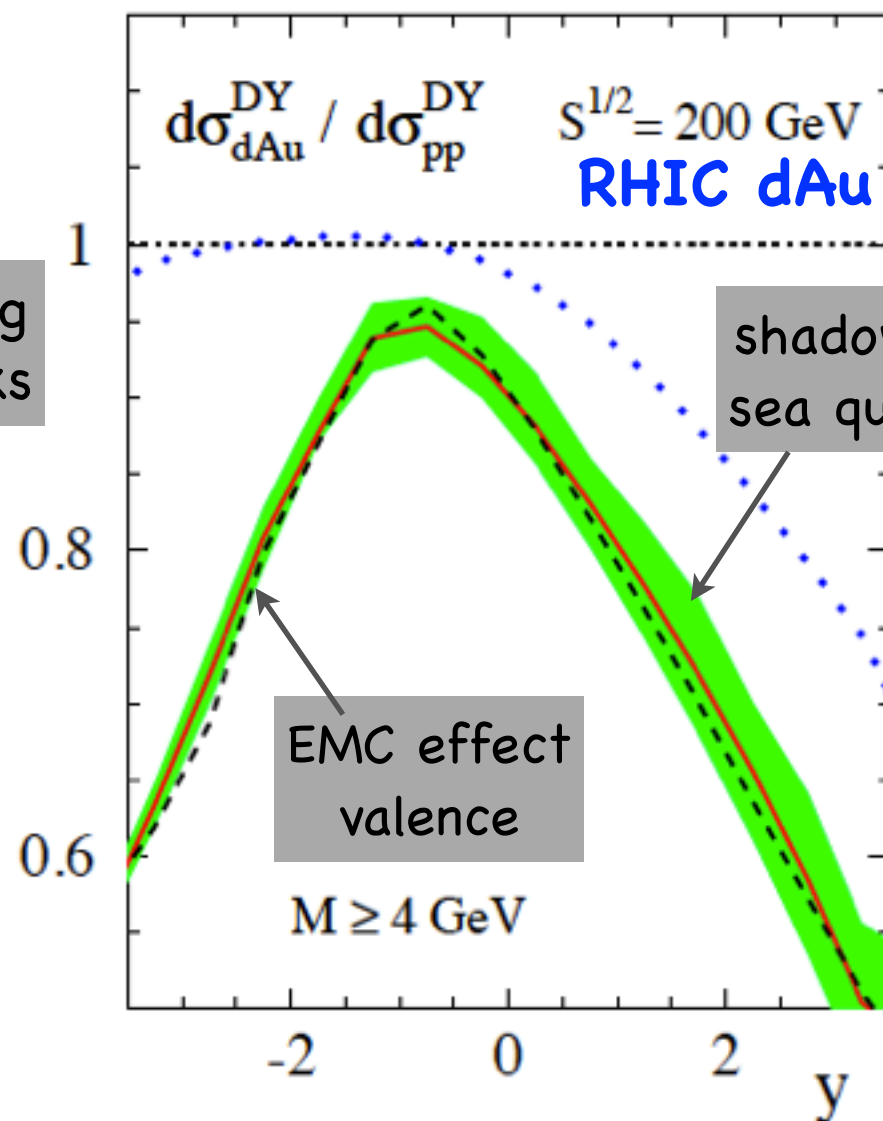
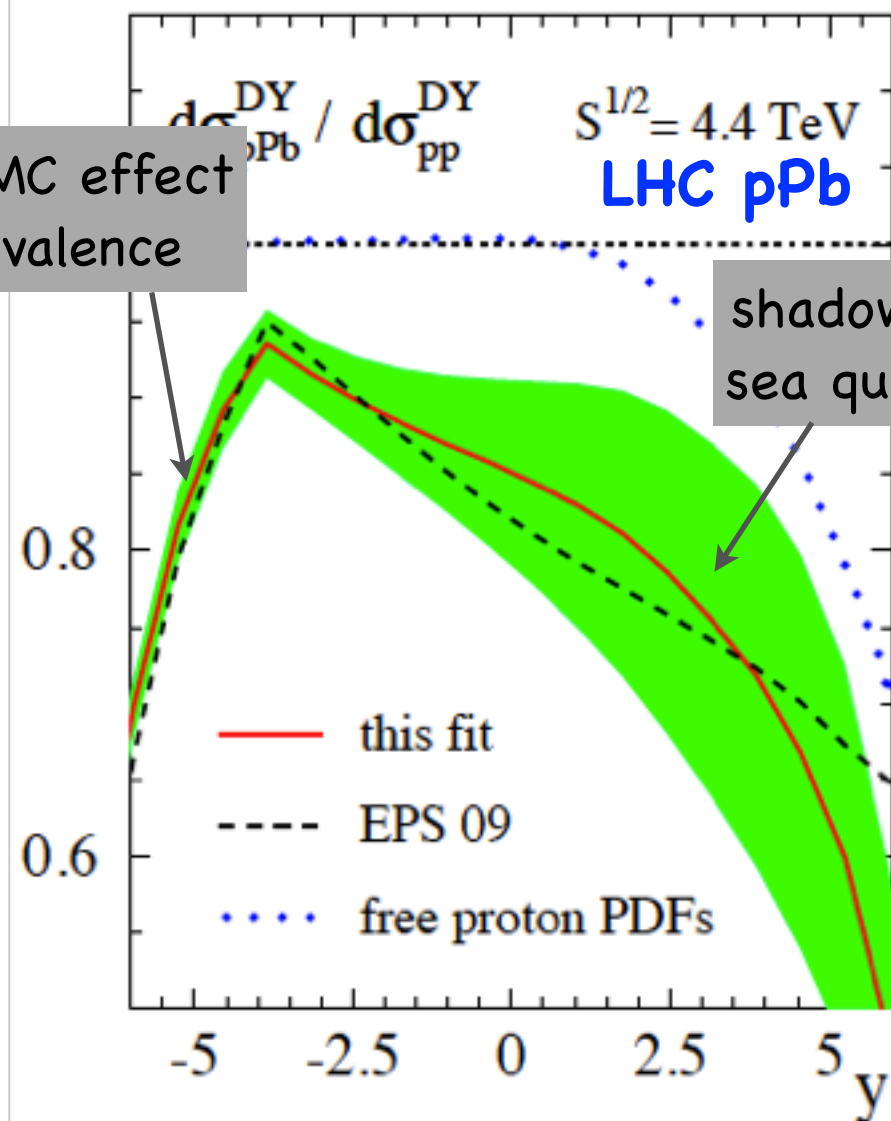
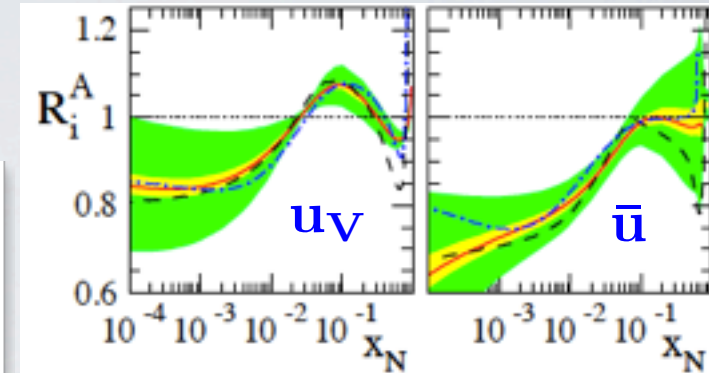
Drell Yan lepton pairs in dAu/pPb

LO $d\sigma_{DY}^{pA} \propto e_u^2 [u(x_1)\bar{u}^A(x_2) + \bar{u}(x_1)u^A(x_2)]$
 $+ e_d^2 [d(x_1)\bar{d}^A(x_2) + \bar{d}(x_1)d^A(x_2)]$

large positive y

large negative y

$$x_{1,2} = \sqrt{M^2/s} e^{\pm y}$$



x reach at $y=3$

RHIC: $x_2 \simeq 10^{-3}$

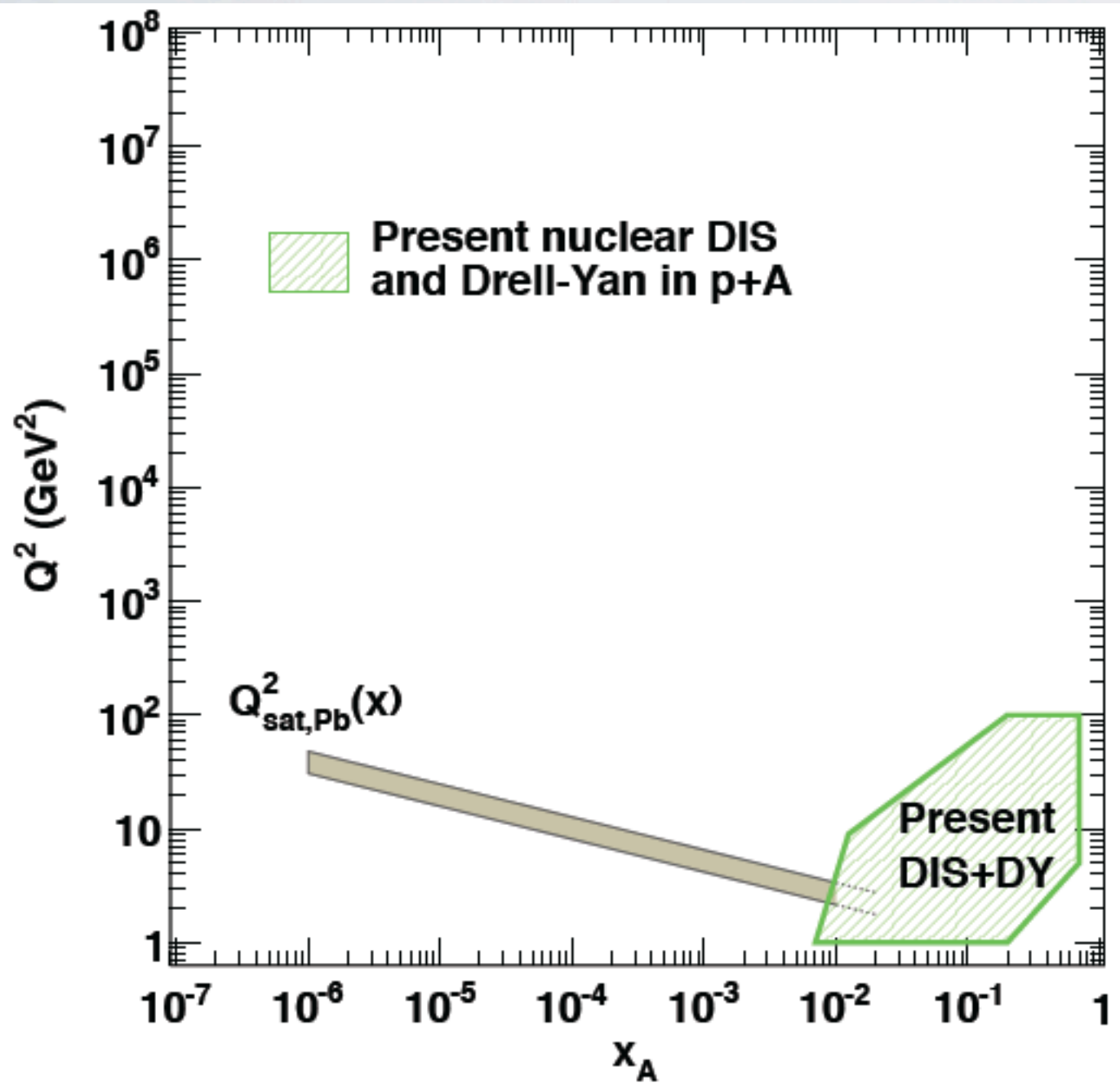
LHC: $x_2 \simeq 5 \times 10^{-5}$

potential of pPb @ LHC

first run scheduled for early 2013

see Salgado et al., 1105.3919

kinematic reach

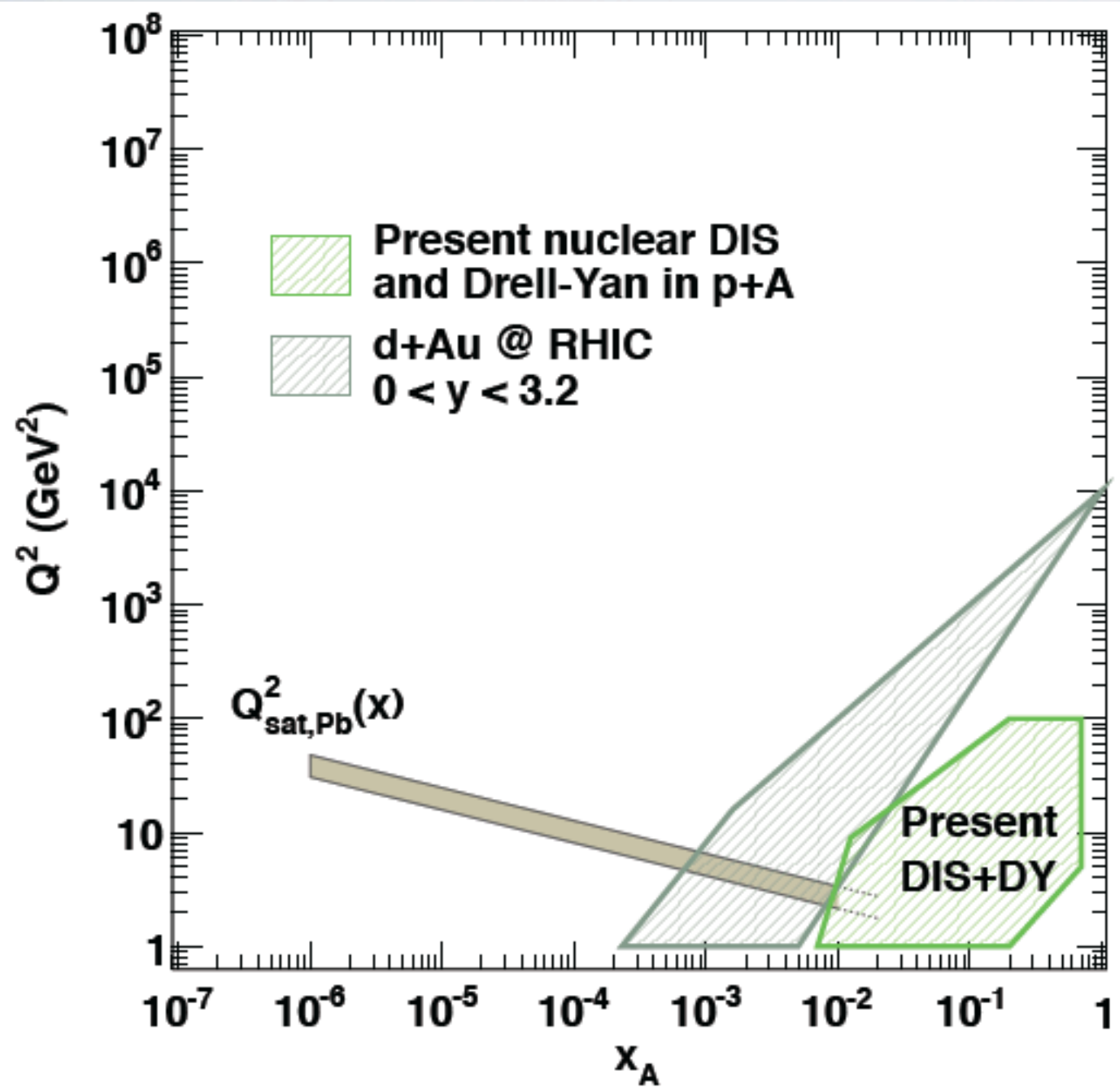


potential of pPb @ LHC

first run scheduled for early 2013

see Salgado et al., 1105.3919

kinematic reach

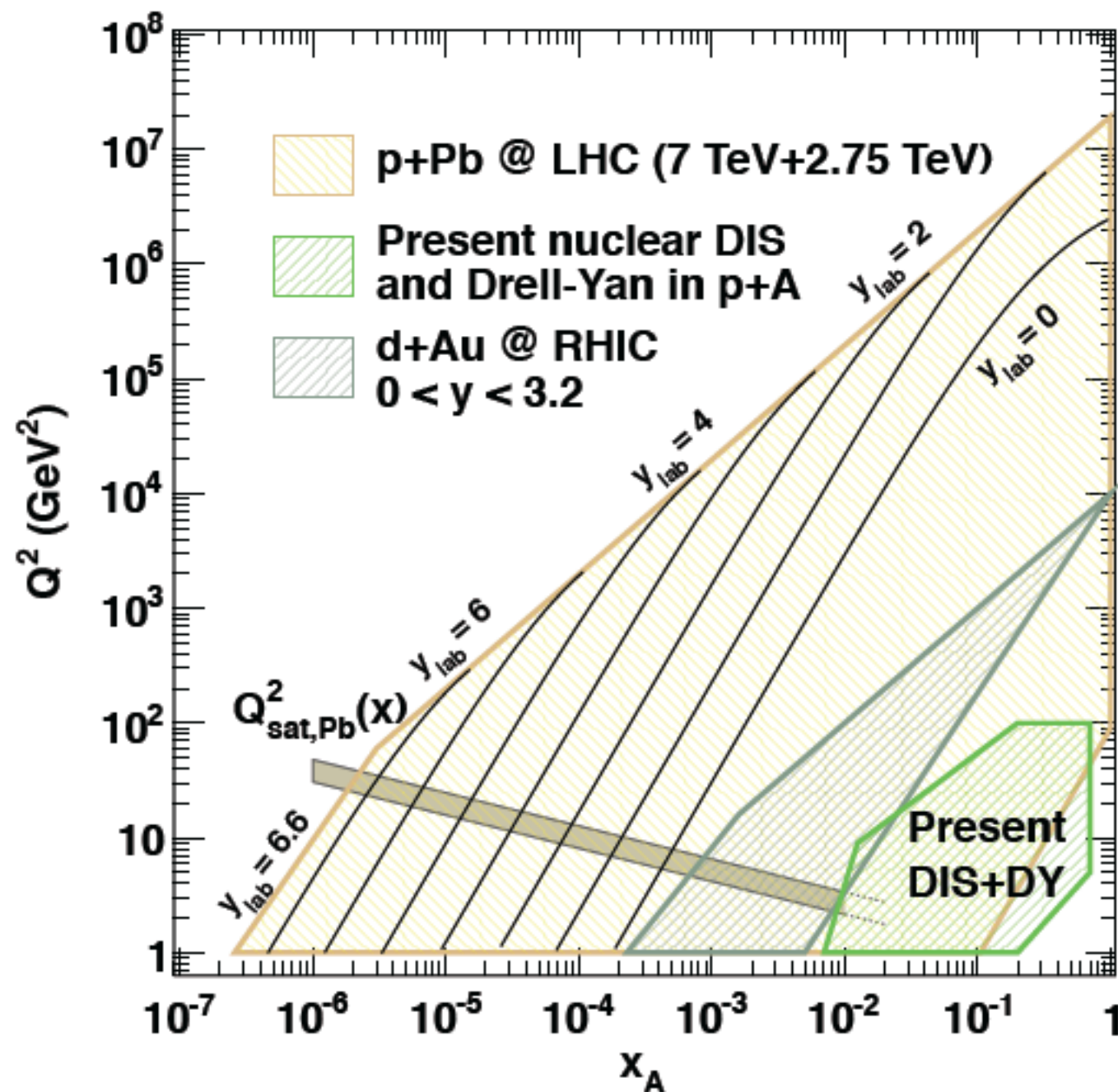


potential of pPb @ LHC

first run scheduled for early 2013

see Salgado et al., 1105.3919

kinematic reach

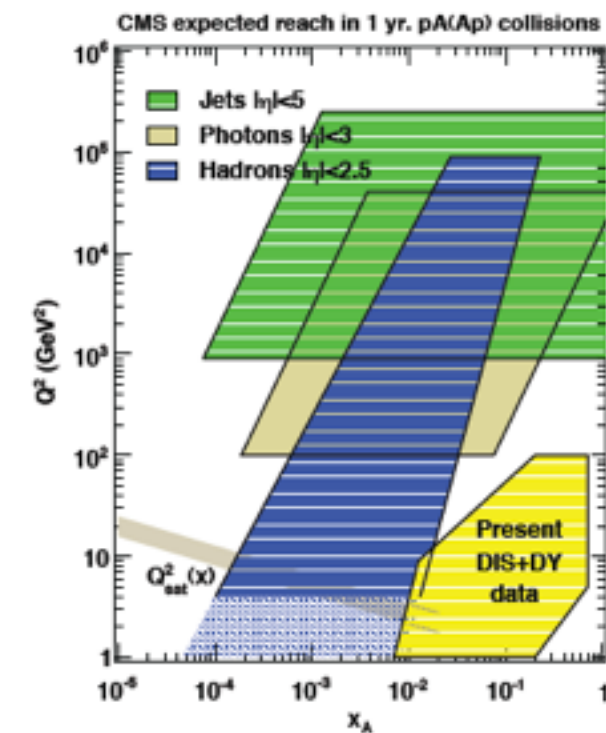
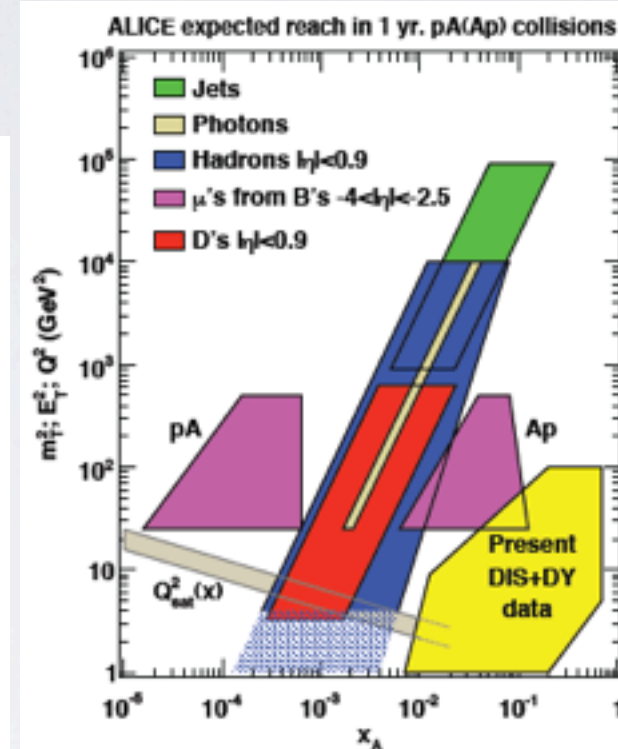
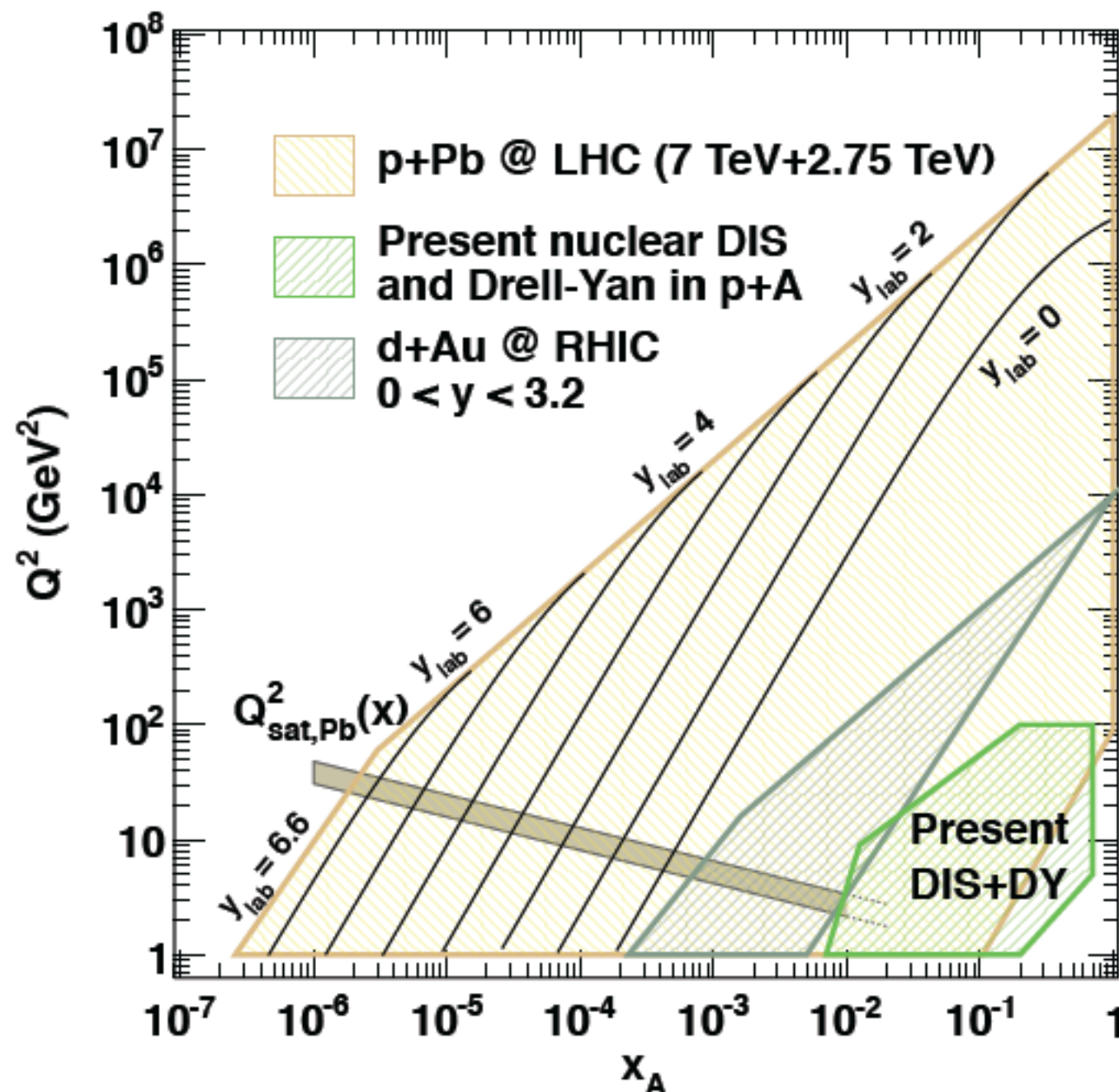


potential of pPb @ LHC

first run scheduled for early 2013

see Salgado et al., 1105.3919

kinematic reach



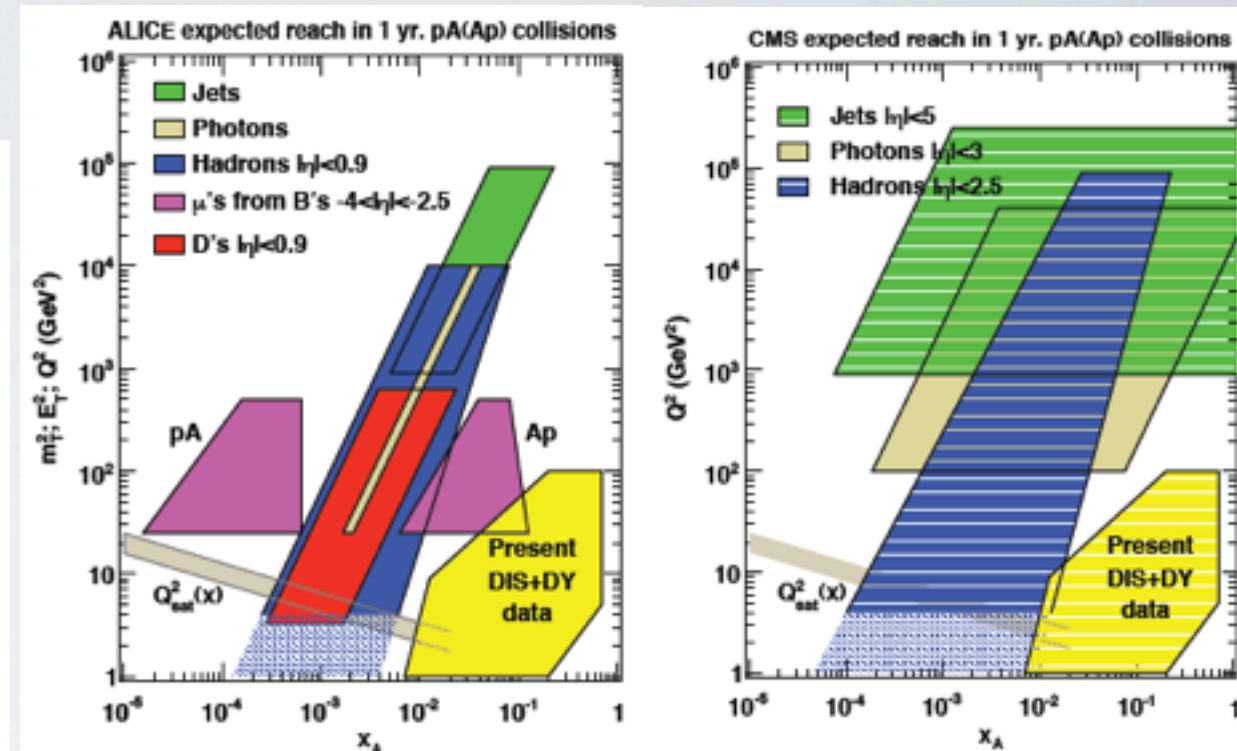
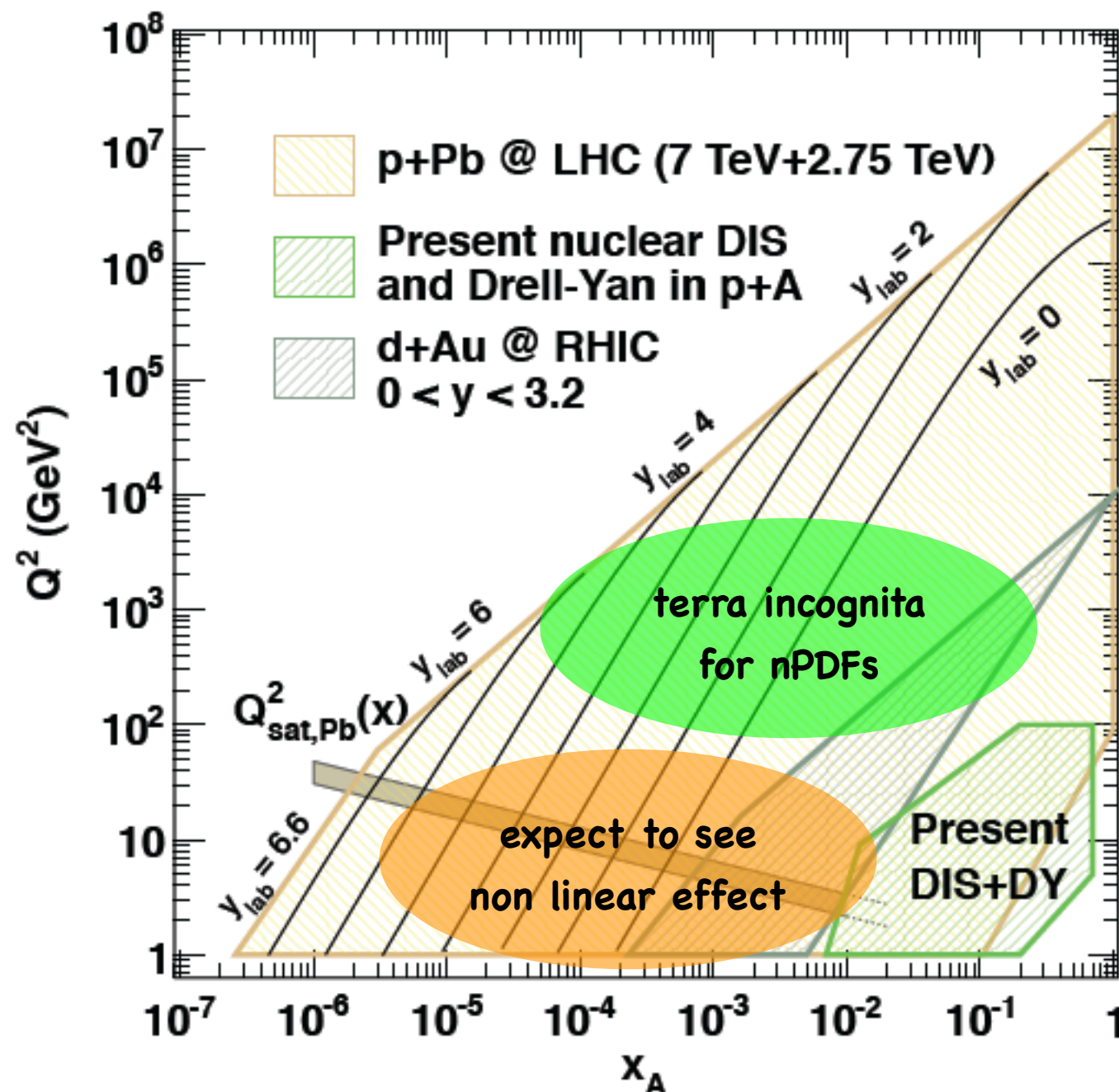
- ▶ small x already accessible at mid rapidity
- ▶ many conceivable probes

potential of pPb @ LHC

first run scheduled for early 2013

see Salgado et al., 1105.3919

kinematic reach



- ▶ small x already accessible at mid rapidity
- ▶ many conceivable probes

expect great impact on nPDF fits

take away message

- ❑ **first fully global QCD analysis of nuclear PDFs at NLO**
includes charged lepton DIS, neutrino DIS, Drell Yan, and dAu pion data
- ❑ **main observations**
no tension with neutrino DIS data (unlike in nCTEQ fit)
much more moderate modifications of gluon from RHIC data (unlike in EPS fit)
- ❑ **technical advances**
treatment of heavy quark mass effects
use of numerical efficient Mellin technique throughout
uncertainty estimates with improved Hessian method (eigenvector/error sets)
- ❑ **exciting prospects for upcoming LHC pPb and future RHIC runs**
impact of electromagnetic probes (prompt photons and Drell Yan)

more distant future: electron-ion collider (EIC/LHeC)

to study nPDFs, universality, factorization, and the transition to saturation with precision